King Saud University Department of Mathematics M-203

(Differential and Integral Calculus) Second Mid-Term Examination

(Summer-Semester 1435/1436)

Max. Marks: 25

Time: 90 Minutes

Marking Scheme: All questions carry equal marks

Q. No: 1 Reverse the order of integration, and evaluate the resulting integral

$$\int_{0}^{2} \int_{y/2}^{2} e^{x^{2}} dx dy.$$

Q. No: 2 Use polar coordinates to evaluate the integral

$$\int_{0}^{3} \int_{0}^{\sqrt{9-x^{2}}} (x^{2} + y^{2})^{\frac{3}{2}} dy dx .$$

Q. No: 3 Find the surface area of the surface S if S is the portion of the graph of z = 2 + xy that lies inside the cylinder $x^2 + y^2 = 1$.

Q. No: 4 Find the volume of the solid bounded by the coordinated planes and the plane x + y + z = 1, using a triple integral.

Q. No: 5 Use cylindrical coordinates to evaluate the following integral:

$$\int_{-3}^{3} \int_{-\sqrt{9-y^2}}^{\sqrt{9-y^2}} \int_{\sqrt{x^2+y^2}}^{12-x^2-y^2} dz dx dy.$$