

CHAPTER 6

قانون حفظ الطاقة

Conservation of Energy

- One form of energy can be converted into another form of energy.
- Conservative and non-conservative forces



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Kinetic energy: Energy associated with *motion*

Potential energy: Energy associated with *position*

Potential energy U:

- Can be thought of as stored energy that can either do work or be converted to kinetic energy.
- When work gets done on an object, its potential and/or kinetic energy increases.
- ⇒ There are different types of potential energy:
 - ✿ Gravitational energy
 - ✿ Elastic potential energy (energy in a stretched spring)
 - ✿ Others (magnetic, electric, chemical, ...)

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Gravitational Potential Energy

Potential Energy (PE) = Energy associated with position or configuration of a mass.

Consider a problem in which the height of a mass above the Earth changes from y_1 to y_2 :

$W_{\text{grav}}=?$

UP $\rightarrow W_g = -mg s = -mg (y_2 - y_1)$

Down $\rightarrow W_g = +mg s$

$W_g = -mg (y_2 - y_1)$

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$mg y \equiv U_g \equiv \text{gravitational potential energy (PE)}$

$\rightarrow U_2 - U_1 = \Delta U$

$\rightarrow W_g = -mg (y_2 - y_1) = U_1 - U_2 = -\Delta U_g$

$W_g = -\Delta U_g$

Changing the configuration of an interacting system requires work
example: lifting a book

The change in potential energy is equal to the negative of the work done

$\Delta U_g = -W$

But Work/Kinetic Energy Theorem says: $W = \Delta K$

$W = -\Delta U = \Delta K$

$\Delta K + \Delta U = 0$

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Total Mechanical Energy

The change in potential energy is equal to the negative of the work done

$$\Delta U = -W$$

But Work/Kinetic Energy Theorem says: $W = \Delta K$

$$W = -\Delta U = \Delta K \quad \Rightarrow \quad \Delta K + \Delta U = 0$$

$$\Delta K + \Delta U = 0$$

$$K_2 - K_1 + U_2 - U_1 = 0$$

$$K_2 + U_2 = K_1 + U_1 = \text{constant} = E \equiv \text{Total mechanical energy}$$

NOTE that the ONLY forces is gravitational energy which doing the work

The sum of K and U for any state of the system = the sum of K and U for any other state of the system

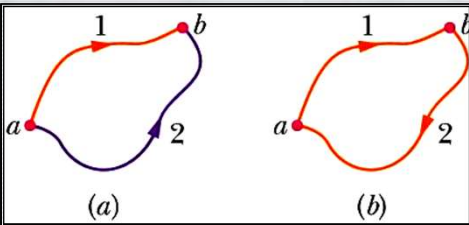
In an isolated system acted upon only by conservative forces

Mechanical Energy is conserved

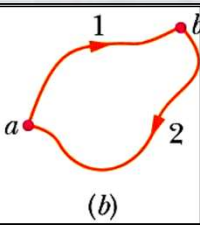
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Conservative Forces

(a) A force is conservative if work done by that force acting on a particle moving between points is **independent** of the path the particle takes between the two points



(a)



(b)

(b) The total work done by a **conservative force** is **zero** when the particle moves around any **closed path** and returns to its initial position

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Work done by gravity

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- $W_g = \mathbf{F} \cdot \Delta \mathbf{r} = mg \Delta r \cos \theta = mg h$
 $W_g = mgh$ (Depends only on h!)

$$W_{NET} = W_1 + W_2 + \dots + W_n$$

$$= \mathbf{F} \cdot \Delta \mathbf{r}_1 + \mathbf{F} \cdot \Delta \mathbf{r}_2 + \dots + \mathbf{F} \cdot \Delta \mathbf{r}_n$$

$$= \mathbf{F} \cdot (\Delta \mathbf{r}_1 + \Delta \mathbf{r}_2 + \dots + \Delta \mathbf{r}_n)$$

$$= \mathbf{F} \cdot \Delta \mathbf{r}$$

$$= Fh$$

$W_g = mgh$

**Depends only on h,
not on path taken!**

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Non-conservative forces:

A force is non-conservative if it causes a change in mechanical energy; mechanical energy is the sum of kinetic and potential energy.

Example: Frictional force.

- ✳ This energy cannot be converted back into other forms of energy (irreversible).
- ✳ Work does depend on path.

For straight line $W = -f d$

For semi-circle path $W = -f(\pi d / 2)$

Work varies depending on the path. Energy is dissipated

The presence of a non-conservative force reduces the ability of a system to do work (*dissipative force*)

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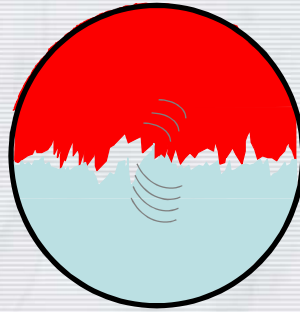
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Energy dissipation: e.g. sliding friction

As the parts scrape by each other they start small-scale vibrations, which transfer energy into atomic motion

The atoms' vibrations go back and forth—they have energy, but no average momentum. The increased atomic vibrations appear to us as a rise in the temperature of the parts. The temperature of an object is related to the thermal energy it has. Friction transfers some energy into thermal energy



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When there is **NO** work done by **APPLIED FORCES**, the total mechanical energy is constant or **CONSERVED**

If $W_a \neq 0 \rightarrow$

$$K_2 + U_2 = K_1 + U_1 + W_a$$

OR

$$\Delta K + \Delta U = W_{nc}$$

W_{nc} = work done by **ANY** other forces than gravitational force spring forces (e.g. any applied non-conservative force or frictional force)

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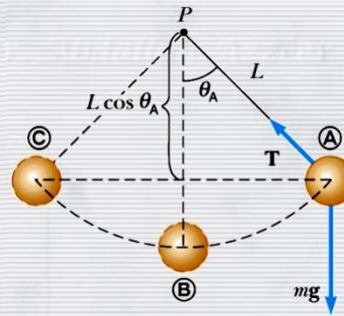
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Example 8.3

Nose crusher?

A bowling ball of mass m is suspended from the ceiling by a cord of length L . The ball is released from rest when the cord makes an angle θ_A with the vertical.



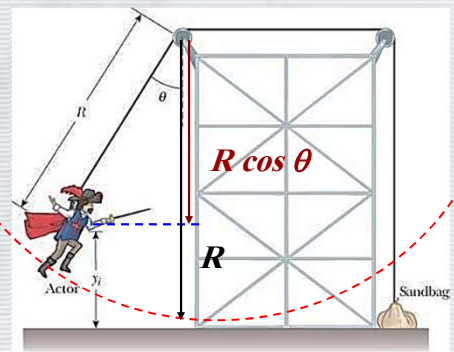
- (a) Find the speed of the ball at the lowest point B.
- (b) What is the tension T_B in the cord at point B?
- (c) The ball swings back. Will it crush the operator's nose?

Example

(a) An actor uses some clever staging to make his entrance.

$M_{actor} = 65 \text{ kg}$, $M_{bag} = 130 \text{ kg}$, $R = 3 \text{ m}$

What is the max. value of θ can have before sandbag lifts of the floor?

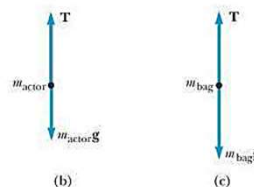


(b) Free-body diagram for actor at the bottom of the circular path. (c) Free-body diagram for sandbag.

$$K_f + U_f = K_i + U_i$$

$$\frac{1}{2} M_{actor} v_f^2 + 0 = 0 + M_{actor} g y_i$$

$$y_i = R - R \cos \theta = R(1 - \cos \theta)$$



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$$v_f^2 = 2gR(1 - \cos\theta)$$

How we can obtain v ????

$$\sum F_y = T - M_{\text{actor}} g = M_{\text{actor}} \frac{v_f^2}{R}$$

$$\Rightarrow T = M_{\text{actor}} g + M_{\text{actor}} \frac{v_f^2}{R}$$

For the sandbag not to move $\Rightarrow a=0 \Rightarrow T=M_{\text{bag}}g$

$$\theta = 60^\circ$$

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Example

$m=3 \text{ kg}$, $d=1 \text{ m}$, $\theta=30^\circ$,
 $v_i=0$, $f_k=5 \text{ N}$, $h=0.5 \text{ m}$,
 $v_f=?$

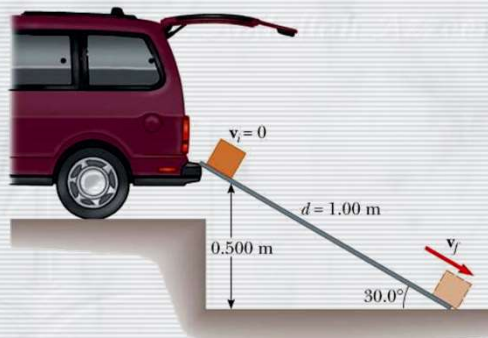
$$\Delta K + \Delta U = W_{nc}$$

$$K_f - K_i + U_f - U_i = W_{f_k}$$

$$\frac{1}{2}mv_f^2 - 0 + 0 - mgh = -f_k d$$

$$v_f = \sqrt{\frac{2}{m}(mgh - f_k d)} = 2.54 \text{ m/s}$$

What happen when you don't know h ?



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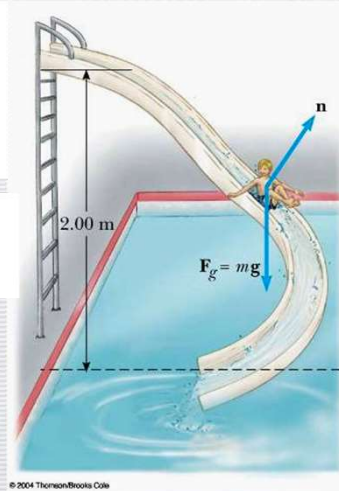
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Example 8.6

A child of mass m rides on an irregularly curved slide of height $h = 2.00$ m, as shown in Figure 8.12. The child starts from rest at the top.

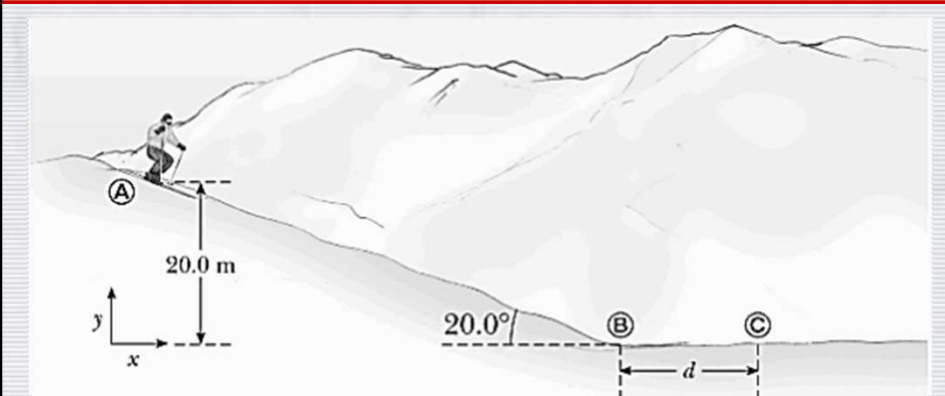
(A) Determine his speed at the bottom, assuming no friction is present.

(B) If a force of kinetic friction acts on the child, how much mechanical energy does the system lose? Assume that $v_f = 3.00$ m/s and $m = 20.0$ kg.

**example**

A skier starts from rest at the top of a frictionless incline of height 20.0 m, as shown. At the bottom of the incline, he encounters a horizontal surface where the coefficient of kinetic friction between the skis and the snow is 0.210.

(a) How far does he travel on the horizontal stretch.



$$\Delta E = 0 = \Delta K + \Delta U$$

$$mgh = \frac{1}{2}mv^2$$

$$v = \sqrt{2gh}$$

$$v = \sqrt{2 \times 9.8 \times 20.0} = 19.8 \text{ m/s}$$

$$\Delta K = K_f - K_i = -f_k d$$

Since $K_f = 0$ $-K_i = -f_k d$; $f_k d = K_i$

$$f_k = \mu_k n = \mu_k mg$$

$$d = \frac{K_i}{\mu_k mg} = \frac{\frac{1}{2}mv^2}{\mu_k mg} = \frac{v^2}{2\mu_k g} = \frac{(19.8)^2}{2 \times 0.210 \times 9.80} = 95.2 \text{ m}$$

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MINI REVIEW: WORK – KE – PE

Work done by constant force: $W = \mathbf{F} \cdot \mathbf{d} = Fd \cos\theta$

e.g. Work done by gravity: $W_g = -mg \Delta y$

Change in gravitational PE: $\Delta U_g = -W_g = mg \Delta y$

Work – Energy Thm: $\Sigma W_{non-con} = \Delta E_{mech} = \Delta K + \Delta U$

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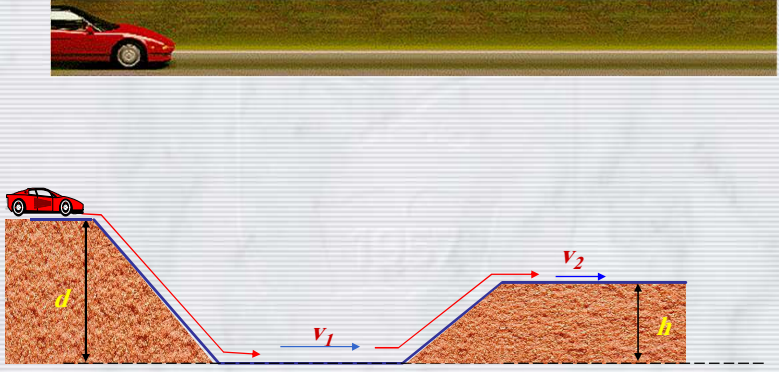
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Example : Hotwheel

A toy car slides on the frictionless track shown below. It starts at rest, drops a distance d , moves horizontally at speed v_1 , rises a distance h , and ends up moving horizontally with speed v_2 .

Find v_1 and v_2 .

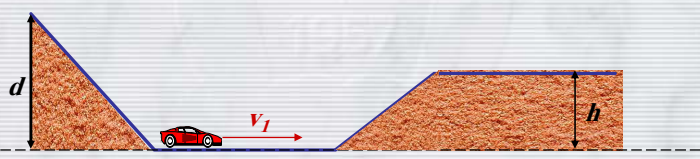


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- **K+U energy is conserved, so $\Delta E = 0$**

$$\Delta K = -\Delta U$$
- **Moving down a distance d ,**

$$\Delta U = -mgd, \quad \Delta K = \frac{1}{2}mv_1^2 \quad \Rightarrow$$
- **Solving for the speed:**

$$v_1 = \sqrt{2gd}$$


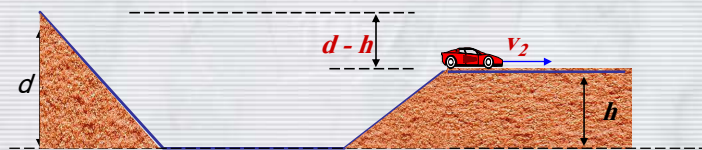
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- At the end, we are a distance $d - h$ below our starting point.

$$\Delta U = -mg(d - h), \quad \Delta K = \frac{1}{2}mv_2^2$$

Solving for the speed:

$$v_2 = \sqrt{2g(d - h)}$$



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Example:

With what speed does the weight have just before contact with the nail?

$$\Delta K + \Delta U = 0$$

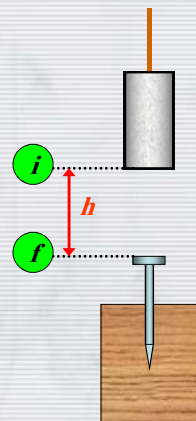
$$U_i = mgh$$

$$U_f = 0$$

$$K_i = 0$$

$$K_f = \frac{1}{2}mv^2$$

$$v = \sqrt{2gh}$$



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What is the force of resistance between the nail and the block?

$$\Delta K + \Delta U = W_{nc} = -fd$$

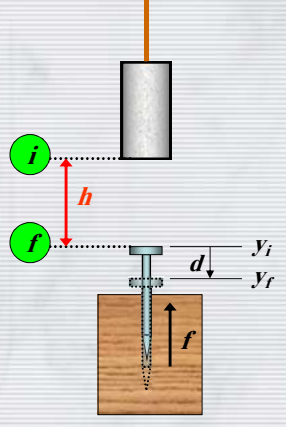
$$U_i = 0$$

$$U_f = -mgd$$

$$K_i = mgh$$

$$K_f = 0$$

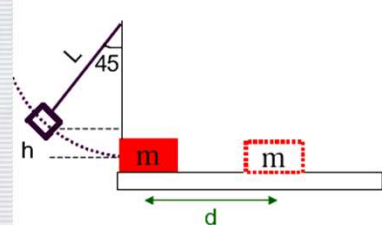
Solve you get

$$f = mg \left(\frac{h+d}{d} \right)$$


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Using Energy to Find Resistive Forces
Pendulum & Sliding Block

What is the work done by friction?



$$KE_i = KE_f = 0$$

$$U_i = mgh$$

$$= mgL(1 - \cos \theta)$$

$$U_f = 0$$

$$\Delta KE + \Delta U = W_{nc}$$

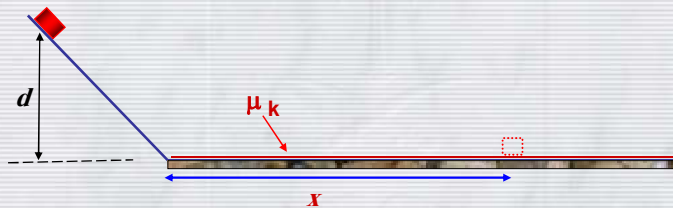
$$W_{nc} = \Delta U = mgL(1 - \cos \theta) = -fd$$

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Example;

A block slides down a frictionless ramp. Suppose the horizontal (bottom) portion of the track is rough, such that the coefficient of kinetic friction between the block and the track is μ_k .

How far, x , does the block go along the bottom portion of the track before stopping?



Using $W_{nc} = \Delta K + \Delta U$

As before, $\Delta U = -mgd$

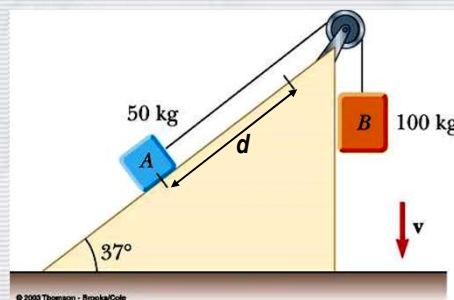
W_{nc} = work done by friction = $-\mu_k mgx$.

$\Delta K = 0$ since the block starts out and ends up at rest.

$W_{nc} = \Delta U \Rightarrow -\mu_k mgx = -mgd \Rightarrow x = d / \mu_k$

Example

Two blocks, A and B ($m_A = 50 \text{ kg}$ and $m_B = 100 \text{ kg}$), are connected by a string as shown. If the blocks begin at rest, what will their speeds be after A has slid a distance $d = 0.25 \text{ m}$? Assume the pulley and incline are frictionless.



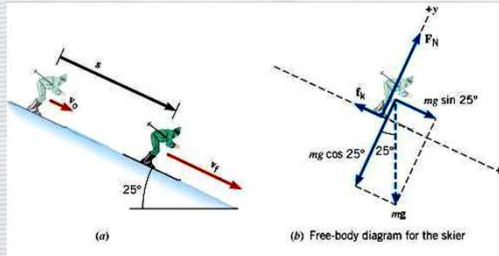
ANS: 1.51 m/s

Example:

A skier ($m=58 \text{ kg}$) is traveling down a 25 degree slope. His skis against the snow exert a frictional force of 70 N. He starts out with a velocity of 3.6 m/s. What velocity does he end up with after traveling 57 m downhill?

What is the net force along the direction of the displacement?

$$\sum F_s = mg \sin \theta + (-70 \text{ N})$$



$$W = \sum F_s \times s = \frac{1}{2} m v^2 - \frac{1}{2} m v_0^2$$

$$[mg \sin \theta + (-70 \text{ N})] \times s = \frac{1}{2} m v^2 - \frac{1}{2} m v_0^2$$

From this, we can solve for v!

Energy Loss in Automobile

Automobile uses only at 13% of its fuel to propel the vehicle.

Why?

67% in the engine:

1. Incomplete burning
2. Heat
3. Sound

16% in friction in mechanical parts

4% in operating other crucial parts such as oil and fuel pumps, etc

13% used for balancing energy loss related to moving vehicle, like air resistance and road friction to tire, etc

Two frictional forces involved in moving vehicles $m_{car} = 1450 \text{ kg}$ Weight $= mg = 14200 \text{ N}$

Coefficient of Rolling Friction; $\mu = 0.016$ $\mu n = \mu mg = 227 \text{ N}$

Air Drag $f_a = \frac{1}{2} D \rho A v^2 = \frac{1}{2} \times 0.5 \times 1.293 \times 2v^2 = 0.647v^2$ **Total Resistance** $f_t = f_r + f_a$

Total power to keep speed $v=26.8 \text{ m/s}=60 \text{ mi/h}$ $P = f_t v = (691 \text{ N}) \cdot 26.8 = 18.5 \text{ kW}$

Power to overcome each component of resistance $P_r = f_r v = (227) \cdot 26.8 = 6.08 \text{ kW}$

$P_a = f_a v = (464.7) \cdot 26.8 = 12.5 \text{ kW}$

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SUMMARY

NOT very good for:

- 1) **times**
- 2) **directions**
- 3) **accelerations**

If zero, then
mechanical energy
is conserved!

$$\Delta K = \frac{1}{2} m(v_f^2 - v_i^2)$$

$$\sum W_{nc} = \Delta K + \Delta U$$

e.g. work by friction $f_k d$

e.g. $\Delta U_g = mg\Delta y$
 $\Delta U_{el} = \frac{1}{2} k \Delta x^2$

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