

Problem 1

Solution

- 1) Population at 2030
- 2) Lpcd at 2030
- 3) Total average daily demand, Q_{avg} in 2030

- No specify which method, we use Arithmetic method

$$P_{2030} = P_{2010} + K_a t$$

$$K_1 = \Delta P / \Delta t = (8990 - 8100) / (1980 - 1970) = 89$$

$$K_2 = (11400 - 8990) / (1990 - 1980) = 241$$

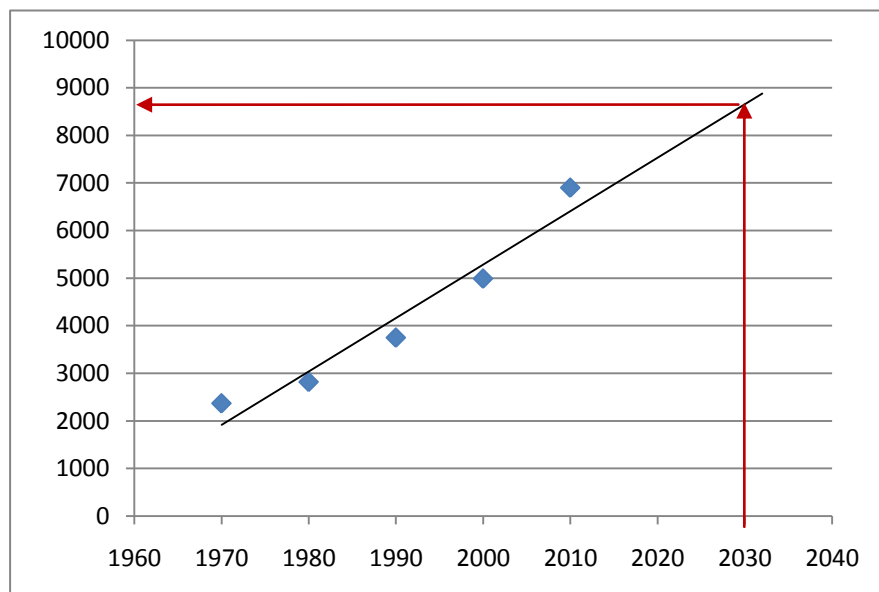
$$K_3 = 340$$

$$K_4 = 380$$

$$K_{avg} = \frac{\sum K}{n} = \frac{89 + 241 + 340 + 380}{4} = 262.5$$

$$\begin{aligned} P_{2030} &= 18600 + 262.5 (2030 - 2010) \\ &= 23850 \text{ capita} \end{aligned}$$

To determine Q_{avg} in 2030 a linear regression that passes through the points in a relationship between flow (m^3/d) and years, finding the flow in 2030



3) at 2030 $Q_{avg} = 8600 \text{ m}^3/d$

2) water consumption per capita = $8600 / 23850 = 0.3605 \text{ m}^3/c = 360.5 \text{ Lpcd}$

Problem 2

Given: $P_0 = 56000$ person , $Q_{avg} = 9,499,500 \text{ m}^3/12\text{months}$
 $Q_{max(daily)} = 43,000,000 \text{ L}$ $P_{after 10 \text{ yr}} = 72,600$

Find: Q_{avg} & Q_{max} after 10 yr

Solution

w.c. per capita = $9499500(1000) / 12 (30) (58000) = 455 \text{ Lpcd}$

Factor = $Q_{max} / Q_{avg} = \frac{43000000}{(1000)(9499500)/(12)(30)} = 1.63$

Assuming that no change in the w.c.per capita

$$\begin{aligned} Q_{avg} &= 72600 (455) = 33033000 \text{ L/d} = 33033 \text{ m}^3/\text{d} \\ Q_{max} &= 33033 (1.63) = 53843.79 \text{ m}^3/\text{d} \end{aligned}$$

Problem 3

Given: $P_{20} = 36000 \text{ c}$, $P_0 = 28500 \text{ c}$, w.c. = $16200 \text{ m}^3/\text{d}$
W.T.P design capacity = $18900 \text{ m}^3/\text{d}$

Find: in which year (t) w.c. will reach design capacity?

Solution

Present w.c. = $16200 / 28500 = 0.568 \text{ m}^3/\text{cd}$

Population when design capacity is reached = $18900 / 0.568 = 33275 \text{ c}$

Arithmetic rate of growth, $K = \Delta P / \Delta t = (36000 - 28500) / 20 = 375 \text{ (c/y)}$

To find t when w.c. will reach $18900 \text{ m}^3/\text{d}$ with a population of 33275 :

$$\begin{aligned} P &= P_0 + K t \quad \rightarrow \quad t = (P - P_0) / K \\ &= (33275 - 28500) / 375 = 12.73 \text{ years} \end{aligned}$$

Problem 4

Given: ultimate popu. Density = 14500 per km^2
Total area = 115000 m^2 , avg. WW.flow = 300 Lpcd

Find: max WW flow ..

Solution

Population = $14500 (115000 / 1,000,000) = 1667.5 = 1668 \text{ capita}$

$$Q_{avg} = 300 (1668) = 500400 \text{ L/d}$$

$$Q_{max} = 1.8 (500400) = 900720 \text{ L/d}$$

Problem 5

Solution

1) Arithmetic: - find $K_a(1960-1970) = (P_{1970} - P_{1960})/\Delta t$

$$= \frac{(90-80)*1000}{1970-1960} = 1000$$

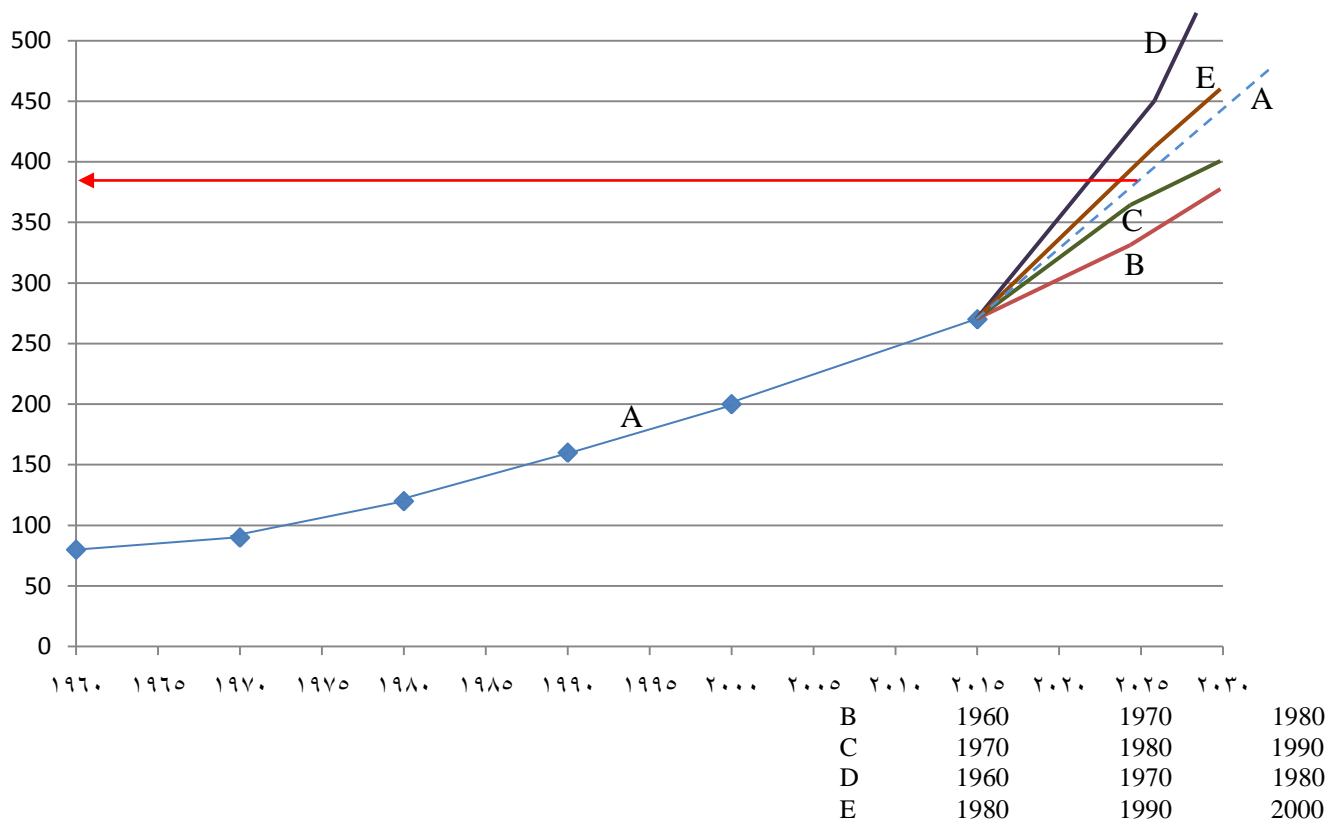
 $K_a(1970-1980), K_a(1980-1990), K_a(1990-2000), K_a(2000-2015)$
 - find average K_a
 - $P_{2025} = P_{2015} + K_a t = 270,000 + K_a * 10$

2) Geometric: - find $K_g(1960-1970) = \ln(P_{1970}/P_{1960})/\Delta t$

$$= \ln(90/80) / (1970-1960)$$

 $K_g(1970-1980), K_g(1980-1990), K_g(1990-2000), K_g(2000-2015)$
 - find average K_g
 - $P_{2025} = P_{2015} e^{\Delta t K_g} = 270,000 * e^{10(K_g)}$

3) Comparative:



4) Logistic:

$$P_t = \frac{P_{sat}}{1 + e^{(a+b \Delta t)}} \quad \text{where} \quad P_{sat} = \frac{2P_0P_1P_2 - P_1^2(P_0 + P_2)}{P_0P_1 - P_1^2}$$

$$a = \ln\left(\frac{P_{sat} - P_2}{P_2}\right)$$

$$b = \frac{1}{n} \ln \left[\frac{P_0(P_{sat} - P_1)}{P_1(P_{sat} - P_0)} \right]$$

Note: P_0 , P_1 and P_2 must have (n) the same time intervals between it

To find P at t=2025

Take P_0 at 1980, P_1 at 1990 and P_2 at 2000 with n=10

$$P_{sat} = \frac{2(120)(160)(200) - (160)^2(120+200)}{(120)(200) - (160)^2} = 320 \times 10^3$$

$$a = \ln\left(\frac{320-200}{200}\right) = -0.51$$

$$b = \frac{1}{10} \ln \left[\frac{120(320-160)}{160(320-120)} \right] = -0.051$$

$$\Delta t = t_{P \text{ estimate}} - t_{P0} = 2025 - 1980 = 45 \text{ yrs}$$

$$P_t = \frac{320}{1 + e^{(-0.51 + -0.051(45))}}$$

$$= 301.806 \times 10^3$$

$$= 301806 \text{ person}$$