



Tut. Sess. (10)

Ch 16: Credibility p. 397 Textbook

* pb 16.3 p. 398

Ans:

at $p=0.9$, $\Phi(y_p) = (1+p)/2 = 0.95$
 $\Rightarrow y_p = 1.645$ (calculated from standard Normal prob. dist. n, Table)

$$\therefore \lambda_0 = (y_p / \Gamma)^2 \quad \therefore \lambda_0 = \left(\frac{1.645}{0.05} \right)^2 = 1082.41$$

where $\Gamma = 0.05$

The mean is $\bar{y} = E(X_i)$
 $= \frac{475 + 550 + 400}{3} = 475$

Variance is $\sigma^2 = \frac{\sum (x_i - \bar{y})^2}{n-1} = \frac{0^2 + 75^2 + 75^2}{2}$

$$\sigma^2 = 5625 \Rightarrow \sigma = \sqrt{5625} = 75$$

For full credibility

$$n \geq \lambda_0 \left(\frac{\sigma}{\bar{y}} \right)^2$$

$$n \geq 1082.41 \left(\frac{75}{475} \right)^2$$

$$n \geq 26.9853$$

The credibility factor is

$$Z = \sqrt{\frac{n}{\lambda_0 \sigma^2 / \bar{y}^2}} = \sqrt{\frac{3}{26.9853}}$$

$$\therefore Z = 0.3334$$

The partial credibility through premium is

$$P_c = Z\bar{X} + (1-Z)M$$
$$= 0.3334(475) + 0.6666(600)$$

$\therefore P_c = 558.325$, where the average of payments is $\bar{X} = 475$ and the manual premium M is 600.

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Ans:

at $p = 0.95$, $\Phi(y_p) = (1+p)/2 = 0.975$

$\Rightarrow y_p = 1.96$ (by using Standard Normal dist'n Table)

$$\Rightarrow \lambda_0 = (y_p/\sigma)^2 = (1.96/0.05)^2 = 1536.64$$

$$E(X) = \int_0^{100} x \left(\frac{100-x}{5000} \right) dx$$

$$= \int_0^{100} \frac{100x - x^2}{5000} dx$$

$$= \frac{1}{5000} \left[100 \left(\frac{x^2}{2} \right) - \frac{x^3}{3} \right]_0^{100}$$

$$E(X) = \frac{100^3}{5000} \left(\frac{1}{2} - \frac{1}{3} \right) = \frac{1000}{5} \left(\frac{1}{6} \right) = \frac{100}{3}$$

$$E(X^2) = \int_0^{100} x^2 \left(\frac{100-x}{5000} \right) dx$$

$$E(X^2) = \int_0^{100} \left(\frac{100x^2 - x^3}{5000} \right) dx$$

$$= \frac{5000}{3}$$

$$\therefore \text{Var}(X) = E(X^2) - [E(X)]^2 = \frac{5000}{3} - \frac{10000}{9} = \frac{5000}{9}$$

To get the expected number of claims, use the following formula:

$$n\lambda = \lambda_0 \left[1 + \frac{\sigma^2}{\theta^2} \right]$$

where $\sigma^2 = \text{Var}(X)$, $\theta = E(X)$

$$\begin{aligned} \therefore \text{the expected \# of claims} &= 1,536.64 \left[1 + \frac{5000}{10000} \right] \\ &= 1,536.64 (1.5) \\ &= 2,304.96 \\ &\approx 2,305 \end{aligned}$$

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$$\alpha = p = 0.90, \quad \Phi(y_p) = (1+p)/2 = 0.95$$

$\Rightarrow y_p = 1.645$ (by using Standard Normal distn table.)

$$\Rightarrow \lambda_0 = (y_p/r)^2 = (1.645/0.06)^2 = 751.6736$$

To get the expected number of claims, use the following formula:

$$n\lambda = \lambda_0 \left[1 + \frac{\sigma^2}{\theta^2} \right]$$

where $\sigma^2 = (7500)^2$, $\theta = 1500$

$$\therefore \text{The expected \# of claims} = 751.6736 \left[1 + \frac{(7,500)^2}{(1,500)^2} \right]$$

$$= 19,543.51$$

$$\approx 19,544$$

□

Hom Assignment * n # (5) Mid II

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