

Therefore the impulse on the automobile due to the collision is $\vec{I} = \Delta \vec{p} = \vec{p}_{,-} - \vec{p}_{,i} = (3900 + 22500) \ kg \cdot m / s \\ = 26400 \ kg \cdot m / s = 2.64 \times 10^4 kg \cdot m / s$ The average force exerted on the automobile during the collision is $\vec{F} = \frac{\Delta \vec{p}}{\Delta t} = \frac{2.64 \times 10^4}{0.150} = 1.76 \times 10^5 \ N$ Read the rest of the example

Sample Problem

A pitched 140 g baseball, in horizontal flight with a speed v_i of 39.0 m/s, is struck by a bat. After leaving the bat, the ball travels in the opposite direction with speed v_f , also 39.0 m/s.

(a) What impulse I acts on the ball while it is in contact with the bat during the collision?

$$I = p_f - p_i = mv_f - mv_i$$

= (0.140 kg)(39.0 m/s) - (0.140 kg)(-39.0 m/s)
= 10.9 kg · m/s

Note that I is the impulse on the ball. The final direction of the ball is positive.



(b) The impact time Δt for the baseball-bat collision is 1.20 ms. What average force acts on the baseball?

$$F_{avg} = \frac{I}{\Delta t} = \frac{10.9 \ kg \cdot m \ /s}{0.00120 \ s} = 9080 \ N$$

Note that this average force is from the bat to the ball. The positive direction of the force is in the final velocity of the ball.

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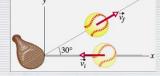
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(c) Now suppose the collision is not head-on, and the ball leaves the bat with a speed v_j of 45.0 m/s at an upward angle of 30.0°. What now is the impulse on the ball?

The impulse on the ball is:

$$\vec{I} = \Delta \vec{p} = \vec{p}_f - \vec{p}_i = m\vec{v}_f - m\vec{v}_i$$

$$I_x = p_{fx} - p_{ix} = m (v_{fx} - v_{ix})$$



= $(0.140 \text{ kg}) [(45.0 \text{ m/s})(\cos 30.0^{\circ}) - (-39.0 \text{ m/s})] = 10.92 \text{ kg} \cdot \text{m/s}$

$$I_{y} = p_{fy} - p_{iy} = m (v_{fy} - v_{iy})$$

 $= (0.140 \, kg) \left[(45.0 \, m \, / s) (\sin 30.0^{\circ}) - 0 \right]$

 $= 3.150 \, kg \cdot m \, / s$

 $\vec{I} = (10.9 \ \hat{i} + 3.15 \ \hat{j}) \ kg \cdot m \ / s$

$$I = \sqrt{I_x^2 + I_y^2} = 11.4 \text{ kg} \cdot m / s$$

$$\theta = \tan^{-1} \frac{I_y}{I_x} = 16^{\circ}$$

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Sample Problem

A ballot box with mass m = 6.0 kg slides with speed v = 4.0 m/s across a frictionless floor in the positive direction of an x axis. It suddenly explodes into two pieces. One piece, with mass $m_1 = 2.0$ kg, moves in the positive direction of the x axis with speed $v_1 = 8.0$ m/s. What is the velocity of the second piece, with mass m_2 ?

$$\vec{P}_{i} = m\vec{v}$$

$$\vec{P}_{f-1} = m_{1}\vec{v}_{1} \quad and \quad \vec{P}_{f-2} = m_{2}\vec{v}_{2}$$

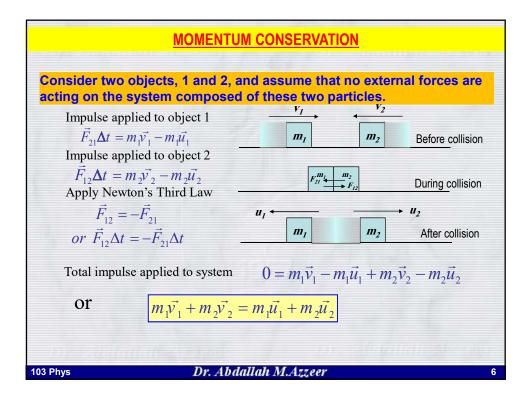
$$\vec{P}_{f} = \vec{P}_{f-1} + \vec{P}_{f-2} = m_{1}\vec{v}_{1} + m_{2}\vec{v}_{2}$$

$$P_{i} = P_{f}$$

$$mv = m_{1}v_{1} + m_{2}v_{2}$$

$$(6.0 kg)(4.0 m/s) = (2.0 kg)(8.0 m/s) + (4.0 kg)v_{2}$$

$$v_{2} = 2.0 m/s$$
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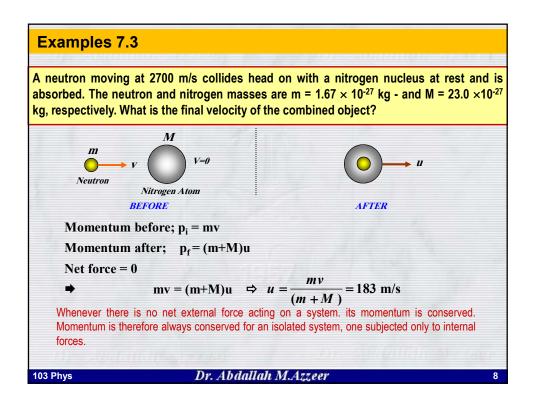


♦ Net momentum of the two objects before and after collision is the same

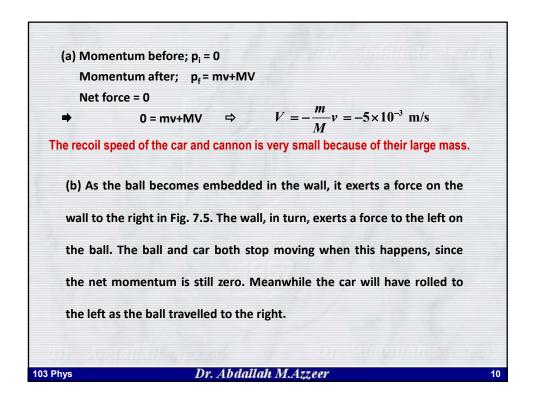
• THE TOTAL MOMENTUM OF THE SYSTEM IS CONSERVED

• For conservation of momentum, the external forces must be zero

In one dimension in component form, $m_1v_{1x} + m_2v_{2x} = m_1u_{1x} + m_2u_{2x}$ $m_1v_{1y} + m_2v_{2y} = m_1u_{1y} + m_2u_{2y}$ 103 Phys Dr. Abdallah M. Azzeer7



A cannon is mounted inside a railroad car, which is initially at rest but can move frictionlessly (Fig. 7.5). It fires a cannonball of mass m = 5 kg with a horizontal velocity v = 15 m/s relative to the ground at the opposite wall. The total mass of the cannon and railroad car is M = 15,000 kg. (Assume that the mass of the exhaust gases is negligible.) (a) What is the velocity V of the car while the cannonball is in flight? (b) If the cannonball becomes embedded in the wall, what is the velocity of the car and ball after impact? Li1103 Phys LECTURES SLIDESI103Phys_Slides_T1Y3839ICH9Flash **Dr. Abdallah M.Azzeer*** 9



Suppose that, after the cannonball strikes the far wall of the railroad car, both the cannonball and the railroad car move with common velocity U.

Conservation of momentum implies that the net horizontal momentum of the system is the same before and after the collision.

MV+mv=(M+m)U

However, we have already seen that mv+MV=0. It follows that U=0: in other words, the railroad car is brought to a complete halt when the cannonball strikes its far wall.

BUT

In the frame of reference of the railroad car, the cannonball moves with velocity (v-

V) after the cannon is fired. Hence, the time of flight of the cannonball if (L=10m)

is:
$$t = \frac{L}{v - V} = \frac{10}{15 - (-5 \times 10^{-3})} = 0.666 \text{ sec}$$

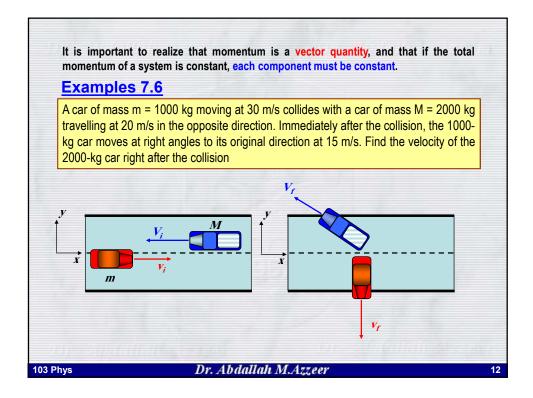
The distance moved by the railroad car in this time interval is d=Vt=-0.33 cm

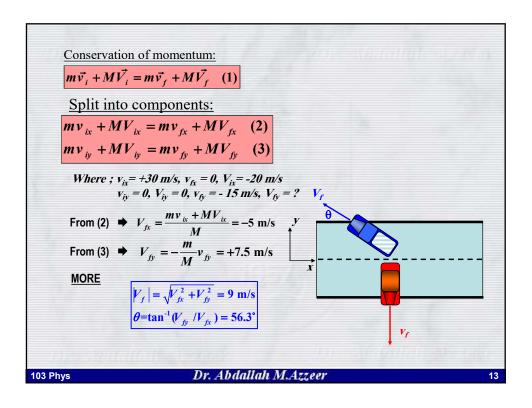
Thus, the railroad car moves 3.3 mm in the opposite direction to the direction of motion of the cannonball.

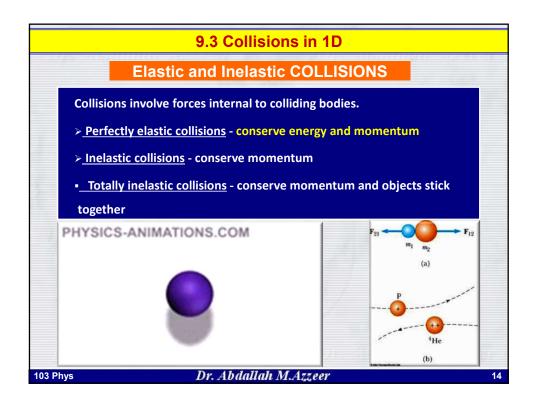
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