## CHAPTER 8

## Potential Energy and Conservation of Energy



Kinetic energy: Energy associated with motion
Potential energy: Energy associated with position

## Potential energy U:

$>$ Can be thought of as stored energy that can either do work or be converted to kinetic energy.
$>$ When work gets done on an object, its potential and/or kinetic energy increases.
$\Rightarrow$ There are different types of potential energy:

* Gravitational energy
* Elastic potential energy (energy in an stretched spring)
* Others (magnetic, electric, chemical, ...)


## Gravitational Potential Energy

Potential Energy $(\mathbf{P E}) \equiv$ Energy associated with position or configuration of a mass.

Consider a problem in which the height of a mass above the Earth changes from $y_{1}$ to $y_{2}$ :
$\mathbf{W}_{\text {grav }}=$ ?
$U P \Rightarrow W_{g}=-m g s=-m g\left(y_{2}-y_{1}\right)$
Down $\Rightarrow \mathrm{W}_{\mathrm{g}}=+\mathrm{mg} \mathrm{s}$

$$
\mathbf{W}_{g}=-m g\left(y_{2}-y_{1}\right)
$$



$$
\begin{aligned}
& \text { mgy } \equiv U_{g} \equiv \text { gravitational potential energy }(P E) \\
& \Rightarrow U_{2}-U_{1}=\Delta U \\
& \Rightarrow W_{g}=-m g\left(y_{2}-y_{1}\right)=U_{1}-U_{2}=-\Delta U_{g} \\
& \\
& \quad W_{g}=-\Delta U_{g}
\end{aligned}
$$

Changing the configuration of an interacting system requires work example: lifting a book
The change in potential energy is equal to the negative of the work done

$$
\Delta U_{g}=-W
$$

But Work/Kinetic Energy Theorem says: $W=\Delta K$

$$
\begin{gathered}
W=-\Delta U=\Delta K \\
\Delta K+\Delta U=0
\end{gathered}
$$

## Total Mechanical Energy

The change in potential energy is equal to the negative of the work done

## $\Delta U=-W$

But Work/Kinetic Energy Theorem says: $W=\Delta K$
$W=-\Delta U=\Delta K, \square \Delta K+\Delta U=0$
$\Delta K+\Delta U=0$
$K_{2}-K_{1}+U_{2}-U_{1}=0$
$K_{2}+U_{2}=K_{1}+U_{1}=$ constant $=E \equiv$ Total mechanical energy
NOTE that the ONLY forces is gravitational energy which doing the work
The sum of $K$ and $U$ for any state of the system = the sum of $K$ and $U$ for any other state of the system
In an isolated system acted upon only by conservative forces
Mechanical Energy is conserved

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## Example 8.1

A bowler drops bowling ball of mass 7 kg on his toe. Choosing floor level as $\mathrm{y}=\mathbf{0}$, estimate the total work done on the ball by the gravitational force as the ball falls.

Let's assume the top of the toe is 0.03 m from the floor and the hand was 0.5 m above the floor.
$U_{i}=m g y_{i}=7 \times 9.8 \times 0.5=34.3 \mathrm{~J}$
$U_{f}=m g y_{f}=7 \times 9.8 \times 0.03=2.06 \mathrm{~J}$
$W_{g}=-\Delta U=-\left(U_{f}-U_{i}\right)=32.24 \mathrm{~J} \cong 30 \mathrm{~J}$

| b) Perform the same calculation using the top of the bowler's head as the origin. <br> Assuming the bowler's height is 1.8 m |
| :--- |
| What has to change? |
| First we must re-compute the positions of ball at the hand and of the toe. |
| Assuming the bowler's height is 1.8 m , the ball's original position is -1.3 m, |
| and the toe is at -1.77 m. |
| $\qquad U_{i}=m g y_{i}=7 \times 9.8 \times(-1.3)=-89.2 \mathrm{~J}$ |
| $U_{f}=m g y_{f}=7 \times 9.8 \times(-1.77)=-121.4 \mathrm{~J}$ |
| $W_{g}=-\Delta U=-\left(U_{f}-U_{i}\right)=32.2 \mathrm{~J} \cong 30 \mathrm{~J}$ |
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## Conservative Forces

(a) A force is conservative if work done by that force acting on a particle moving between points is independent of the path the particle takes between the two points

(b) The total work done by a conservative force is zero when the particle moves around any closed path and returns to its initial position

## Conservative Forces

To repeat the idea on the last slide: We have seen that the work done by a conservative force does not depend on the path taken.

$$
\square W_{1}=W_{2}
$$

Therefore the work done in a closed path is 0 .

$$
\begin{aligned}
\square W_{N E T} & =W_{1}-W_{2} \\
& =W_{1}-W_{1}=0
\end{aligned}
$$




Non-conservative forces:
A force is non-conservative if it causes a change in mechanical energy; mechanical energy is the sum of kinetic and potential energy.
Example: Frictional force.
*This energy cannot be converted back into other forms of energy (irreversible).
Work does depend on path.
For straight line $W=-\boldsymbol{f} \boldsymbol{d}$
For semi-circle path $W=-f(\pi d / 2)$


Work varies depending on the path. Energy is dissipated

The presence of a non-conservative force reduces the ability of a system to do work (dissipative force)

## Energy dissipation: e.g. sliding friction

As the parts scrape by each other they start small-scale vibrations, which transfer energy into atomic motion

The atoms' vibrations go back and forththey have energy, but no average momentum. The increased atomic vibrations appear to us as a rise in the temperature of the parts. The temperature of an object is related to the thermal energy it has. Friction transfers some energy into thermal energy




| Three identical balls are thrown with the same initial speed from the top of a building. <br> Total Energy $\begin{gathered} E=K+U_{g}=\frac{1}{2} m v_{0}^{2}+m g h \\ A t y=0 \\ E=\frac{1}{2} m v^{2}=\frac{1}{2} m v_{0}^{2}+m g h \\ v=\sqrt{v_{0}^{2}+2 g h} \end{gathered}$ $\begin{gathered} v_{0}=v_{0} \cos \theta \hat{i}+v_{0} \sin \theta \hat{j} \\ \hat{i}: v_{x}=v_{0} \cos \theta \\ \hat{j}: v_{y}=v_{0} \sin \theta-g t \\ y=h+v_{0} \sin \theta \cdot t-\frac{1}{2} g t^{2}=0 \\ t=\frac{v_{0} \sin \theta+\sqrt{v_{0}^{2} \sin ^{2} \theta+2 g h}}{g} \\ v_{y}=-\sqrt{v_{0}^{2} \sin ^{2} \theta+2 g h} \\ v=\sqrt{v_{x}^{2}+v_{y}^{2}}=\sqrt{v_{0}^{2} \sin ^{2} \theta+2 g h+v_{0}^{2} \cos ^{2} \theta} \\ =\sqrt{v_{0}^{2}+2 g h} \end{gathered}$ |
| :---: |
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- READ Quick Quiz 8.7 \& 8.8

A ball connected to a massless spring suspended vertically. What forms of potential energy are associated with the ball-spring-Earth system when the ball is displaced downward?

## - READ Example 8.2

A ball is dropped from a height $h$ above the ground. Initially, the total energy of the ball-Earth system is potential energy, equal to mgh relative to the ground. At the elevation $y$, the total energy is the sum of the kinetic and potential energies.

## Example 8.3

Nose crusher?
A bowling ball of mass $m$ is suspended from the ceiling by a cord of length $L$. The ball is released from rest when the cord makes an angle $\theta_{A}$ with the vertical.
(a) Find the speed of the ball at the lowest point B.

(b) What is the tension $T_{B}$ in the cord at point $B$ ?
(c) The ball swings back. Will it crush the operator's nose?

## Example 8.4

(a) An actor uses some clever staging; to make his entrance.
$M_{\text {actor }}=65 \mathrm{~kg}, M_{\text {bag }}=130 \mathrm{~kg}, \mathrm{R}=3 \mathrm{~m}$
What is the max. value of $\theta$ can have before sandbag lifts of the floor?
(b) Free-body diagram for actor at the bottom of the circular path. (c) Free-body diagram for sandbag.

$$
\begin{aligned}
& K_{f}+U_{f}=K_{i}+U_{i} \\
& \frac{1}{\mathbf{2}} M_{\text {actor }} v_{f}^{2}+0=0+M_{\text {actor }} g y_{i} \\
& \boldsymbol{y}_{i}=\boldsymbol{R}-\boldsymbol{R} \cos \theta=\boldsymbol{R}(\mathbf{1}-\cos \theta)
\end{aligned}
$$

$$
v_{f}^{2}=2 g R(1-\cos \theta)
$$

How we can obtain v ????

$$
\sum F_{y}=T-M_{a c t o r} g=M_{\text {actor }} \frac{v_{f}^{2}}{R}
$$

$$
\Rightarrow T=M_{a c t o r} g+M_{a c t o r} \frac{v_{f}^{2}}{R}
$$

For the sandbag not to move $\Rightarrow a=0 \Rightarrow T=M_{\text {bag }} g$

$$
\theta=60^{\circ}
$$


^- سقطت كرة كتلتها 200 من ارتفاع 4 m على أرض مستوية فارتدت الى ارتفاع m 4 m 2.5 ، الطاقة الحركية
(a) 2.95 J
(b) 4.90 J
(c) 7.85 J
(d) 12.70 J

Q- تبدا سيارة كتلتها 1500 kg في الحركة الي أسفل من قمة مرتفع بسرعة 30 m/s 30 وتصل الى الأسفل ثم تصعد المى أعلى قمة مرتفع آخروتصل اليه بسرعة 20 m/s ، إذا كانت قمتي المرتفعين متساوية فإن الشغل المبذول بواسطة قوة الاحتكاك تساوي:

(a) $\mathbf{2 0 0 , 0 0 0 ~ J}$
(b) $400,000 \mathrm{~J}$
(c) $\mathbf{4 5 0 , 0 0 0} \mathrm{J}$
(d) $500,000 \mathrm{~J}$

- ا شاحنة كتلتها ثلاثة أضعاف كتلة سيارة وتتحرك ضعف سرعة السيارة • إذا كانت K تمثل الطاقة الحركية للسيارة فإن الطاقة الحركية للشاحنة هي:
(a) K
(b) 6 K
(c) 12 K
(d) 24 K

