

Problem # 1

Prove that the failure plane is inclined at an angle ($\theta_f = 45 + \phi/2$) to the major principal plane. Assume that Mohr-Coulomb failure criterion is valid. Using:

- i) Analytical solution.
- ii) Mohr's circle and simple geometry.

Problem # 2

In a shear box test on a clay soil the shear load was applied immediately after the normal load. The following results were obtained:

Test #	1	2	3	4
Normal stress (kN/m^2)	120	230	340	450
Shear stress (kN/m^2)	133	150	168	186

- i) Determine the shear strength parameters: c and ϕ .
- ii) Determine the principal stresses at failure and the orientations of the principal planes for test #2.
- iii) Determine the orientation of the plane of maximum shear stress at failure, and the maximum shear stress and the normal stress on that plane for test #4.
- iv) If an undrained triaxial test were to be carried out on the same soil at a cell pressure of 150 kN/m^2 , what would be the expected deviator stress at failure?
- v) If an unconfined compression test were to be carried out on the same soil, what value would be obtained for the cohesion.

Problem # 3

Using the triaxial test apparatus, a soil sample was first consolidated at a cell pressure of 600 kN/m^2 under a maintained back pressure of 300 kN/m^2 . Then with the drains closed the cell pressure was raised to 720 kN/m^2 , resulting in the pore pressure increasing to 415 kN/m^2 . Following this the axial load was raised to give an increase in deviator stress of 550 kN/m^2 , while the cell pressure remained constant, the pore pressure reading was 562 kN/m^2 . Calculate the pore pressure coefficients B and A .

$$\sigma_1 = \sigma_3 + \Delta \sigma$$

$$562 = 720 + \Delta \sigma$$

$$\begin{aligned} \sigma_1 &= \sigma_3 + \Delta \sigma \\ \sigma_1 &= 720 + 550 \\ \sigma_1 &= 1270 \end{aligned}$$

Problem #4

The results shown below were obtained at failure in a series of consolidated-undrained triaxial compression tests, with pore water pressure measurement, on specimens of a saturated clay.

Test #	Cell pressure (kN/m ²)	Deviator stress (kN/m ²)	Pore water pressure (kN/m ²)
1	150	192	80
2	300	341	154
3	450	504	222

- a) Plot the total and effective Mohr circles for each test, and determine the Mohr-Coulomb strength parameters in terms of both total and effective stresses.
- b) If the normal effective stress on a plane through the clay deposit is 400 kN/m², what is the shear strength along that plane.

Problem #5

During a consolidated-undrained triaxial test, the following data were obtained:

Change in length of sample (mm)	0	0.75	1.50	3.0	6.0	9.10	10.6
Deviator stress (kN/m ²)	0	120	200	280	360	420	460
Pore pressure (kN/m ²)	0	103	153	92	215	232	248

The cell pressure is 250 kN/m² and the original length of the saturated sample is 76 mm.

- a) Plot the variation of $\Delta\sigma$ with the axial strain of the sample.
- b) Plot the variation of the pore pressure coefficient A with the axial strain of the sample, stating the value at failure.