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Why would someone designing a pipeline include these strange loops? Pipelines carrying liquids often contain such loops to allow for expansion and contraction as the temperature changes. We will study thermal expansion in this chapter.

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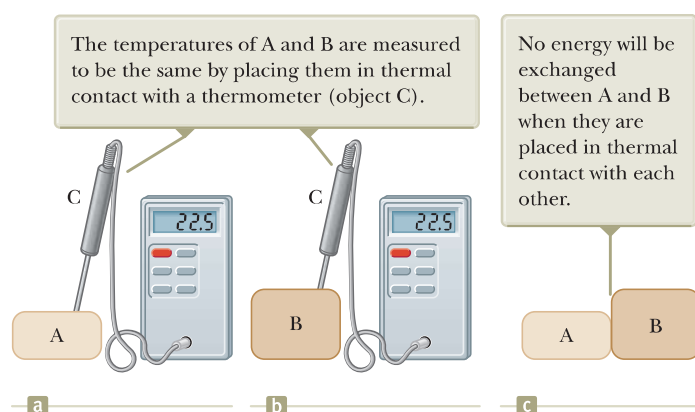
In our study of mechanics, we carefully defined such concepts as *mass*, *force*, and *kinetic energy* to facilitate our quantitative approach. Likewise, a quantitative description of thermal phenomena requires careful definitions of such important terms as *temperature*, *heat*, and *internal energy*. This chapter begins with a discussion of temperature.

Next, when studying thermal phenomena, we consider the importance of the particular substance we are investigating. For example, gases expand appreciably when heated, whereas liquids and solids expand only slightly.

This chapter concludes with a study of ideal gases on the macroscopic scale. Here, we are concerned with the relationships among such quantities as pressure, volume, and temperature of a gas. In Chapter 21, we shall examine gases on a microscopic scale, using a model that represents the components of a gas as small particles.

### 19.1 Temperature and the Zeroth Law of Thermodynamics

We often associate the concept of temperature with how hot or cold an object feels when we touch it. In this way, our senses provide us with a qualitative indication of temperature. Our senses, however, are unreliable and often mislead us. For exam-



**Figure 19.1** The zeroth law of thermodynamics.

ple, if you stand in bare feet with one foot on carpet and the other on an adjacent tile floor, the tile feels colder than the carpet *even though both are at the same temperature*. The two objects feel different because tile transfers energy by heat at a higher rate than carpet does. Your skin “measures” the rate of energy transfer by heat rather than the actual temperature. What we need is a reliable and reproducible method for measuring the relative hotness or coldness of objects rather than the rate of energy transfer. Scientists have developed a variety of thermometers for making such quantitative measurements.

Two objects at different initial temperatures eventually reach some intermediate temperature when placed in contact with each other. For example, when hot water and cold water are mixed in a bathtub, energy is transferred from the hot water to the cold water and the final temperature of the mixture is somewhere between the initial hot and cold temperatures.

Imagine that two objects are placed in an insulated container such that they interact with each other but not with the environment. If the objects are at different temperatures, energy is transferred between them, even if they are initially not in physical contact with each other. The energy-transfer mechanisms from Chapter 8 that we will focus on are heat and electromagnetic radiation. For purposes of this discussion, let’s assume two objects are in **thermal contact** with each other if energy can be exchanged between them by these processes due to a temperature difference. **Thermal equilibrium** is a situation in which two objects would not exchange energy by heat or electromagnetic radiation if they were placed in thermal contact.

Let’s consider two objects A and B, which are not in thermal contact, and a third object C, which is our thermometer. We wish to determine whether A and B are in thermal equilibrium with each other. The thermometer (object C) is first placed in thermal contact with object A until thermal equilibrium is reached<sup>1</sup> as shown in Figure 19.1a. From that moment on, the thermometer’s reading remains constant and we record this reading. The thermometer is then removed from object A and placed in thermal contact with object B as shown in Figure 19.1b. The reading is again recorded after thermal equilibrium is reached. If the two readings are the same, we can conclude that object A and object B are in thermal equilibrium with each other. If they are placed in contact with each other as in Figure 19.1c, there is no exchange of energy between them.

<sup>1</sup>We assume a negligible amount of energy transfers between the thermometer and object A in the time interval during which they are in thermal contact. Without this assumption, which is also made for the thermometer and object B, the measurement of the temperature of an object disturbs the system so that the measured temperature is different from the initial temperature of the object. In practice, whenever you measure a temperature with a thermometer, you measure the disturbed system, not the original system.

We can summarize these results in a statement known as the **zeroth law of thermodynamics** (the law of equilibrium):

**Zeroth law  
of thermodynamics** ▶

If objects A and B are separately in thermal equilibrium with a third object C, then A and B are in thermal equilibrium with each other.

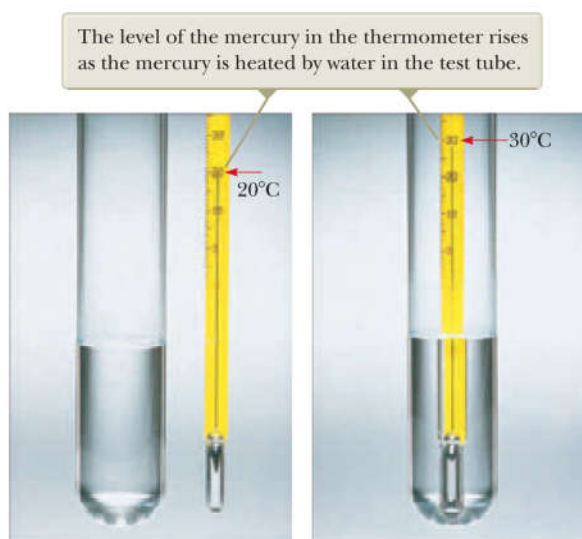
This statement can easily be proved experimentally and is very important because it enables us to define temperature. We can think of **temperature** as the property that determines whether an object is in thermal equilibrium with other objects. Two objects in thermal equilibrium with each other are at the same temperature. Conversely, if two objects have different temperatures, they are not in thermal equilibrium with each other. We now know that temperature is something that determines whether or not energy will transfer between two objects in thermal contact. In Chapter 21, we will relate temperature to the mechanical behavior of molecules.

**Quick Quiz 19.1** Two objects, with different sizes, masses, and temperatures, are placed in thermal contact. In which direction does the energy travel? **(a)** Energy travels from the larger object to the smaller object. **(b)** Energy travels from the object with more mass to the one with less mass. **(c)** Energy travels from the object at higher temperature to the object at lower temperature.

## 19.2 Thermometers and the Celsius Temperature Scale

Thermometers are devices used to measure the temperature of a system. All thermometers are based on the principle that some physical property of a system changes as the system's temperature changes. Some physical properties that change with temperature are (1) the volume of a liquid, (2) the dimensions of a solid, (3) the pressure of a gas at constant volume, (4) the volume of a gas at constant pressure, (5) the electric resistance of a conductor, and (6) the color of an object.

A common thermometer in everyday use consists of a mass of liquid—usually mercury or alcohol—that expands into a glass capillary tube when heated (Fig. 19.2). In this case, the physical property that changes is the volume of a liquid. Any temperature change in the range of the thermometer can be defined as being proportional to the change in length of the liquid column. The thermometer can be calibrated by placing it in thermal contact with a natural system that remains



**Figure 19.2** A mercury thermometer before and after increasing its temperature.



at constant temperature. One such system is a mixture of water and ice in thermal equilibrium at atmospheric pressure. On the **Celsius temperature scale**, this mixture is defined to have a temperature of zero degrees Celsius, which is written as  $0^{\circ}\text{C}$ ; this temperature is called the *ice point* of water. Another commonly used system is a mixture of water and steam in thermal equilibrium at atmospheric pressure; its temperature is defined as  $100^{\circ}\text{C}$ , which is the *steam point* of water. Once the liquid levels in the thermometer have been established at these two points, the length of the liquid column between the two points is divided into 100 equal segments to create the Celsius scale. Therefore, each segment denotes a change in temperature of one Celsius degree.

Thermometers calibrated in this way present problems when extremely accurate readings are needed. For instance, the readings given by an alcohol thermometer calibrated at the ice and steam points of water might agree with those given by a mercury thermometer only at the calibration points. Because mercury and alcohol have different thermal expansion properties, when one thermometer reads a temperature of, for example,  $50^{\circ}\text{C}$ , the other may indicate a slightly different value. The discrepancies between thermometers are especially large when the temperatures to be measured are far from the calibration points.<sup>2</sup>

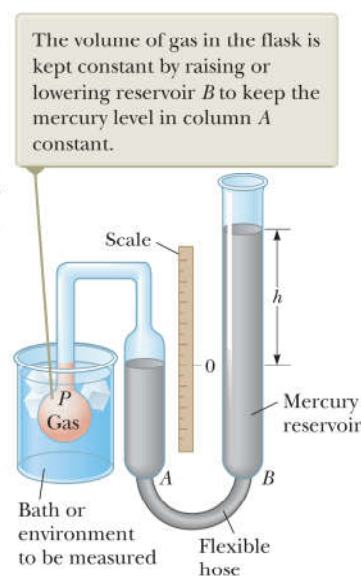
An additional practical problem of any thermometer is the limited range of temperatures over which it can be used. A mercury thermometer, for example, cannot be used below the freezing point of mercury, which is  $-39^{\circ}\text{C}$ , and an alcohol thermometer is not useful for measuring temperatures above  $85^{\circ}\text{C}$ , the boiling point of alcohol. To surmount this problem, we need a universal thermometer whose readings are independent of the substance used in it. The gas thermometer, discussed in the next section, approaches this requirement.

### 19.3 The Constant-Volume Gas Thermometer and the Absolute Temperature Scale

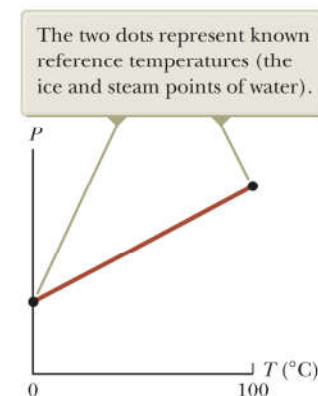
One version of a gas thermometer is the constant-volume apparatus shown in Figure 19.3. The physical change exploited in this device is the variation of pressure of a fixed volume of gas with temperature. The flask is immersed in an ice-water bath, and mercury reservoir *B* is raised or lowered until the top of the mercury in column *A* is at the zero point on the scale. The height *h*, the difference between the mercury levels in reservoir *B* and column *A*, indicates the pressure in the flask at  $0^{\circ}\text{C}$  by means of Equation 14.4,  $P = P_0 + \rho gh$ .

The flask is then immersed in water at the steam point. Reservoir *B* is readjusted until the top of the mercury in column *A* is again at zero on the scale, which ensures that the gas's volume is the same as it was when the flask was in the ice bath (hence the designation "constant-volume"). This adjustment of reservoir *B* gives a value for the gas pressure at  $100^{\circ}\text{C}$ . These two pressure and temperature values are then plotted as shown in Figure 19.4. The line connecting the two points serves as a calibration curve for unknown temperatures. (Other experiments show that a linear relationship between pressure and temperature is a very good assumption.) To measure the temperature of a substance, the gas flask of Figure 19.3 is placed in thermal contact with the substance and the height of reservoir *B* is adjusted until the top of the mercury column in *A* is at zero on the scale. The height of the mercury column in *B* indicates the pressure of the gas; knowing the pressure, the temperature of the substance is found using the graph in Figure 19.4.

Now suppose temperatures of different gases at different initial pressures are measured with gas thermometers. Experiments show that the thermometer readings are nearly independent of the type of gas used as long as the gas pressure is low and the temperature is well above the point at which the gas liquefies



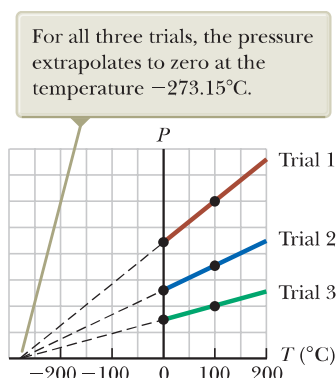
**Figure 19.3** A constant-volume gas thermometer measures the pressure of the gas contained in the flask immersed in the bath.



**Figure 19.4** A typical graph of pressure versus temperature taken with a constant-volume gas thermometer.

<sup>2</sup>Two thermometers that use the same liquid may also give different readings, due in part to difficulties in constructing uniform-bore glass capillary tubes.



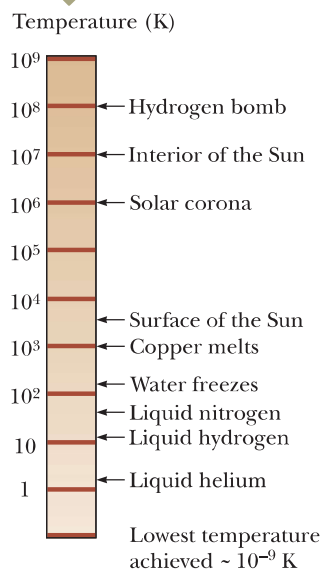


**Figure 19.5** Pressure versus temperature for experimental trials in which gases have different pressures in a constant-volume gas thermometer.

### Pitfall Prevention 19.1

**A Matter of Degree** Notations for temperatures in the Kelvin scale do not use the degree sign. The unit for a Kelvin temperature is simply “kelvins” and not “degrees Kelvin.”

Note that the scale is logarithmic.



**Figure 19.6** Absolute temperatures at which various physical processes occur.

(Fig. 19.5). The agreement among thermometers using various gases improves as the pressure is reduced.

If we extend the straight lines in Figure 19.5 toward negative temperatures, we find a remarkable result: **in every case, the pressure is zero when the temperature is  $-273.15^\circ\text{C}$** ! This finding suggests some special role that this particular temperature must play. It is used as the basis for the **absolute temperature scale**, which sets  $-273.15^\circ\text{C}$  as its zero point. This temperature is often referred to as **absolute zero**. It is indicated as a zero because at a lower temperature, the pressure of the gas would become negative, which is meaningless. The size of one degree on the absolute temperature scale is chosen to be identical to the size of one degree on the Celsius scale. Therefore, the conversion between these temperatures is

$$T_C = T - 273.15 \quad (19.1)$$

where  $T_C$  is the Celsius temperature and  $T$  is the absolute temperature.

Because the ice and steam points are experimentally difficult to duplicate and depend on atmospheric pressure, an absolute temperature scale based on two new fixed points was adopted in 1954 by the International Committee on Weights and Measures. The first point is absolute zero. The second reference temperature for this new scale was chosen as the **triple point of water**, which is the single combination of temperature and pressure at which liquid water, gaseous water, and ice (solid water) coexist in equilibrium. This triple point occurs at a temperature of  $0.01^\circ\text{C}$  and a pressure of 4.58 mm of mercury. On the new scale, which uses the unit *kelvin*, the temperature of water at the triple point was set at 273.16 kelvins, abbreviated 273.16 K. This choice was made so that the old absolute temperature scale based on the ice and steam points would agree closely with the new scale based on the triple point. This new absolute temperature scale (also called the **Kelvin scale**) employs the SI unit of absolute temperature, the **kelvin**, which is defined to be  $1/273.16$  of the difference between absolute zero and the temperature of the triple point of water.

Figure 19.6 gives the absolute temperature for various physical processes and structures. The temperature of absolute zero (0 K) cannot be achieved, although laboratory experiments have come very close, reaching temperatures of less than one nanokelvin.

## The Celsius, Fahrenheit, and Kelvin Temperature Scales<sup>3</sup>

Equation 19.1 shows that the Celsius temperature  $T_C$  is shifted from the absolute (Kelvin) temperature  $T$  by  $273.15^\circ$ . Because the size of one degree is the same on the two scales, a temperature difference of  $5^\circ\text{C}$  is equal to a temperature difference of 5 K. The two scales differ only in the choice of the zero point. Therefore, the ice-point temperature on the Kelvin scale, 273.15 K, corresponds to  $0.00^\circ\text{C}$ , and the Kelvin-scale steam point, 373.15 K, is equivalent to  $100.00^\circ\text{C}$ .

A common temperature scale in everyday use in the United States is the **Fahrenheit scale**. This scale sets the temperature of the ice point at  $32^\circ\text{F}$  and the temperature of the steam point at  $212^\circ\text{F}$ . The relationship between the Celsius and Fahrenheit temperature scales is

$$T_F = \frac{9}{5}T_C + 32^\circ\text{F} \quad (19.2)$$

We can use Equations 19.1 and 19.2 to find a relationship between changes in temperature on the Celsius, Kelvin, and Fahrenheit scales:

$$\Delta T_C = \Delta T = \frac{5}{9}\Delta T_F \quad (19.3)$$

Of these three temperature scales, only the Kelvin scale is based on a true zero value of temperature. The Celsius and Fahrenheit scales are based on an arbitrary zero associated with one particular substance, water, on one particular planet, the

<sup>3</sup>Named after Anders Celsius (1701–1744), Daniel Gabriel Fahrenheit (1686–1736), and William Thomson, Lord Kelvin (1824–1907), respectively.

Earth. Therefore, if you encounter an equation that calls for a temperature  $T$  or that involves a ratio of temperatures, you *must* convert all temperatures to kelvins. If the equation contains a change in temperature  $\Delta T$ , using Celsius temperatures will give you the correct answer, in light of Equation 19.3, but it is always *safest* to convert temperatures to the Kelvin scale.

- Quick Quiz 19.2** Consider the following pairs of materials. Which pair represents two materials, one of which is twice as hot as the other? (a) boiling water at  $100^\circ\text{C}$ , a glass of water at  $50^\circ\text{C}$  (b) boiling water at  $100^\circ\text{C}$ , frozen methane at  $-50^\circ\text{C}$  (c) an ice cube at  $-20^\circ\text{C}$ , flames from a circus fire-eater at  $233^\circ\text{C}$  (d) none of those pairs

### Example 19.1 Converting Temperatures

On a day when the temperature reaches  $50^\circ\text{F}$ , what is the temperature in degrees Celsius and in kelvins?

#### SOLUTION

**Conceptualize** In the United States, a temperature of  $50^\circ\text{F}$  is well understood. In many other parts of the world, however, this temperature might be meaningless because people are familiar with the Celsius temperature scale.

**Categorize** This example is a simple substitution problem.

Solve Equation 19.2 for the Celsius temperature and substitute numerical values:

$$T_C = \frac{5}{9}(T_F - 32) = \frac{5}{9}(50 - 32) = 10^\circ\text{C}$$

Use Equation 19.1 to find the Kelvin temperature:

$$T = T_C + 273.15 = 10^\circ\text{C} + 273.15 = 283\text{ K}$$

A convenient set of weather-related temperature equivalents to keep in mind is that  $0^\circ\text{C}$  is (literally) freezing at  $32^\circ\text{F}$ ,  $10^\circ\text{C}$  is cool at  $50^\circ\text{F}$ ,  $20^\circ\text{C}$  is room temperature,  $30^\circ\text{C}$  is warm at  $86^\circ\text{F}$ , and  $40^\circ\text{C}$  is a hot day at  $104^\circ\text{F}$ .

## 19.4 Thermal Expansion of Solids and Liquids

Our discussion of the liquid thermometer makes use of one of the best-known changes in a substance: as its temperature increases, its volume increases. This phenomenon, known as **thermal expansion**, plays an important role in numerous engineering applications. For example, thermal-expansion joints such as those shown in Figure 19.7 must be included in buildings, concrete highways, railroad tracks,

Without these joints to separate sections of roadway on bridges, the surface would buckle due to thermal expansion on very hot days or crack due to contraction on very cold days.



a

The long, vertical joint is filled with a soft material that allows the wall to expand and contract as the temperature of the bricks changes.



b

**Figure 19.7** Thermal-expansion joints in (a) bridges and (b) walls.



brick walls, and bridges to compensate for dimensional changes that occur as the temperature changes.

Thermal expansion is a consequence of the change in the *average* separation between the atoms in an object. To understand this concept, let's model the atoms as being connected by stiff springs as discussed in Section 15.3 and shown in Figure 15.11b. At ordinary temperatures, the atoms in a solid oscillate about their equilibrium positions with an amplitude of approximately  $10^{-11}$  m and a frequency of approximately  $10^{13}$  Hz. The average spacing between the atoms is about  $10^{-10}$  m. As the temperature of the solid increases, the atoms oscillate with greater amplitudes; as a result, the average separation between them increases.<sup>4</sup> Consequently, the object expands.

If thermal expansion is sufficiently small relative to an object's initial dimensions, the change in any dimension is, to a good approximation, proportional to the first power of the temperature change. Suppose an object has an initial length  $L_i$  along some direction at some temperature and the length changes by an amount  $\Delta L$  for a change in temperature  $\Delta T$ . Because it is convenient to consider the fractional change in length per degree of temperature change, we define the **average coefficient of linear expansion** as

$$\alpha \equiv \frac{\Delta L / L_i}{\Delta T}$$

Experiments show that  $\alpha$  is constant for small changes in temperature. For purposes of calculation, this equation is usually rewritten as

$$\Delta L = \alpha L_i \Delta T \quad (19.4)$$

or as

$$L_f - L_i = \alpha L_i (T_f - T_i) \quad (19.5)$$

where  $L_f$  is the final length,  $T_i$  and  $T_f$  are the initial and final temperatures, respectively, and the proportionality constant  $\alpha$  is the average coefficient of linear expansion for a given material and has units of  $(^\circ\text{C})^{-1}$ . Equation 19.4 can be used for both thermal expansion, when the temperature of the material increases, and thermal contraction, when its temperature decreases.

It may be helpful to think of thermal expansion as an effective magnification or as a photographic enlargement of an object. For example, as a metal washer is heated (Fig. 19.8), all dimensions, including the radius of the hole, increase according to Equation 19.4. A cavity in a piece of material expands in the same way as if the cavity were filled with the material.

Table 19.1 lists the average coefficients of linear expansion for various materials. For these materials,  $\alpha$  is positive, indicating an increase in length with increasing temperature. That is not always the case, however. Some substances—calcite ( $\text{CaCO}_3$ ) is one example—expand along one dimension (positive  $\alpha$ ) and contract along another (negative  $\alpha$ ) as their temperatures are increased.

Because the linear dimensions of an object change with temperature, it follows that surface area and volume change as well. The change in volume is proportional to the initial volume  $V_i$  and to the change in temperature according to the relationship

$$\Delta V = \beta V_i \Delta T \quad (19.6)$$

where  $\beta$  is the **average coefficient of volume expansion**. To find the relationship between  $\beta$  and  $\alpha$ , assume the average coefficient of linear expansion of the solid is the same in all directions; that is, assume the material is *isotropic*. Consider a solid box of dimensions  $\ell$ ,  $w$ , and  $h$ . Its volume at some temperature  $T_i$  is  $V_i = \ell wh$ . If the

Thermal expansion  
in one dimension

#### Pitfall Prevention 19.2

**Do Holes Become Larger or Smaller?** When an object's temperature is raised, every linear dimension increases in size. That includes any holes in the material, which expand in the same way as if the hole were filled with the material as shown in Figure 19.8.

Thermal expansion  
in three dimensions

<sup>4</sup>More precisely, thermal expansion arises from the *asymmetrical* nature of the potential energy curve for the atoms in a solid as shown in Figure 15.11a. If the oscillators were truly harmonic, the average atomic separations would not change regardless of the amplitude of vibration.

**Table 19.1** Average Expansion Coefficients for Some Materials Near Room Temperature

Material (Solids)	Average Linear Expansion Coefficient ( $\alpha$ )( $^{\circ}\text{C}$ ) $^{-1}$	Material (Liquids and Gases)	Average Volume Expansion Coefficient ( $\beta$ )( $^{\circ}\text{C}$ ) $^{-1}$
Aluminum	$24 \times 10^{-6}$	Acetone	$1.5 \times 10^{-4}$
Brass and bronze	$19 \times 10^{-6}$	Alcohol, ethyl	$1.12 \times 10^{-4}$
Concrete	$12 \times 10^{-6}$	Benzene	$1.24 \times 10^{-4}$
Copper	$17 \times 10^{-6}$	Gasoline	$9.6 \times 10^{-4}$
Glass (ordinary)	$9 \times 10^{-6}$	Glycerin	$4.85 \times 10^{-4}$
Glass (Pyrex)	$3.2 \times 10^{-6}$	Mercury	$1.82 \times 10^{-4}$
Invar (Ni-Fe alloy)	$0.9 \times 10^{-6}$	Turpentine	$9.0 \times 10^{-4}$
Lead	$29 \times 10^{-6}$	Air <sup>a</sup> at $0^{\circ}\text{C}$	$3.67 \times 10^{-3}$
Steel	$11 \times 10^{-6}$	Helium <sup>a</sup>	$3.665 \times 10^{-3}$

<sup>a</sup>Gases do not have a specific value for the volume expansion coefficient because the amount of expansion depends on the type of process through which the gas is taken. The values given here assume the gas undergoes an expansion at constant pressure.

temperature changes to  $T_i + \Delta T$ , its volume changes to  $V_i + \Delta V$ , where each dimension changes according to Equation 19.4. Therefore,

$$\begin{aligned}
 V_i + \Delta V &= (\ell + \Delta\ell)(w + \Delta w)(h + \Delta h) \\
 &= (\ell + \alpha\ell\Delta T)(w + \alpha w\Delta T)(h + \alpha h\Delta T) \\
 &= \ell wh(1 + \alpha\Delta T)^3 \\
 &= V_i[1 + 3\alpha\Delta T + 3(\alpha\Delta T)^2 + (\alpha\Delta T)^3]
 \end{aligned}$$

Dividing both sides by  $V_i$  and isolating the term  $\Delta V/V_i$ , we obtain the fractional change in volume:

$$\frac{\Delta V}{V_i} = 3\alpha\Delta T + 3(\alpha\Delta T)^2 + (\alpha\Delta T)^3$$

Because  $\alpha\Delta T \ll 1$  for typical values of  $\Delta T$  ( $< \sim 100^{\circ}\text{C}$ ), we can neglect the terms  $3(\alpha\Delta T)^2$  and  $(\alpha\Delta T)^3$ . Upon making this approximation, we see that

$$\frac{\Delta V}{V_i} = 3\alpha\Delta T \rightarrow \Delta V = (3\alpha)V_i\Delta T$$

Comparing this expression to Equation 19.6 shows that

$$\beta = 3\alpha$$

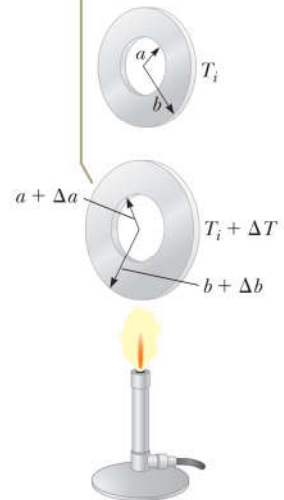
In a similar way, you can show that the change in area of a rectangular plate is given by  $\Delta A = 2\alpha A_i\Delta T$  (see Problem 61).

A simple mechanism called a *bimetallic strip*, found in practical devices such as mechanical thermostats, uses the difference in coefficients of expansion for different materials. It consists of two thin strips of dissimilar metals bonded together. As the temperature of the strip increases, the two metals expand by different amounts and the strip bends as shown in Figure 19.9.

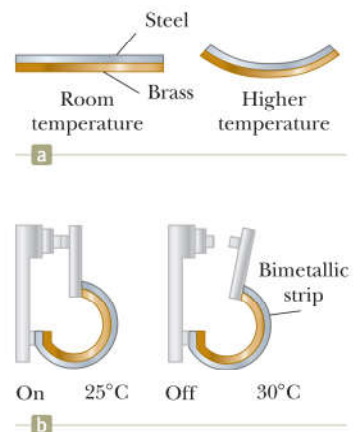
**Quick Quiz 19.3** If you are asked to make a very sensitive glass thermometer, which of the following working liquids would you choose? (a) mercury (b) alcohol (c) gasoline (d) glycerin

**Quick Quiz 19.4** Two spheres are made of the same metal and have the same radius, but one is hollow and the other is solid. The spheres are taken through the same temperature increase. Which sphere expands more? (a) The solid sphere expands more. (b) The hollow sphere expands more. (c) They expand by the same amount. (d) There is not enough information to say.

As the washer is heated, all dimensions increase, including the radius of the hole.



**Figure 19.8** Thermal expansion of a homogeneous metal washer. (The expansion is exaggerated in this figure.)



**Figure 19.9** (a) A bimetallic strip bends as the temperature changes because the two metals have different expansion coefficients. (b) A bimetallic strip used in a thermostat to break or make electrical contact.



**Example 19.2** Expansion of a Railroad Track

A segment of steel railroad track has a length of 30.000 m when the temperature is 0.0°C.

**(A)** What is its length when the temperature is 40.0°C?

**SOLUTION**

**Conceptualize** Because the rail is relatively long, we expect to obtain a measurable increase in length for a 40°C temperature increase.

**Categorize** We will evaluate a length increase using the discussion of this section, so this part of the example is a substitution problem.

Use Equation 19.4 and the value of the coefficient of linear expansion from Table 19.1:

$$\Delta L = \alpha L_i \Delta T = [11 \times 10^{-6} (\text{°C})^{-1}](30.000 \text{ m})(40.0\text{°C}) = 0.013 \text{ m}$$

Find the new length of the track:

$$L_f = 30.000 \text{ m} + 0.013 \text{ m} = 30.013 \text{ m}$$

**(B)** Suppose the ends of the rail are rigidly clamped at 0.0°C so that expansion is prevented. What is the thermal stress set up in the rail if its temperature is raised to 40.0°C?

**SOLUTION**

**Categorize** This part of the example is an analysis problem because we need to use concepts from another chapter.

**Analyze** The thermal stress is the same as the tensile stress in the situation in which the rail expands freely and is then compressed with a mechanical force  $F$  back to its original length.

Find the tensile stress from Equation 12.6 using Young's modulus for steel from Table 12.1:

$$\text{Tensile stress} = \frac{F}{A} = Y \frac{\Delta L}{L_i}$$

$$\frac{F}{A} = (20 \times 10^{10} \text{ N/m}^2) \left( \frac{0.013 \text{ m}}{30.000 \text{ m}} \right) = 8.7 \times 10^7 \text{ N/m}^2$$

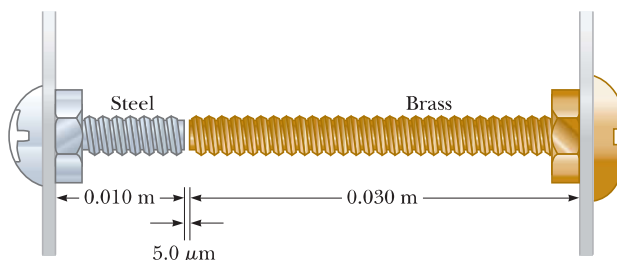
**Finalize** The expansion in part (A) is 1.3 cm. This expansion is indeed measurable as predicted in the Conceptualize step. The thermal stress in part (B) can be avoided by leaving small expansion gaps between the rails.

**WHAT IF?** What if the temperature drops to −40.0°C? What is the length of the unclamped segment?

**Answer** The expression for the change in length in Equation 19.4 is the same whether the temperature increases or decreases. Therefore, if there is an increase in length of 0.013 m when the temperature increases by 40°C, there is a decrease in length of 0.013 m when the temperature decreases by 40°C. (We assume  $\alpha$  is constant over the entire range of temperatures.) The new length at the colder temperature is 30.000 m − 0.013 m = 29.987 m.

**Example 19.3** The Thermal Electrical Short

A poorly designed electronic device has two bolts attached to different parts of the device that almost touch each other in its interior as in Figure 19.10. The steel and brass bolts are at different electric potentials, and if they touch, a short circuit will develop, damaging the device. (We will study electric potential in Chapter 25.) The initial gap between the ends of the bolts is  $d = 5.0 \mu\text{m}$  at 27°C. At what temperature will the bolts touch? Assume the distance between the walls of the device is not affected by the temperature change.



**Figure 19.10** (Example 19.3) Two bolts attached to different parts of an electrical device are almost touching when the temperature is 27°C. As the temperature increases, the ends of the bolts move toward each other.

**SOLUTION**

**Conceptualize** Imagine the ends of both bolts expanding into the gap between them as the temperature rises.

► 19.3 continued

**Categorize** We categorize this example as a thermal expansion problem in which the *sum* of the changes in length of the two bolts must equal the length of the initial gap between the ends.

**Analyze** Set the sum of the length changes equal to the width of the gap:

$$\Delta L_{\text{br}} + \Delta L_{\text{st}} = \alpha_{\text{br}} L_{i,\text{br}} \Delta T + \alpha_{\text{st}} L_{i,\text{st}} \Delta T = d$$

Solve for  $\Delta T$ :

$$\Delta T = \frac{d}{\alpha_{\text{br}} L_{i,\text{br}} + \alpha_{\text{st}} L_{i,\text{st}}}$$

Substitute numerical values:

$$\Delta T = \frac{5.0 \times 10^{-6} \text{ m}}{[19 \times 10^{-6} (\text{°C})^{-1}](0.030 \text{ m}) + [11 \times 10^{-6} (\text{°C})^{-1}](0.010 \text{ m})} = 7.4\text{°C}$$

Find the temperature at which the bolts touch:

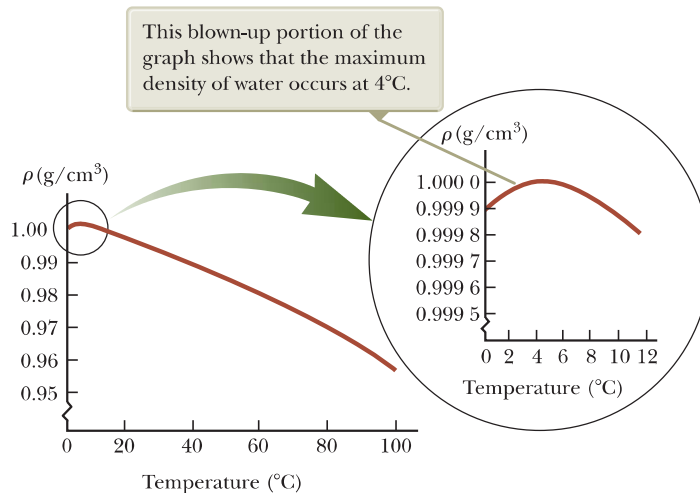
$$T = 27\text{°C} + 7.4\text{°C} = 34\text{°C}$$

**Finalize** This temperature is possible if the air conditioning in the building housing the device fails for a long period on a very hot summer day.

## The Unusual Behavior of Water

Liquids generally increase in volume with increasing temperature and have average coefficients of volume expansion about ten times greater than those of solids. Cold water is an exception to this rule as you can see from its density-versus-temperature curve shown in Figure 19.11. As the temperature increases from 0°C to 4°C, water contracts and its density therefore increases. Above 4°C, water expands with increasing temperature and so its density decreases. Therefore, the density of water reaches a maximum value of 1.000 g/cm<sup>3</sup> at 4°C.

We can use this unusual thermal-expansion behavior of water to explain why a pond begins freezing at the surface rather than at the bottom. When the air temperature drops from, for example, 7°C to 6°C, the surface water also cools and consequently decreases in volume. The surface water is denser than the water below it, which has not cooled and decreased in volume. As a result, the surface water sinks, and warmer water from below moves to the surface. When the air temperature is between 4°C and 0°C, however, the surface water expands as it cools, becoming less dense than the water below it. The mixing process stops, and eventually the surface water freezes. As the water freezes, the ice remains on the surface because ice is less dense than water. The ice continues to build up at the surface, while water near the



**Figure 19.11** The variation in the density of water at atmospheric pressure with temperature.



bottom remains at 4°C. If that were not the case, fish and other forms of marine life would not survive.

## 19.5 Macroscopic Description of an Ideal Gas

The volume expansion equation  $\Delta V = \beta V_i \Delta T$  is based on the assumption that the material has an initial volume  $V_i$  before the temperature change occurs. Such is the case for solids and liquids because they have a fixed volume at a given temperature.

The case for gases is completely different. The interatomic forces within gases are very weak, and, in many cases, we can imagine these forces to be nonexistent and still make very good approximations. Therefore, *there is no equilibrium separation* for the atoms and no “standard” volume at a given temperature; the volume depends on the size of the container. As a result, we cannot express changes in volume  $\Delta V$  in a process on a gas with Equation 19.6 because we have no defined volume  $V_i$  at the beginning of the process. Equations involving gases contain the volume  $V$ , rather than a *change* in the volume from an initial value, as a variable.

For a gas, it is useful to know how the quantities volume  $V$ , pressure  $P$ , and temperature  $T$  are related for a sample of gas of mass  $m$ . In general, the equation that interrelates these quantities, called the *equation of state*, is very complicated. If the gas is maintained at a very low pressure (or low density), however, the equation of state is quite simple and can be determined from experimental results. Such a low-density gas is commonly referred to as an **ideal gas**.<sup>5</sup> We can use the **ideal gas model** to make predictions that are adequate to describe the behavior of real gases at low pressures.

It is convenient to express the amount of gas in a given volume in terms of the number of moles  $n$ . One **mole** of any substance is that amount of the substance that contains **Avogadro’s number**  $N_A = 6.022 \times 10^{23}$  of constituent particles (atoms or molecules). The number of moles  $n$  of a substance is related to its mass  $m$  through the expression

$$n = \frac{m}{M} \quad (19.7)$$

where  $M$  is the molar mass of the substance. The molar mass of each chemical element is the atomic mass (from the periodic table; see Appendix C) expressed in grams per mole. For example, the mass of one He atom is 4.00 u (atomic mass units), so the molar mass of He is 4.00 g/mol.

Now suppose an ideal gas is confined to a cylindrical container whose volume can be varied by means of a movable piston as in Figure 19.12. If we assume the cylinder does not leak, the mass (or the number of moles) of the gas remains constant. For such a system, experiments provide the following information:

- When the gas is kept at a constant temperature, its pressure is inversely proportional to the volume. (This behavior is described historically as Boyle’s law.)
- When the pressure of the gas is kept constant, the volume is directly proportional to the temperature. (This behavior is described historically as Charles’s law.)
- When the volume of the gas is kept constant, the pressure is directly proportional to the temperature. (This behavior is described historically as Gay-Lussac’s law.)

These observations are summarized by the **equation of state for an ideal gas**:

$$PV = nRT \quad (19.8)$$

Equation of state for  
an ideal gas ►



**Figure 19.12** An ideal gas confined to a cylinder whose volume can be varied by means of a movable piston.

<sup>5</sup>To be more specific, the assumptions here are that the temperature of the gas must not be too low (the gas must not condense into a liquid) or too high and that the pressure must be low. The concept of an ideal gas implies that the gas molecules do not interact except upon collision and that the molecular volume is negligible compared with the volume of the container. In reality, an ideal gas does not exist. The concept of an ideal gas is nonetheless very useful because real gases at low pressures are well-modeled as ideal gases.

In this expression, also known as the **ideal gas law**,  $n$  is the number of moles of gas in the sample and  $R$  is a constant. Experiments on numerous gases show that as the pressure approaches zero, the quantity  $PV/nT$  approaches the same value  $R$  for all gases. For this reason,  $R$  is called the **universal gas constant**. In SI units, in which pressure is expressed in pascals ( $1 \text{ Pa} = 1 \text{ N/m}^2$ ) and volume in cubic meters, the product  $PV$  has units of newton  $\cdot$  meters, or joules, and  $R$  has the value

$$R = 8.314 \text{ J/mol} \cdot \text{K} \quad (19.9)$$

If the pressure is expressed in atmospheres and the volume in liters ( $1 \text{ L} = 10^3 \text{ cm}^3 = 10^{-3} \text{ m}^3$ ), then  $R$  has the value

$$R = 0.08206 \text{ L} \cdot \text{atm/mol} \cdot \text{K}$$

Using this value of  $R$  and Equation 19.8 shows that the volume occupied by 1 mol of *any* gas at atmospheric pressure and at  $0^\circ\text{C}$  (273 K) is 22.4 L.

The ideal gas law states that if the volume and temperature of a fixed amount of gas do not change, the pressure also remains constant. Consider a bottle of champagne that is shaken and then spews liquid when opened as shown in Figure 19.13. A common misconception is that the pressure inside the bottle is increased when the bottle is shaken. On the contrary, because the temperature of the bottle and its contents remains constant as long as the bottle is sealed, so does the pressure, as can be shown by replacing the cork with a pressure gauge. The correct explanation is as follows. Carbon dioxide gas resides in the volume between the liquid surface and the cork. The pressure of the gas in this volume is set higher than atmospheric pressure in the bottling process. Shaking the bottle displaces some of the carbon dioxide gas into the liquid, where it forms bubbles, and these bubbles become attached to the inside of the bottle. (No new gas is generated by shaking.) When the bottle is opened, the pressure is reduced to atmospheric pressure, which causes the volume of the bubbles to increase suddenly. If the bubbles are attached to the bottle (beneath the liquid surface), their rapid expansion expels liquid from the bottle. If the sides and bottom of the bottle are first tapped until no bubbles remain beneath the surface, however, the drop in pressure does not force liquid from the bottle when the champagne is opened.

The ideal gas law is often expressed in terms of the total number of molecules  $N$ . Because the number of moles  $n$  equals the ratio of the total number of molecules and Avogadro's number  $N_A$ , we can write Equation 19.8 as

$$PV = nRT = \frac{N}{N_A} RT$$

$$PV = Nk_B T \quad (19.10)$$

where  $k_B$  is **Boltzmann's constant**, which has the value

$$k_B = \frac{R}{N_A} = 1.38 \times 10^{-23} \text{ J/K} \quad (19.11)$$

It is common to call quantities such as  $P$ ,  $V$ , and  $T$  the **thermodynamic variables** of an ideal gas. If the equation of state is known, one of the variables can always be expressed as some function of the other two.

**Quick Quiz 19.5** A common material for cushioning objects in packages is made by trapping bubbles of air between sheets of plastic. Is this material more effective at keeping the contents of the package from moving around inside the package on (a) a hot day, (b) a cold day, or (c) either hot or cold days?

**Quick Quiz 19.6** On a winter day, you turn on your furnace and the temperature of the air inside your home increases. Assume your home has the normal amount of leakage between inside air and outside air. Is the number of moles of air in your room at the higher temperature (a) larger than before, (b) smaller than before, or (c) the same as before?



**Figure 19.13** A bottle of champagne is shaken and opened. Liquid spews out of the opening. A common misconception is that the pressure inside the bottle is increased by the shaking.

### Pitfall Prevention 19.3

**So Many  $k$ s** There are a variety of physical quantities for which the letter  $k$  is used. Two we have seen previously are the force constant for a spring (Chapter 15) and the wave number for a mechanical wave (Chapter 16). Boltzmann's constant is another  $k$ , and we will see  $k$  used for thermal conductivity in Chapter 20 and for an electrical constant in Chapter 23. To make some sense of this confusing state of affairs, we use a subscript B for Boltzmann's constant to help us recognize it. In this book, you will see Boltzmann's constant as  $k_B$ , but you may see Boltzmann's constant in other resources as simply  $k$ .

### ◀ Boltzmann's constant



### Example 19.4 Heating a Spray Can

A spray can containing a propellant gas at twice atmospheric pressure (202 kPa) and having a volume of 125.00 cm<sup>3</sup> is at 22°C. It is then tossed into an open fire. (*Warning:* Do not do this experiment; it is very dangerous.) When the temperature of the gas in the can reaches 195°C, what is the pressure inside the can? Assume any change in the volume of the can is negligible.

#### SOLUTION

**Conceptualize** Intuitively, you should expect that the pressure of the gas in the container increases because of the increasing temperature.

**Categorize** We model the gas in the can as ideal and use the ideal gas law to calculate the new pressure.

**Analyze** Rearrange Equation 19.8:

$$(1) \quad \frac{PV}{T} = nR$$

No air escapes during the compression, so  $n$ , and therefore  $nR$ , remains constant. Hence, set the initial value of the left side of Equation (1) equal to the final value:

$$(2) \quad \frac{P_i V_i}{T_i} = \frac{P_f V_f}{T_f}$$

Because the initial and final volumes of the gas are assumed to be equal, cancel the volumes:

$$(3) \quad \frac{P_i}{T_i} = \frac{P_f}{T_f}$$

Solve for  $P_f$ :

$$P_f = \left(\frac{T_f}{T_i}\right)P_i = \left(\frac{468 \text{ K}}{295 \text{ K}}\right)(202 \text{ kPa}) = 320 \text{ kPa}$$

**Finalize** The higher the temperature, the higher the pressure exerted by the trapped gas as expected. If the pressure increases sufficiently, the can may explode. Because of this possibility, you should never dispose of spray cans in a fire.

**WHAT IF?** Suppose we include a volume change due to thermal expansion of the steel can as the temperature increases. Does that alter our answer for the final pressure significantly?

**Answer** Because the thermal expansion coefficient of steel is very small, we do not expect much of an effect on our final answer.

Find the change in the volume of the can using Equation 19.6 and the value for  $\alpha$  for steel from Table 19.1:

$$\begin{aligned} \Delta V &= \beta V_i \Delta T = 3\alpha V_i \Delta T \\ &= 3[11 \times 10^{-6} (\text{°C})^{-1}](125.00 \text{ cm}^3)(173 \text{ °C}) = 0.71 \text{ cm}^3 \end{aligned}$$

Start from Equation (2) again and find an equation for the final pressure:

$$P_f = \left(\frac{T_f}{T_i}\right)\left(\frac{V_i}{V_f}\right)P_i$$

This result differs from Equation (3) only in the factor  $V_i/V_f$ . Evaluate this factor:

$$\frac{V_i}{V_f} = \frac{125.00 \text{ cm}^3}{(125.00 \text{ cm}^3 + 0.71 \text{ cm}^3)} = 0.994 = 99.4\%$$

Therefore, the final pressure will differ by only 0.6% from the value calculated without considering the thermal expansion of the can. Taking 99.4% of the previous final pressure, the final pressure including thermal expansion is 318 kPa.

## Summary

### Definitions

Two objects are in **thermal equilibrium** with each other if they do not exchange energy when in thermal contact.



**Temperature** is the property that determines whether an object is in thermal equilibrium with other objects. Two objects in thermal equilibrium with each other are at the same temperature. The SI unit of absolute temperature is the **kelvin**, which is defined to be  $1/273.16$  of the difference between absolute zero and the temperature of the triple point of water.

## Concepts and Principles

The **zeroth law of thermodynamics** states that if objects A and B are separately in thermal equilibrium with a third object C, then objects A and B are in thermal equilibrium with each other.

When the temperature of an object is changed by an amount  $\Delta T$ , its length changes by an amount  $\Delta L$  that is proportional to  $\Delta T$  and to its initial length  $L_i$ :

$$\Delta L = \alpha L_i \Delta T \quad (19.4)$$

where the constant  $\alpha$  is the **average coefficient of linear expansion**. The **average coefficient of volume expansion**  $\beta$  for a solid is approximately equal to  $3\alpha$ .

An **ideal gas** is one for which  $PV/nT$  is constant. An ideal gas is described by the **equation of state**,

$$PV = nRT \quad (19.8)$$

where  $n$  equals the number of moles of the gas,  $P$  is its pressure,  $V$  is its volume,  $R$  is the universal gas constant ( $8.314 \text{ J/mol} \cdot \text{K}$ ), and  $T$  is the absolute temperature of the gas. A real gas behaves approximately as an ideal gas if it has a low density.

## Objective Questions

**1.** denotes answer available in *Student Solutions Manual/Study Guide*

- Markings to indicate length are placed on a steel tape in a room that is at a temperature of  $22^\circ\text{C}$ . Measurements are then made with the same tape on a day when the temperature is  $27^\circ\text{C}$ . Assume the objects you are measuring have a smaller coefficient of linear expansion than steel. Are the measurements (a) too long, (b) too short, or (c) accurate?
- When a certain gas under a pressure of  $5.00 \times 10^6 \text{ Pa}$  at  $25.0^\circ\text{C}$  is allowed to expand to 3.00 times its original volume, its final pressure is  $1.07 \times 10^6 \text{ Pa}$ . What is its final temperature? (a) 450 K (b) 233 K (c) 212 K (d) 191 K (e) 115 K
- If the volume of an ideal gas is doubled while its temperature is quadrupled, does the pressure (a) remain the same, (b) decrease by a factor of 2, (c) decrease by a factor of 4, (d) increase by a factor of 2, or (e) increase by a factor of 4?
- The pendulum of a certain pendulum clock is made of brass. When the temperature increases, what happens to the period of the clock? (a) It increases. (b) It decreases. (c) It remains the same.
- A temperature of  $162^\circ\text{F}$  is equivalent to what temperature in kelvins? (a) 373 K (b) 288 K (c) 345 K (d) 201 K (e) 308 K
- A cylinder with a piston holds  $0.50 \text{ m}^3$  of oxygen at an absolute pressure of 4.0 atm. The piston is pulled outward, increasing the volume of the gas until the pressure drops to 1.0 atm. If the temperature stays constant, what new volume does the gas occupy? (a)  $1.0 \text{ m}^3$  (b)  $1.5 \text{ m}^3$  (c)  $2.0 \text{ m}^3$  (d)  $0.12 \text{ m}^3$  (e)  $2.5 \text{ m}^3$
- What would happen if the glass of a thermometer expanded more on warming than did the liquid in the tube? (a) The thermometer would break. (b) It could be used only for temperatures below room temperature. (c) You would have to hold it with the bulb on top. (d) The scale on the thermometer is reversed so that higher temperature values would be found closer to the bulb. (e) The numbers would not be evenly spaced.
- A cylinder with a piston contains a sample of a thin gas. The kind of gas and the sample size can be changed. The cylinder can be placed in different constant-temperature baths, and the piston can be held in different positions. Rank the following cases according to the pressure of the gas from the highest to the lowest, displaying any cases of equality. (a) A 0.002-mol sample of oxygen is held at 300 K in a  $100\text{-cm}^3$  container. (b) A 0.002-mol sample of oxygen is held at 600 K in a  $200\text{-cm}^3$  container. (c) A 0.002-mol sample of oxygen is held at 600 K in a  $300\text{-cm}^3$  container. (d) A 0.004-mol sample of helium is held at 300 K in a  $200\text{-cm}^3$  container. (e) A 0.004-mol sample of helium is held at 250 K in a  $200\text{-cm}^3$  container.
- Two cylinders A and B at the same temperature contain the same quantity of the same kind of gas. Cylinder A has three times the volume of cylinder B. What can you conclude about the pressures the gases exert? (a) We can conclude nothing about the pressures.

- (b) The pressure in A is three times the pressure in B. (c) The pressures must be equal. (d) The pressure in A must be one-third the pressure in B.
- 10.** A rubber balloon is filled with 1 L of air at 1 atm and 300 K and is then put into a cryogenic refrigerator at 100 K. The rubber remains flexible as it cools. (i) What happens to the volume of the balloon? (a) It decreases to  $\frac{1}{3}$  L. (b) It decreases to  $1/\sqrt{3}$  L. (c) It is constant. (d) It increases to  $\sqrt{3}$  L. (e) It increases to 3 L. (ii) What happens to the pressure of the air in the balloon? (a) It decreases to  $\frac{1}{3}$  atm. (b) It decreases to  $1/\sqrt{3}$  atm. (c) It is constant. (d) It increases to  $\sqrt{3}$  atm. (e) It increases to 3 atm.
- 11.** The average coefficient of linear expansion of copper is  $17 \times 10^{-6} (\text{°C})^{-1}$ . The Statue of Liberty is 93 m tall on a summer morning when the temperature is 25°C. Assume the copper plates covering the statue are mounted edge to edge without expansion joints and do not buckle or bind on the framework supporting them as the day grows hot. What is the order of magnitude of the statue's increase in height? (a) 0.1 mm (b) 1 mm (c) 1 cm (d) 10 cm (e) 1 m
- 12.** Suppose you empty a tray of ice cubes into a bowl partly full of water and cover the bowl. After one-half hour, the contents of the bowl come to thermal equilibrium, with more liquid water and less ice than you started with. Which of the following is true? (a) The temperature of the liquid water is higher than the temperature of the remaining ice. (b) The temperature of the liquid water is the same as that of the ice. (c) The temperature of the liquid water is less than that of the ice. (d) The comparative temperatures of the liquid water and ice depend on the amounts present.
- 13.** A hole is drilled in a metal plate. When the metal is raised to a higher temperature, what happens to the diameter of the hole? (a) It decreases. (b) It increases. (c) It remains the same. (d) The answer depends on the initial temperature of the metal. (e) None of those answers is correct.
- 14.** On a very cold day in upstate New York, the temperature is  $-25^{\circ}\text{C}$ , which is equivalent to what Fahrenheit temperature? (a)  $-46^{\circ}\text{F}$  (b)  $-77^{\circ}\text{F}$  (c)  $18^{\circ}\text{F}$  (d)  $-25^{\circ}\text{F}$  (e)  $-13^{\circ}\text{F}$

### Conceptual Questions

**1.** denotes answer available in *Student Solutions Manual/Study Guide*

- 1.** Common thermometers are made of a mercury column in a glass tube. Based on the operation of these thermometers, which has the larger coefficient of linear expansion, glass or mercury? (Don't answer the question by looking in a table.)
- 2.** A piece of copper is dropped into a beaker of water. (a) If the water's temperature rises, what happens to the temperature of the copper? (b) Under what conditions are the water and copper in thermal equilibrium?
- 3.** (a) What does the ideal gas law predict about the volume of a sample of gas at absolute zero? (b) Why is this prediction incorrect?
- 4.** Some picnickers stop at a convenience store to buy some food, including bags of potato chips. They then drive up into the mountains to their picnic site. When they unload the food, they notice that the bags of chips are puffed up like balloons. Why did that happen?
- 5.** In describing his upcoming trip to the Moon, and as portrayed in the movie *Apollo 13* (Universal, 1995), astronaut Jim Lovell said, "I'll be walking in a place where there's a 400-degree difference between sunlight and shadow." Suppose an astronaut standing on the Moon holds a thermometer in his gloved hand. (a) Is the thermometer reading the temperature of the vacuum at the Moon's surface? (b) Does it read any temperature? If so, what object or substance has that temperature?
- 6.** Metal lids on glass jars can often be loosened by running hot water over them. Why does that work?
- 7.** An automobile radiator is filled to the brim with water when the engine is cool. (a) What happens to the water when the engine is running and the water has been raised to a high temperature? (b) What do modern automobiles have in their cooling systems to prevent the loss of coolants?
- 8.** When the metal ring and metal sphere in Figure CQ19.8 are both at room temperature, the sphere can barely be passed through the ring. (a) After the sphere is warmed in a flame, it cannot be passed through the ring. Explain. (b) **What If?** What if the ring is warmed and the sphere is left at room temperature? Does the sphere pass through the ring?

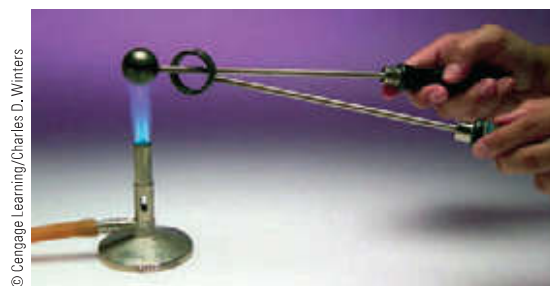


Figure CQ19.8

- 9.** Is it possible for two objects to be in thermal equilibrium if they are not in contact with each other? Explain.
- 10.** Use a periodic table of the elements (see Appendix C) to determine the number of grams in one mole of (a) hydrogen, which has diatomic molecules; (b) helium; and (c) carbon monoxide.

## Problems

ENHANCED

WebAssign

The problems found in this chapter may be assigned online in Enhanced WebAssign

1. straightforward; 2. intermediate; 3. challenging

1. full solution available in the *Student Solutions Manual/Study Guide*

AMT

Analysis Model tutorial available in Enhanced WebAssign

GP

Guided Problem

M

Master It tutorial available in Enhanced WebAssign

W

Watch It video solution available in Enhanced WebAssign

## Section 19.2 Thermometers and the Celsius Temperature Scale

## Section 19.3 The Constant-Volume Gas Thermometer and the Absolute Temperature Scale

- A nurse measures the temperature of a patient to be  $41.5^{\circ}\text{C}$ . (a) What is this temperature on the Fahrenheit scale? (b) Do you think the patient is seriously ill? Explain.
- The temperature difference between the inside and the outside of a home on a cold winter day is  $57.0^{\circ}\text{F}$ . Express this difference on (a) the Celsius scale and (b) the Kelvin scale.
- Convert the following temperatures to their values on the Fahrenheit and Kelvin scales: (a) the sublimation point of dry ice,  $-78.5^{\circ}\text{C}$ ; (b) human body temperature,  $37.0^{\circ}\text{C}$ .
- The boiling point of liquid hydrogen is  $20.3\text{ K}$  at atmospheric pressure. What is this temperature on (a) the Celsius scale and (b) the Fahrenheit scale?
- Liquid nitrogen has a boiling point of  $-195.81^{\circ}\text{C}$  at atmospheric pressure. Express this temperature (a) in degrees Fahrenheit and (b) in kelvins.
- Death Valley holds the record for the highest recorded temperature in the United States. On July 10, 1913, at a place called Furnace Creek Ranch, the temperature rose to  $134^{\circ}\text{F}$ . The lowest U.S. temperature ever recorded occurred at Prospect Creek Camp in Alaska on January 23, 1971, when the temperature plummeted to  $-79.8^{\circ}\text{F}$ . (a) Convert these temperatures to the Celsius scale. (b) Convert the Celsius temperatures to Kelvin.
- In a student experiment, a constant-volume gas thermometer is calibrated in dry ice ( $-78.5^{\circ}\text{C}$ ) and in boiling ethyl alcohol ( $78.0^{\circ}\text{C}$ ). The separate pressures are  $0.900\text{ atm}$  and  $1.635\text{ atm}$ . (a) What value of absolute zero in degrees Celsius does the calibration yield? What pressures would be found at (b) the freezing and (c) the boiling points of water? *Hint:* Use the linear relationship  $P = A + BT$ , where  $A$  and  $B$  are constants.

## Section 19.4 Thermal Expansion of Solids and Liquids

*Note:* Table 19.1 is available for use in solving problems in this section.

8. The concrete sections of a certain superhighway are designed to have a length of  $25.0\text{ m}$ . The sections are poured and cured at  $10.0^{\circ}\text{C}$ . What minimum spacing

should the engineer leave between the sections to eliminate buckling if the concrete is to reach a temperature of  $50.0^{\circ}\text{C}$ ?

9. The active element of a certain laser is made of a glass rod  $30.0\text{ cm}$  long and  $1.50\text{ cm}$  in diameter. Assume the average coefficient of linear expansion of the glass is equal to  $9.00 \times 10^{-6} (^{\circ}\text{C})^{-1}$ . If the temperature of the rod increases by  $65.0^{\circ}\text{C}$ , what is the increase in (a) its length, (b) its diameter, and (c) its volume?

10. **Review.** Inside the wall of a house, an L-shaped section of hot-water pipe consists of three parts: a straight, horizontal piece  $h = 28.0\text{ cm}$  long; an elbow; and a straight, vertical piece  $\ell = 134\text{ cm}$  long (Fig. P19.10). A stud and a second-story floorboard hold the ends of this section of copper pipe stationary. Find the magnitude and direction of the displacement of the pipe elbow when the water flow is turned on, raising the temperature of the pipe from  $18.0^{\circ}\text{C}$  to  $46.5^{\circ}\text{C}$ .

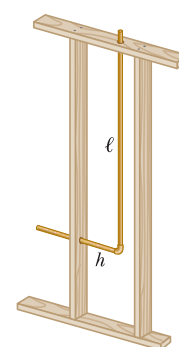


Figure P19.10

11. A copper telephone wire has essentially no sag between poles  $35.0\text{ m}$  apart on a winter day when the temperature is  $-20.0^{\circ}\text{C}$ . How much longer is the wire on a summer day when the temperature is  $35.0^{\circ}\text{C}$ ?
12. A pair of eyeglass frames is made of epoxy plastic. At room temperature ( $20.0^{\circ}\text{C}$ ), the frames have circular lens holes  $2.20\text{ cm}$  in radius. To what temperature must the frames be heated if lenses  $2.21\text{ cm}$  in radius are to be inserted in them? The average coefficient of linear expansion for epoxy is  $1.30 \times 10^{-4} (^{\circ}\text{C})^{-1}$ .
13. The Trans-Alaska pipeline is  $1\,300\text{ km}$  long, reaching from Prudhoe Bay to the port of Valdez. It experiences temperatures from  $-73^{\circ}\text{C}$  to  $+35^{\circ}\text{C}$ . How much does the steel pipeline expand because of the difference in temperature? How can this expansion be compensated for?
14. Each year thousands of children are badly burned by hot tap water. Figure P19.14 (page 584) shows a cross-sectional view of an antiscalding faucet attachment designed to prevent such accidents. Within the device, a spring made of material with a high coefficient of thermal expansion controls a movable plunger. When the



water temperature rises above a preset safe value, the expansion of the spring causes the plunger to shut off the water flow. Assuming that the initial length  $L$  of the unstressed spring is 2.40 cm and its coefficient of linear expansion is  $22.0 \times 10^{-6} (\text{°C})^{-1}$ , determine the increase in length of the spring when the water temperature rises by  $30.0\text{°C}$ . (You will find the increase in length to be small. Therefore, to provide a greater variation in valve opening for the temperature change anticipated, actual devices have a more complicated mechanical design.)

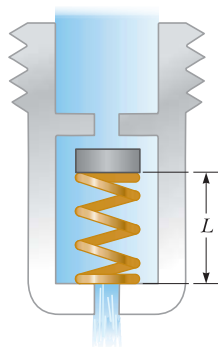


Figure P19.14

15. A square hole 8.00 cm along each side is cut in a sheet of copper. (a) Calculate the change in the area of this hole resulting when the temperature of the sheet is increased by 50.0 K. (b) Does this change represent an increase or a decrease in the area enclosed by the hole?
16. The average coefficient of volume expansion for carbon tetrachloride is  $5.81 \times 10^{-4} (\text{°C})^{-1}$ . If a 50.0-gal steel container is filled completely with carbon tetrachloride when the temperature is  $10.0\text{°C}$ , how much will spill over when the temperature rises to  $30.0\text{°C}$ ?
17. At  $20.0\text{°C}$ , an aluminum ring has an inner diameter of  $5.0000\text{ cm}$  and a brass rod has a diameter of  $5.0500\text{ cm}$ . (a) If only the ring is warmed, what temperature must it reach so that it will just slip over the rod? (b) **What If?** If both the ring and the rod are warmed together, what temperature must they both reach so that the ring barely slips over the rod? (c) Would this latter process work? Explain. *Hint:* Consult Table 20.2 in the next chapter.
18. **W** Why is the following situation impossible? A thin brass ring has an inner diameter  $10.00\text{ cm}$  at  $20.0\text{°C}$ . A solid aluminum cylinder has diameter  $10.02\text{ cm}$  at  $20.0\text{°C}$ . Assume the average coefficients of linear expansion of the two metals are constant. Both metals are cooled together to a temperature at which the ring can be slipped over the end of the cylinder.
19. **A** A volumetric flask made of Pyrex is calibrated at  $20.0\text{°C}$ . It is filled to the 100-mL mark with  $35.0\text{°C}$  acetone. After the flask is filled, the acetone cools and the flask warms so that the combination of acetone and flask reaches a uniform temperature of  $32.0\text{°C}$ . The combination is then cooled back to  $20.0\text{°C}$ . (a) What is the volume of the acetone when it cools to  $20.0\text{°C}$ ? (b) At the temperature of  $32.0\text{°C}$ , does the level of acetone lie above or below the 100-mL mark on the flask? Explain.
20. **Review.** On a day that the temperature is  $20.0\text{°C}$ , a concrete walk is poured in such a way that the ends of the walk are unable to move. Take Young's modulus for concrete to be  $7.00 \times 10^9\text{ N/m}^2$  and the compressive strength to be  $2.00 \times 10^9\text{ N/m}^2$ . (a) What is the stress in the cement on a hot day of  $50.0\text{°C}$ ? (b) Does the concrete fracture?

21. A hollow aluminum cylinder 20.0 cm deep has an internal capacity of 2.000 L at  $20.0\text{°C}$ . It is completely filled with turpentine at  $20.0\text{°C}$ . The turpentine and the aluminum cylinder are then slowly warmed together to  $80.0\text{°C}$ . (a) How much turpentine overflows? (b) What is the volume of turpentine remaining in the cylinder at  $80.0\text{°C}$ ? (c) If the combination with this amount of turpentine is then cooled back to  $20.0\text{°C}$ , how far below the cylinder's rim does the turpentine's surface recede?
22. **Review.** The Golden Gate Bridge in San Francisco has a main span of length 1.28 km, one of the longest in the world. Imagine that a steel wire with this length and a cross-sectional area of  $4.00 \times 10^{-6}\text{ m}^2$  is laid in a straight line on the bridge deck with its ends attached to the towers of the bridge. On a summer day the temperature of the wire is  $35.0\text{°C}$ . (a) When winter arrives, the towers stay the same distance apart and the bridge deck keeps the same shape as its expansion joints open. When the temperature drops to  $-10.0\text{°C}$ , what is the tension in the wire? Take Young's modulus for steel to be  $20.0 \times 10^{10}\text{ N/m}^2$ . (b) Permanent deformation occurs if the stress in the steel exceeds its elastic limit of  $3.00 \times 10^8\text{ N/m}^2$ . At what temperature would the wire reach its elastic limit? (c) **What If?** Explain how your answers to parts (a) and (b) would change if the Golden Gate Bridge were twice as long.
23. A sample of lead has a mass of 20.0 kg and a density of  $11.3 \times 10^3\text{ kg/m}^3$  at  $0\text{°C}$ . (a) What is the density of lead at  $90.0\text{°C}$ ? (b) What is the mass of the sample of lead at  $90.0\text{°C}$ ?
24. A sample of a solid substance has a mass  $m$  and a density  $\rho_0$  at a temperature  $T_0$ . (a) Find the density of the substance if its temperature is increased by an amount  $\Delta T$  in terms of the coefficient of volume expansion  $\beta$ . (b) What is the mass of the sample if the temperature is raised by an amount  $\Delta T$ ?
25. **M** An underground gasoline tank can hold  $1.00 \times 10^3$  gallons of gasoline at  $52.0\text{°F}$ . Suppose the tank is being filled on a day when the outdoor temperature (and the temperature of the gasoline in a tanker truck) is  $95.0\text{°F}$ . When the underground tank registers that it is full, how many gallons have been transferred from the truck, according to a non-temperature-compensated gauge on the truck? Assume the temperature of the gasoline quickly cools from  $95.0\text{°F}$  to  $52.0\text{°F}$  upon entering the tank.

### Section 19.5 Macroscopic Description of an Ideal Gas

26. A rigid tank contains 1.50 moles of an ideal gas. Determine the number of moles of gas that must be withdrawn from the tank to lower the pressure of the gas from 25.0 atm to 5.00 atm. Assume the volume of the tank and the temperature of the gas remain constant during this operation.
27. Gas is confined in a tank at a pressure of 11.0 atm and a temperature of  $25.0\text{°C}$ . If two-thirds of the gas

is withdrawn and the temperature is raised to  $75.0^{\circ}\text{C}$ , what is the pressure of the gas remaining in the tank?

28. Your father and your younger brother are confronted with the same puzzle. Your father's garden sprayer and your brother's water cannon both have tanks with a capacity of 5.00 L (Fig. P19.28). Your father puts a negligible amount of concentrated fertilizer into his tank. They both pour in 4.00 L of water and seal up their tanks, so the tanks also contain air at atmospheric pressure. Next, each uses a hand-operated pump to inject more air until the absolute pressure in the tank reaches 2.40 atm. Now each uses his device to spray out water—not air—until the stream becomes feeble, which it does when the pressure in the tank reaches 1.20 atm. To accomplish spraying out all the water, each finds he must pump up the tank three times. Here is the puzzle: most of the water sprays out after the second pumping. The first and the third pumping-up processes seem just as difficult as the second but result in a much smaller amount of water coming out. Account for this phenomenon.

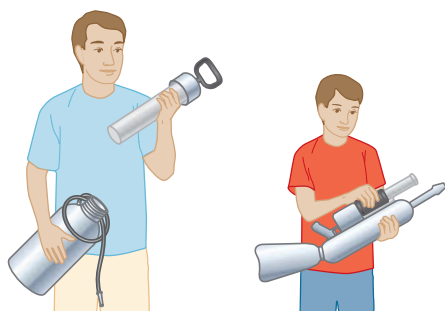


Figure P19.28

29. Gas is contained in an 8.00-L vessel at a temperature of  $20.0^{\circ}\text{C}$  and a pressure of 9.00 atm. (a) Determine the number of moles of gas in the vessel. (b) How many molecules are in the vessel?
30. A container in the shape of a cube 10.0 cm on each edge contains air (with equivalent molar mass  $28.9\text{ g/mol}$ ) at atmospheric pressure and temperature  $300\text{ K}$ . Find (a) the mass of the gas, (b) the gravitational force exerted on it, and (c) the force it exerts on each face of the cube. (d) Why does such a small sample exert such a great force?
31. An auditorium has dimensions  $10.0\text{ m} \times 20.0\text{ m} \times 30.0\text{ m}$ . How many molecules of air fill the auditorium at  $20.0^{\circ}\text{C}$  and a pressure of 101 kPa (1.00 atm)?
32. The pressure gauge on a tank registers the gauge pressure, which is the difference between the interior pressure and exterior pressure. When the tank is full of oxygen ( $\text{O}_2$ ), it contains 12.0 kg of the gas at a gauge pressure of 40.0 atm. Determine the mass of oxygen that has been withdrawn from the tank when the pressure reading is 25.0 atm. Assume the temperature of the tank remains constant.
33. (a) Find the number of moles in one cubic meter of an ideal gas at  $20.0^{\circ}\text{C}$  and atmospheric pressure. (b) For air, Avogadro's number of molecules has mass 28.9 g. Calculate the mass of one cubic meter of air. (c) State how this result compares with the tabulated density of air at  $20.0^{\circ}\text{C}$ .
34. Use the definition of Avogadro's number to find the mass of a helium atom.
35. A popular brand of cola contains 6.50 g of carbon dioxide dissolved in 1.00 L of soft drink. If the evaporating carbon dioxide is trapped in a cylinder at 1.00 atm and  $20.0^{\circ}\text{C}$ , what volume does the gas occupy?
36. In state-of-the-art vacuum systems, pressures as low as  $1.00 \times 10^{-9}\text{ Pa}$  are being attained. Calculate the number of molecules in a  $1.00\text{-m}^3$  vessel at this pressure and a temperature of  $27.0^{\circ}\text{C}$ .
37. An automobile tire is inflated with air originally at  $10.0^{\circ}\text{C}$  and normal atmospheric pressure. During the process, the air is compressed to 28.0% of its original volume and the temperature is increased to  $40.0^{\circ}\text{C}$ . (a) What is the tire pressure? (b) After the car is driven at high speed, the tire's air temperature rises to  $85.0^{\circ}\text{C}$  and the tire's interior volume increases by 2.00%. What is the new tire pressure (absolute)?
38. **Review.** To measure how far below the ocean surface a bird dives to catch a fish, a scientist uses a method originated by Lord Kelvin. He dusts the interiors of plastic tubes with powdered sugar and then seals one end of each tube. He captures the bird at nighttime in its nest and attaches a tube to its back. He then catches the same bird the next night and removes the tube. In one trial, using a tube 6.50 cm long, water washes away the sugar over a distance of 2.70 cm from the open end of the tube. Find the greatest depth to which the bird dived, assuming the air in the tube stayed at constant temperature.
39. **Review.** The mass of a hot-air balloon and its cargo (not including the air inside) is 200 kg. The air outside is at  $10.0^{\circ}\text{C}$  and 101 kPa. The volume of the balloon is  $400\text{ m}^3$ . To what temperature must the air in the balloon be warmed before the balloon will lift off? (Air density at  $10.0^{\circ}\text{C}$  is  $1.244\text{ kg/m}^3$ .)
40. A room of volume  $V$  contains air having equivalent molar mass  $M$  (in g/mol). If the temperature of the room is raised from  $T_1$  to  $T_2$ , what mass of air will leave the room? Assume that the air pressure in the room is maintained at  $P_0$ .
41. **Review.** At 25.0 m below the surface of the sea, where the temperature is  $5.00^{\circ}\text{C}$ , a diver exhales an air bubble having a volume of  $1.00\text{ cm}^3$ . If the surface temperature of the sea is  $20.0^{\circ}\text{C}$ , what is the volume of the bubble just before it breaks the surface?
42. Estimate the mass of the air in your bedroom. State the quantities you take as data and the value you measure or estimate for each.
43. A cook puts 9.00 g of water in a 2.00-L pressure cooker that is then warmed to  $500^{\circ}\text{C}$ . What is the pressure inside the container?
44. The pressure gauge on a cylinder of gas registers the gauge pressure, which is the difference between the

interior pressure and the exterior pressure  $P_0$ . Let's call the gauge pressure  $P_g$ . When the cylinder is full, the mass of the gas in it is  $m_i$  at a gauge pressure of  $P_{gi}$ . Assuming the temperature of the cylinder remains constant, show that the mass of the gas *remaining* in the cylinder when the pressure reading is  $P_{gf}$  is given by

$$m_f = m_i \left( \frac{P_{gf} + P_0}{P_{gi} + P_0} \right)$$

### Additional Problems

45. Long-term space missions require reclamation of the oxygen in the carbon dioxide exhaled by the crew. In one method of reclamation, 1.00 mol of carbon dioxide produces 1.00 mol of oxygen and 1.00 mol of methane as a byproduct. The methane is stored in a tank under pressure and is available to control the attitude of the spacecraft by controlled venting. A single astronaut exhales 1.09 kg of carbon dioxide each day. If the methane generated in the respiration recycling of three astronauts during one week of flight is stored in an originally empty 150-L tank at  $-45.0^\circ\text{C}$ , what is the final pressure in the tank?
46. A steel beam being used in the construction of a skyscraper has a length of 35.000 m when delivered on a cold day at a temperature of  $15.000^\circ\text{F}$ . What is the length of the beam when it is being installed later on a warm day when the temperature is  $90.000^\circ\text{F}$ ?
47. A spherical steel ball bearing has a diameter of 2.540 cm at  $25.00^\circ\text{C}$ . (a) What is its diameter when its temperature is raised to  $100.0^\circ\text{C}$ ? (b) What temperature change is required to increase its volume by 1.000%?
48. A bicycle tire is inflated to a gauge pressure of 2.50 atm when the temperature is  $15.0^\circ\text{C}$ . While a man rides the bicycle, the temperature of the tire rises to  $45.0^\circ\text{C}$ . Assuming the volume of the tire does not change, find the gauge pressure in the tire at the higher temperature.
49. In a chemical processing plant, a reaction chamber of fixed volume  $V_0$  is connected to a reservoir chamber of fixed volume  $4V_0$  by a passage containing a thermally insulating porous plug. The plug permits the chambers to be at different temperatures. The plug allows gas to pass from either chamber to the other, ensuring that the pressure is the same in both. At one point in the processing, both chambers contain gas at a pressure of 1.00 atm and a temperature of  $27.0^\circ\text{C}$ . Intake and exhaust valves to the pair of chambers are closed. The reservoir is maintained at  $27.0^\circ\text{C}$  while the reaction chamber is heated to  $400^\circ\text{C}$ . What is the pressure in both chambers after that is done?
50. Why is the following situation impossible? An apparatus is designed so that steam initially at  $T = 150^\circ\text{C}$ ,  $P = 1.00$  atm, and  $V = 0.500$  m<sup>3</sup> in a piston-cylinder apparatus undergoes a process in which (1) the volume remains constant and the pressure drops to 0.870 atm, followed by (2) an expansion in which the pressure remains constant and the volume increases to 1.00 m<sup>3</sup>, followed by (3) a return to the initial conditions. It is

important that the pressure of the gas never fall below 0.850 atm so that the piston will support a delicate and very expensive part of the apparatus. Without such support, the delicate apparatus can be severely damaged and rendered useless. When the design is turned into a working prototype, it operates perfectly.

51. A mercury thermometer is constructed as shown in Figure P19.51. The Pyrex glass capillary tube has a diameter of 0.004 00 cm, and the bulb has a diameter of 0.250 cm. Find the change in height of the mercury column that occurs with a temperature change of  $30.0^\circ\text{C}$ .

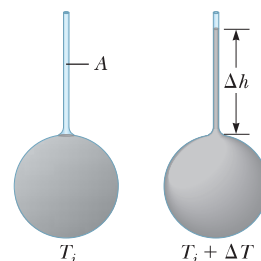


Figure P19.51

Problems 51 and 52.

52. A liquid with a coefficient of volume expansion  $\beta$  just fills a spherical shell of volume  $V$  (Fig. P19.51). The shell and the open capillary of area  $A$  projecting from the top of the sphere are made of a material with an average coefficient of linear expansion  $\alpha$ . The liquid is free to expand into the capillary. Assuming the temperature increases by  $\Delta T$ , find the distance  $\Delta h$  the liquid rises in the capillary.
53. Review. An aluminum pipe is open at both ends and used as a flute. The pipe is cooled to  $5.00^\circ\text{C}$ , at which its length is 0.655 m. As soon as you start to play it, the pipe fills with air at  $20.0^\circ\text{C}$ . After that, by how much does its fundamental frequency change as the metal rises in temperature to  $20.0^\circ\text{C}$ ?

54. Two metal bars are made of invar and a third bar is made of aluminum. At  $0^\circ\text{C}$ , each of the three bars is drilled with two holes 40.0 cm apart. Pins are put through the holes to assemble the bars into an equilateral triangle as in Figure P19.54. (a) First ignore the expansion of the invar. Find

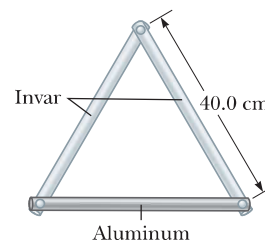


Figure P19.54

- the angle between the invar bars as a function of Celsius temperature. (b) Is your answer accurate for negative as well as positive temperatures? (c) Is it accurate for  $0^\circ\text{C}$ ? (d) Solve the problem again, including the expansion of the invar. Aluminum melts at  $660^\circ\text{C}$  and invar at  $1427^\circ\text{C}$ . Assume the tabulated expansion coefficients are constant. What are (e) the greatest and (f) the smallest attainable angles between the invar bars?
55. A student measures the length of a brass rod with a steel tape at  $20.0^\circ\text{C}$ . The reading is 95.00 cm. What will the tape indicate for the length of the rod when the rod and the tape are at (a)  $-15.0^\circ\text{C}$  and (b)  $55.0^\circ\text{C}$ ?
56. The density of gasoline is 730 kg/m<sup>3</sup> at  $0^\circ\text{C}$ . Its average coefficient of volume expansion is  $9.60 \times 10^{-4} (\text{C}^\circ)^{-1}$ . Assume 1.00 gal of gasoline occupies 0.003 80 m<sup>3</sup>.



How many extra kilograms of gasoline would you receive if you bought 10.0 gal of gasoline at  $0^\circ\text{C}$  rather than at  $20.0^\circ\text{C}$  from a pump that is not temperature compensated?

- 57.** A liquid has a density  $\rho$ . (a) Show that the fractional change in density for a change in temperature  $\Delta T$  is  $\Delta\rho/\rho = -\beta\Delta T$ . (b) What does the negative sign signify? (c) Fresh water has a maximum density of  $1.000\,0\text{ g/cm}^3$  at  $4.0^\circ\text{C}$ . At  $10.0^\circ\text{C}$ , its density is  $0.999\,7\text{ g/cm}^3$ . What is  $\beta$  for water over this temperature interval? (d) At  $0^\circ\text{C}$ , the density of water is  $0.999\,9\text{ g/cm}^3$ . What is the value for  $\beta$  over the temperature range  $0^\circ\text{C}$  to  $4.00^\circ\text{C}$ ?

- 58.** (a) Take the definition of the coefficient of volume expansion to be

$$\beta = \frac{1}{V} \left. \frac{dV}{dT} \right|_{P=\text{constant}} = \frac{1}{V} \frac{\partial V}{\partial T}$$

Use the equation of state for an ideal gas to show that the coefficient of volume expansion for an ideal gas at constant pressure is given by  $\beta = 1/T$ , where  $T$  is the absolute temperature. (b) What value does this expression predict for  $\beta$  at  $0^\circ\text{C}$ ? State how this result compares with the experimental values for (c) helium and (d) air in Table 19.1. *Note:* These values are much larger than the coefficients of volume expansion for most liquids and solids.

- 59. Review.** A clock with a brass pendulum has a period of  $1.000\text{ s}$  at  $20.0^\circ\text{C}$ . If the temperature increases to  $30.0^\circ\text{C}$ , (a) by how much does the period change and (b) how much time does the clock gain or lose in one week?

- 60.** A bimetallic strip of length  $L$  is made of two ribbons of different metals bonded together. (a) First assume the strip is originally straight. As the strip is warmed, the metal with the greater average coefficient of expansion expands more than the other, forcing the strip into an arc with the outer radius having a greater circumference (Fig. P19.60). Derive an expression for the angle of bending  $\theta$  as a function of the initial length of the strips, their average coefficients of linear expansion, the change in temperature, and the separation of the centers of the strips ( $\Delta r = r_2 - r_1$ ). (b) Show that the angle of bending decreases to zero when  $\Delta T$  decreases to zero and also when the two average coefficients of expansion become equal. (c) **What If?** What happens if the strip is cooled?

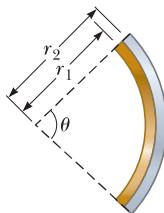


Figure P19.60

- 61.** The rectangular plate shown in Figure P19.61 has an area  $A_i$  equal to  $\ell w$ . If the temperature increases by  $\Delta T$ ,

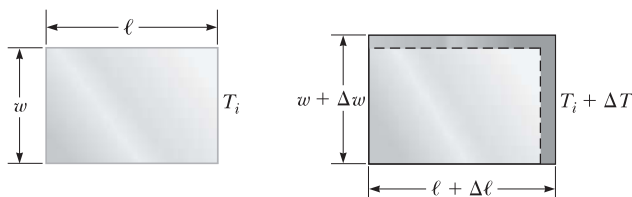


Figure P19.61

each dimension increases according to Equation 19.4, where  $\alpha$  is the average coefficient of linear expansion. (a) Show that the increase in area is  $\Delta A = 2\alpha A_i \Delta T$ . (b) What approximation does this expression assume?

- 62.** The measurement of the average coefficient of volume expansion  $\beta$  for a liquid is complicated because the container also changes size with temperature. Figure P19.62 shows a simple means for measuring  $\beta$  despite the expansion of the container. With this apparatus, one arm of a U-tube is maintained at  $0^\circ\text{C}$  in a water-ice bath, and the other arm is maintained at a different temperature  $T_C$  in a constant-temperature bath. The connecting tube is horizontal. A difference in the length or diameter of the tube between the two arms of the U-tube has no effect on the pressure balance at the bottom of the tube because the pressure depends only on the depth of the liquid. Derive an expression for  $\beta$  for the liquid in terms of  $h_0$ ,  $h_i$ , and  $T_C$ .

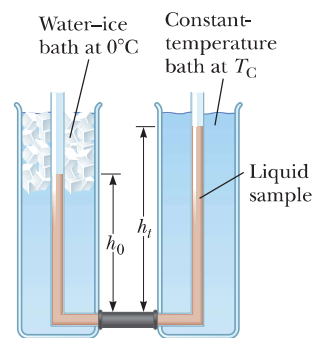


Figure P19.62

- 63.** A copper rod and a steel rod are different in length by  $5.00\text{ cm}$  at  $0^\circ\text{C}$ . The rods are warmed and cooled together. (a) Is it possible that the length difference remains constant at all temperatures? Explain. (b) If so, describe the lengths at  $0^\circ\text{C}$  as precisely as you can. Can you tell which rod is longer? Can you tell the lengths of the rods?

- 64.** A vertical cylinder of cross-sectional area  $A$  is fitted with a tight-fitting, frictionless piston of mass  $m$  (Fig. P19.64). The piston is not restricted in its motion in any way and is supported by the gas at pressure  $P$  below it. Atmospheric pressure is  $P_0$ . We wish to find the height  $h$  in Figure P19.64. (a) What analysis model is appropriate to describe the piston? (b) Write an appropriate force equation for the piston from this analysis model in terms of  $P$ ,  $P_0$ ,  $m$ ,  $A$ , and  $g$ . (c) Suppose  $n$  moles of an ideal gas are in the cylinder at a temperature of  $T$ . Substitute for  $P$  in your answer to part (b) to find the height  $h$  of the piston above the bottom of the cylinder.

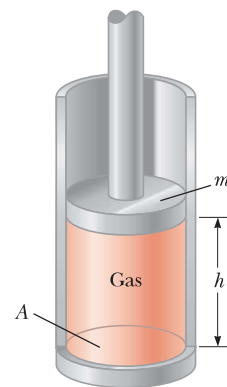


Figure P19.64

- 65. Review.** Consider an object with any one of the shapes displayed in Table 10.2. What is the percentage increase in the moment of inertia of the object when it is warmed from  $0^\circ\text{C}$  to  $100^\circ\text{C}$  if it is composed of (a) copper or (b) aluminum? Assume the average linear expansion coefficients shown in Table 19.1 do not vary between  $0^\circ\text{C}$  and  $100^\circ\text{C}$ . (c) Why are the answers for parts (a) and (b) the same for all the shapes?

66. (a) Show that the density of an ideal gas occupying a volume  $V$  is given by  $\rho = PM/RT$ , where  $M$  is the molar mass. (b) Determine the density of oxygen gas at atmospheric pressure and  $20.0^\circ\text{C}$ .

67. Two concrete spans of a 250-m-long bridge are placed end to end so that no room is allowed for expansion (Fig. P19.67a). If a temperature increase of  $20.0^\circ\text{C}$  occurs, what is the height  $y$  to which the spans rise when they buckle (Fig. P19.67b)?

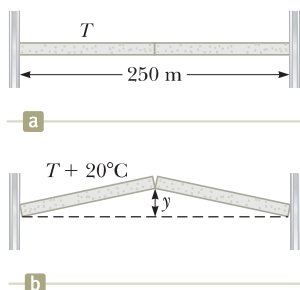


Figure P19.67

Problems 67 and 68.

68. Two concrete spans that form a bridge of length  $L$  are placed end to end so that no room is allowed for expansion (Fig. P19.67a). If a temperature increase of  $\Delta T$  occurs, what is the height  $y$  to which the spans rise when they buckle (Fig. P19.67b)?

69. **Review.** (a) Derive an expression for the buoyant force on a spherical balloon, submerged in water, as a function of the depth  $h$  below the surface, the volume  $V_i$  of the balloon at the surface, the pressure  $P_0$  at the surface, and the density  $\rho_w$  of the water. Assume the water temperature does not change with depth. (b) Does the buoyant force increase or decrease as the balloon is submerged? (c) At what depth is the buoyant force one-half the surface value?

70. **Review.** Following a collision in outer space, a copper disk at  $850^\circ\text{C}$  is rotating about its axis with an angular speed of  $25.0\text{ rad/s}$ . As the disk radiates infrared light, its temperature falls to  $20.0^\circ\text{C}$ . No external torque acts on the disk. (a) Does the angular speed change as the disk cools? Explain how it changes or why it does not. (b) What is its angular speed at the lower temperature?

71. Starting with Equation 19.10, show that the total pressure  $P$  in a container filled with a mixture of several ideal gases is  $P = P_1 + P_2 + P_3 + \dots$ , where  $P_1, P_2, \dots$  are the pressures that each gas would exert if it alone filled the container. (These individual pressures are called the *partial pressures* of the respective gases.) This result is known as *Dalton's law of partial pressures*.

### Challenge Problems

72. **Review.** A steel wire and a copper wire, each of diameter 2.000 mm, are joined end to end. At  $40.0^\circ\text{C}$ , each has an unstretched length of 2.000 m. The wires are connected between two fixed supports 4.000 m apart on a tabletop. The steel wire extends from  $x = -2.000\text{ m}$  to  $x = 0$ , the copper wire extends from  $x = 0$  to  $x = 2.000\text{ m}$ , and the tension is negligible. The temperature is then lowered to  $20.0^\circ\text{C}$ . Assume the average coefficient of linear expansion of steel is  $11.0 \times 10^{-6} (^\circ\text{C})^{-1}$  and that of copper is  $17.0 \times 10^{-6} (^\circ\text{C})^{-1}$ . Take Young's modulus for steel to be  $20.0 \times 10^{10}\text{ N/m}^2$  and that for

copper to be  $11.0 \times 10^{10}\text{ N/m}^2$ . At this lower temperature, find (a) the tension in the wire and (b) the  $x$  coordinate of the junction between the wires.

73. **Review.** A steel guitar string with a diameter of 1.00 mm is stretched between supports 80.0 cm apart. The temperature is  $0.0^\circ\text{C}$ . (a) Find the mass per unit length of this string. (Use the value  $7.86 \times 10^3\text{ kg/m}^3$  for the density.) (b) The fundamental frequency of transverse oscillations of the string is 200 Hz. What is the tension in the string? Next, the temperature is raised to  $30.0^\circ\text{C}$ . Find the resulting values of (c) the tension and (d) the fundamental frequency. Assume both the Young's modulus of  $20.0 \times 10^{10}\text{ N/m}^2$  and the average coefficient of expansion  $\alpha = 11.0 \times 10^{-6} (^\circ\text{C})^{-1}$  have constant values between  $0.0^\circ\text{C}$  and  $30.0^\circ\text{C}$ .

74. A cylinder is closed by a piston connected to a spring of constant  $2.00 \times 10^3\text{ N/m}$  (see Fig. P19.74). With the spring relaxed, the cylinder is filled with 5.00 L of gas at a pressure of 1.00 atm and a temperature of  $20.0^\circ\text{C}$ . (a) If the piston has a cross-sectional area of  $0.0100\text{ m}^2$  and negligible mass, how high will it rise when the temperature is raised to  $250^\circ\text{C}$ ? (b) What is the pressure of the gas at  $250^\circ\text{C}$ ?

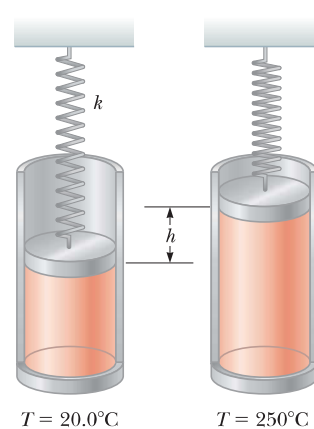


Figure P19.74

75. Helium gas is sold in steel tanks that will rupture if subjected to tensile stress greater than its yield strength of  $5 \times 10^8\text{ N/m}^2$ . If the helium is used to inflate a balloon, could the balloon lift the spherical tank the helium came in? Justify your answer. *Suggestion:* You may consider a spherical steel shell of radius  $r$  and thickness  $t$  having the density of iron and on the verge of breaking apart into two hemispheres because it contains helium at high pressure.

76. A cylinder that has a 40.0-cm radius and is 50.0 cm deep is filled with air at  $20.0^\circ\text{C}$  and 1.00 atm (Fig. P19.76a). A 20.0-kg piston is now lowered into the cylinder, compressing the air trapped inside as it takes equilibrium height  $h_i$  (Fig. P19.76b). Finally, a 25.0-kg dog stands on the piston, further compressing the air, which remains at  $20^\circ\text{C}$  (Fig. P19.76c). (a) How far down

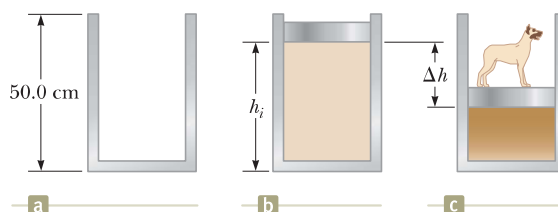


Figure P19.76

( $\Delta h$ ) does the piston move when the dog steps onto it?  
 (b) To what temperature should the gas be warmed to raise the piston and dog back to  $h_i$ ?

77. The relationship  $L = L_i + \alpha L_i \Delta T$  is a valid approximation when  $\alpha \Delta T$  is small. If  $\alpha \Delta T$  is large, one must integrate the relationship  $dL = \alpha L dT$  to determine the final length. (a) Assuming the coefficient of linear expansion of a material is constant as  $L$  varies, determine a general expression for the final length of a rod made of the material. Given a rod of length 1.00 m and a temperature change of 100.0°C, determine the error caused by the approximation when (b)  $\alpha = 2.00 \times 10^{-5} (\text{°C})^{-1}$  (a typical value for a metal) and (c) when  $\alpha = 0.0200 (\text{°C})^{-1}$  (an unrealistically large value for comparison). (d) Using the equation from part (a), solve Problem 21 again to find more accurate results.

78. **Review.** A house roof is a perfectly flat plane that makes an angle  $\theta$  with the horizontal. When its temperature changes, between  $T_c$  before dawn each day and  $T_h$  in the middle of each afternoon, the roof expands and contracts uniformly with a coefficient of thermal expansion  $\alpha_1$ . Resting on the roof is a flat, rectangular metal plate with expansion coefficient  $\alpha_2$ , greater than  $\alpha_1$ . The length of the plate is  $L$ , measured along the slope of the roof. The component of the plate's weight perpendicular to the roof is supported by a normal force uniformly distributed over the area of the plate. The coefficient of kinetic friction between the plate and the roof is  $\mu_k$ . The plate is always at the same temperature as the roof, so we assume its temperature is continuously changing. Because of the difference in expansion coefficients, each bit of the plate is moving relative to the roof below it, except for points along a certain horizontal line running across the plate called the stationary line. If the temperature is rising, parts

of the plate below the stationary line are moving down relative to the roof and feel a force of kinetic friction acting up the roof. Elements of area above the stationary line are sliding up the roof, and on them kinetic friction acts downward parallel to the roof. The stationary line occupies no area, so we assume no force of static friction acts on the plate while the temperature is changing. The plate as a whole is very nearly in equilibrium, so the net friction force on it must be equal to the component of its weight acting down the incline. (a) Prove that the stationary line is at a distance of

$$\frac{L}{2} \left( 1 - \frac{\tan \theta}{\mu_k} \right)$$

below the top edge of the plate. (b) Analyze the forces that act on the plate when the temperature is falling and prove that the stationary line is at that same distance above the bottom edge of the plate. (c) Show that the plate steps down the roof like an inchworm, moving each day by the distance

$$\frac{L}{\mu_k} (\alpha_2 - \alpha_1) (T_h - T_c) \tan \theta$$

(d) Evaluate the distance an aluminum plate moves each day if its length is 1.20 m, the temperature cycles between 4.00°C and 36.0°C, and if the roof has slope 18.5°, coefficient of linear expansion  $1.50 \times 10^{-5} (\text{°C})^{-1}$ , and coefficient of friction 0.420 with the plate. (e) **What If?** What if the expansion coefficient of the plate is less than that of the roof? Will the plate creep up the roof?

79. A 1.00-km steel railroad rail is fastened securely at both ends when the temperature is 20.0°C. As the temperature increases, the rail buckles, taking the shape of an arc of a vertical circle. Find the height  $h$  of the center of the rail when the temperature is 25.0°C. (You will need to solve a transcendental equation.)