بسم اله الرحمن الرحيم
Department of Statistics
\& Operations Research
College of Science, King Saud University
STAT 324

First Midterm Exam
Second Semester
1430-1431 H

|  | لالم المالب |
| :---: | :---: |
| \|فه التحضير | الرقم الجاهي |
| \|لمم الاكتور | رضم اللثعبة |

- Mobile Telephones are not allowed in the classrooms.
- Time allowed is 90 minutes.
- Answer all questions.
- Choose the nearest number to your answer.
- WARNING: Do not copy answers from your neighbors. They have different questions forms.
- For each question, put the code of the correct answer in the following table beneath the question number:

| $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{1 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | C | C | D | B | A | D | B | A | D |


| $\mathbf{1 1}$ | $\mathbf{1 2}$ | $\mathbf{1 3}$ | $\mathbf{1 4}$ | $\mathbf{1 5}$ | $\mathbf{1 6}$ | $\mathbf{1 7}$ | $\mathbf{1 8}$ | $\mathbf{1 9}$ | $\mathbf{2 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| B | B | D | C | A | C | A | B | B | C |


| $\mathbf{2 1}$ | $\mathbf{2 2}$ | $\mathbf{2 3}$ | $\mathbf{2 4}$ | $\mathbf{2 5}$ | $\mathbf{2 6}$ | $\mathbf{2 7}$ | $\mathbf{2 8}$ | $\mathbf{2 9}$ | $\mathbf{3 0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | A | C | B | D | C | A | D | D | A |

Suppose that the error in the reaction temperature, in ${ }^{\circ} \mathrm{C}$, for a controlled laboratory experiment is a continuous random variable X having the function

$$
f(x)= \begin{cases}\frac{8}{x^{3}}, & x>2 \\ 0, & \text { elsewhere }\end{cases}
$$

then:

| (1) | $P(X<4)$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (A) | 0.75 | (B) | 3.0 | (C) | 0.50 | (D) | 0.15 |
| (2) | $P(-1<X<4)$ |  |  |  |  |  |  |  |
|  | (A) | 3.0 | (B) | 0.15 | (C) | 0.75 | (D) | 0.5 |
| (3) | $P(X \geq 5)$ |  |  |  |  |  |  |  |
|  | (A) | 1.0 | (B) | 0.15 | (C) | 0.16 | (D) | 0.5 |
| (4) | The expected value of $\mathrm{X} ; \mathrm{E}(\mathrm{X})$ equals |  |  |  |  |  |  |  |
|  | (A) | 2.0 | (B) | 1.0 | (C) | 8.0 | (D) | 4.0 |

An investment firm offers its customers municipal bands that mature after different numbers of years. Given that cumulative distribution function of X , the number of years to maturity for a randomly selected bond is:

$$
F(x)=\left\{\begin{array}{lc}
0 & x<1 \\
0.24 & 1 \leq x<3 \\
0.56, & 3 \leq x<5 \\
1, & x \geq 5
\end{array}\right.
$$

| (5) | $P(X=5)$ equals to |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (A) | 0.76 | (B) | 0.44 | (C) | 0.56 | (D) | 0.20 |
| (6) | $P(X>2)$ |  |  |  |  |  |  |  |
|  | (A) | 0.76 | (B) | 0.56 | (C) | 0.50 | (D) | 0.20 |
| (7) | $P(1.5<X<5)$ |  |  |  |  |  |  |  |
|  | (A) | 0.2 | (B) | 0.76 | (C) | 0.56 | (D) | 0.32 |

Suppose that $P\left(A_{1}\right)=0.4, P\left(A_{1} \cap A_{2}\right)=0.2, P\left(A_{3} \mid A_{1} \cap A_{2}\right)=0.75$, then:

| (8) | $P\left(A_{2} \mid A_{1}\right)$ equals to |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (A) | 0.00 | (B) | 0.50 | (C) | 0.1 | (D) | 0.2 |
| (9) $P\left(A_{1} \cap A_{2} \cap A_{3}\right)$ equals to |  |  |  |  |  |  |  |  |
|  | (A) | 0.15 | (B) | 0.75 | (C) | 1.0 | (D) | 0.2 |

A certain group of adults are classified according to sex and their level of education as given by the following table:

| Sex <br> Education | Female | Male |
| :--- | :---: | :---: |
| College | 17 | 22 |
| Secondary | 45 | 38 |
| Elementary | 50 | 28 |

If a person is selected at random from this group, then
(10) The probability that the person is female is:
(A) 0.44
(B) 0.50
(C) 0.28
(D) 0.56
(11) The probability that the person is female and has an elementary education is:
(A) 0.64
(B) $\mathbf{0 . 2 5}$
(C) 0.45
(D) 0.50

Suppose that a certain institute offers two training programs $T_{1}$ and $T_{2}$. In the last year, 100 and 200 trainees were enrolled for programs $T_{1}$ and $T_{2}$, respectively. From the past experience it is known that the passing probabilities are 0.75 for the program $\mathrm{T}_{1}$ and 0.80 for the program $\mathrm{T}_{2}$. Assume that at the end of the last year we selected a trainee at random from this institute.

| (12) | The probability that the selected trainee passed the program equals to |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (A) | 0.53 | (B) | 0.78 | (C) | 0.50 | (D) | 0.25 |
| (13) | What is the probability that the selected trainee has been enrolled in the program $\mathrm{T}_{2}$ given that he passed the program |  |  |  |  |  |  |  |
|  | (A) | 0.80 | (B) | 0.32 | (C) | 0.78 | (D) | 0.68 |

If $P(A)=0.9, P(B)=0.6$, and $P\left(A^{C} \cap B\right)=0.1$, then:

| (14) | $P(A \cap B)$ equals to |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (A) | 0.30 | (B) | 0.40 | (C) | 0.50 | (D) | 0.20 |
| (15) | $P(A \cup B)^{C}$ equals to |  |  |  |  |  |  |  |
|  | (A) | 0.00 | (B) | 1.00 | (C) | 0.50 | (D) | 0.15 |
| (16) | $\mathrm{P}\left(\mathrm{A}^{\mathrm{c}} \mid \mathrm{B}\right)$ equals to |  |  |  |  |  |  |  |
|  | (A) | 0.10 | (B) | 0.50 | (C) | 0.17 | (D) | 0.011 |
| (17) | $\mathrm{P}\left(\mathrm{B} \mid \mathrm{A}^{\mathrm{c}}\right)$ equals to |  |  |  |  |  |  |  |
|  | (A) | 1.00 | (B) | 0.011 | (C) | 0.50 | (D) | 0.017 |

If $P(A)=0.8, P(B)=0.5$, and $P(A U B)=0.9$, then:

| (18) | The two events $A$ and $B$ are |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | (A) | dependent | (B) | independent | (C) disjoint |
| (D) | Mutually exclusive |  |  |  |  |

If the function $f(x)=C\left(x^{2}+3\right)$ for $x=0,1,2$ can serve as a probability distribution of the discrete random variable $X$.

| (19) | The value of C equals to |  |  |  |  |  |  |  |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :---: |
|  | (A) | 14 | (B) | $\mathbf{0 . 0 7 1}$ | (C) | 12 | (D) |  |

Suppose that we have probability function $f(x)=0.1 x$, for $x=1,2,3,4$. Then

| $\mathbf{( 2 0 )}$ | $\mathrm{P}(\mathrm{X}>2)$ equals to |  |  |  |  |  |  | (B) 0.1 |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | (A) | 0.3 | (C) | $\mathbf{0 . 7}$ | (D) | 0.9 |  |  |
| $\mathbf{( 2 1 )}$ | The expected value of X equals |  |  |  |  |  |  |  |
|  | (A) | $\mathbf{3 . 0}$ | (B) | 2.5 | (C) | 0.25 | (D) | 0.5 |
| $\mathbf{( 2 2 )}$ | The Variance of X equals |  |  |  |  |  |  |  |
|  | (A) | $\mathbf{1 . 0}$ | (B) | 3.54 | (C) | 1.25 | (D) | 0.5 |

" ${ }^{\prime \prime}$
If the random variable $X$ has probability density

$$
f(x)=\left\{\begin{array}{lr}
\frac{x^{2}}{3}, & \mathrm{k}<\mathrm{x}<2 \\
0, & \text { elsewhere }
\end{array}\right.
$$

| $\mathbf{( 2 3 )}$ | Then the value of k equals |  |  |  |  |  |  |  |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | $(\mathrm{A})$ | 0.44 | $(\mathrm{~B})$ | 0.40 | $(\mathrm{C})$ | $\mathbf{- 1 . 0}$ | $(\mathrm{D})$ | 0.23 |

- 

If the random variable X has probability density

$$
f(x)=\left\{\begin{array}{cc}
1+x, & -1<x<0 \\
1-x & 0 \leq x \leq 1 \\
0 & \text { elsewhere }
\end{array}\right\}
$$

| (24) | $\mathrm{P}(\mathrm{X}<0.5)$ equals to |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (A) | 0.5 | (B) | 0.875 | (C) | 0.375 | (D) | 0.75 |
| (25) | $\mathrm{P}(\mathrm{X}=0.2)$ equals to |  |  |  |  |  |  |  |
|  | (A) | 1.2 | (B) | 0.5 | (C) | 0.8 | (D) | 0 |

- 

The cumulative distribution function $\mathrm{F}(\mathrm{x})$ of a continuous random variable X is as follows:

$$
F(x)=\left\{\begin{array}{lc}
0, & \mathrm{x} \leq-1 \\
\frac{x^{3}+1}{9}, & -1<\mathrm{x}<2 \\
1 & \mathrm{x} \geq 2
\end{array}\right.
$$

| (26) | $P(-0.5<X<1.5)$ equals to |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (A) | 0.30 | (B) | 0.40 | (C) | 0.39 | (D) | 0.20 |
| (27) | $P(X \geq 0.6)$ equals to |  |  |  |  |  |  |  |
|  | (A) | 0.86 | (B) | 0.14 | (C) | 0.50 | (D) | 0.15 |

- 

A random variable ' X ' has $\mathrm{E}(\mathrm{X})=2$ and $\mathrm{E}\left(\mathrm{X}^{2}\right)=8$. Another random variable ' Y ' is related with X as follows:
$\mathrm{Y}=(3 \mathrm{X}+5) / 2$.

| $\mathbf{( 2 8 )}$ | The mean of Y is: |  |  |  |  |  |  |  |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :---: | :---: |
|  | (A) | 2.0 | (B) 6.0 | (C) 8.5 | (D) | $\mathbf{5 . 5}$ |  |  |
| $\mathbf{( 2 9 )}$ | The Variance of Y is: | (B) 8.5 | (C) 6.0 | (D) | $\mathbf{9 . 0}$ |  |  |  |
|  |  |  |  |  |  |  |  |  |

A random variable ' X ' has $\mathrm{E}(\mathrm{X})=2$, and variance $=4$.

| (30) | Then by Chebychev theorem, $\mathrm{P}(-1<\mathrm{X}<5)$ is |  |  |  |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- |
|  | (A) $\geq \mathbf{5 / 9}$ | (B) $\mid \geq 4 / 9$ | (C) $\mid \leq 5 / 9$ | (D) $\mid \leq 4 / 9$ |

