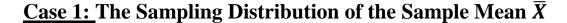
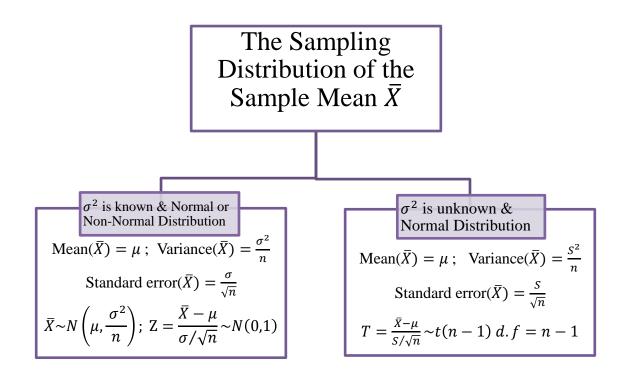
# **Chapter 5: The Sampling Distributions of Sample Statistics:**





### <u>Case 2:</u> The Sampling Distribution of the Difference between two Sample Means $\overline{X}_1 - \overline{X}_2$ :

When  $n \ge 30 \& \sigma_1^2$  and  $\sigma_2^2$  are Known & Normal or Non-Normal distribution.

Then

Mean
$$(\bar{X}_1 - \bar{X}_2) = \mu_1 - \mu_2$$
  
Variance $(\bar{X}_1 - \bar{X}_2) = \frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}$   
Standard error $(\bar{X}_1 - \bar{X}_2) = \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$ 

$$\bar{X}_1 - \bar{X}_2 \sim N\left(\mu_1 - \mu_2, \frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}\right)$$
$$Z = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}} \sim N(0, 1)$$

#### <u>Case 3:</u> The Sampling Distribution of the Sample Proportion $\hat{p}$ :

When  $n \ge 30$ , np > 5, nq > 5 and  $\hat{p} = \frac{x}{n}$ .

Then

Mean 
$$(\hat{p}) = p$$
  
Variance  $(\hat{p}) = \frac{pq}{n}$   
Standard error $(\hat{p}) = \sqrt{\frac{pq}{n}}$   
 $\hat{p} \sim N\left(p, \frac{pq}{n}\right)$   
 $Z = \frac{\hat{p} - p}{\sqrt{\frac{pq}{n}}} \sim N(0, 1)$ 

## <u>Case 4:</u> The Sampling Distribution of Difference between two Sample Proportions $\hat{p}_1 - \hat{p}_2$ :

When  $n_1 \ge 30, n_2 \ge 30, n_1 p_1 > 5, n_1 q_1 > 5, n_2 p_2 > 5, n_2 q_2 > 5$  and  $\hat{p}_1 = \frac{X_1}{n_1}, \hat{p}_2 = \frac{X_2}{n_2};$  $\hat{p}_1 - \hat{p}_2 = \frac{X_1}{n_1} - \frac{X_2}{n_2}.$ 

Then

Mean 
$$(\hat{p}_1 - \hat{p}_2) = p_1 - p_2$$
  
Variance  $(\hat{p}_1 - \hat{p}_2) = \frac{p_1 q_1}{n_1} + \frac{p_2 q_2}{n_2}$ 

Standard deviation 
$$(\hat{p}_1 - \hat{p}_2) = \sqrt{\frac{p_1 q_1}{n_1} + \frac{p_2 q_2}{n_2}}$$
  
 $\hat{p}_1 - \hat{p}_2 \sim N\left(p_1 - p_2, \frac{p_1 q_1}{n_1} + \frac{p_2 q_2}{n_2}\right)$   
 $Z = \frac{(\hat{p}_1 - \hat{p}_2) - (p_1 - p_2)}{\sqrt{\frac{p_1 q_1}{n_1} + \frac{p_2 q_2}{n_2}}} \sim N(0, 1)$ 

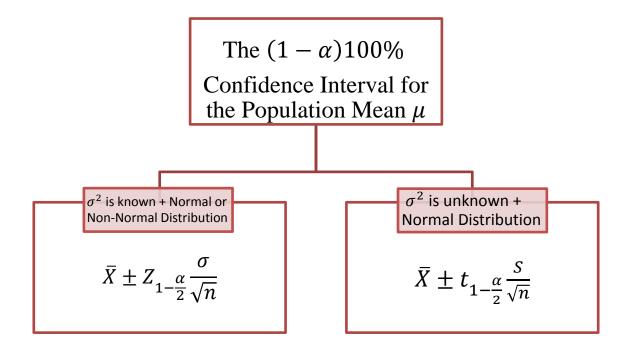
## **Chapter 6:**

# **1.The Point Estimates for the Population Parameters:**

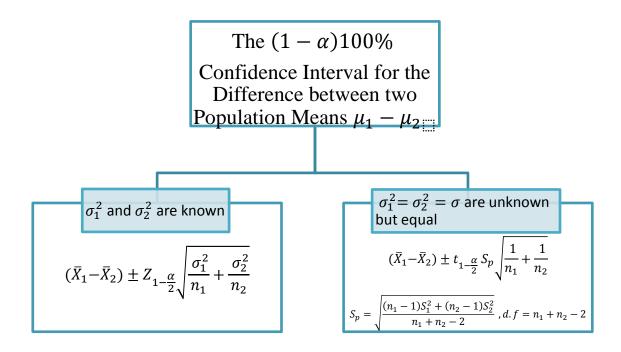
	Population Parameter	Point Estimator
Mean	μ	$\overline{X}$
Variance	$\sigma^2$	<i>S</i> <sup>2</sup>
Standard Deviation	σ	S
Proportion	p	$\hat{p}$
The Difference between two Means	$\mu_1 - \mu_2$	$\bar{X}_1 - \bar{X}_2$
The Difference between two Proportions	$p_1 - p_2$	$\hat{p}_1 - \hat{p}_2$

# **2.The Confidence Intervals for the Population Parameters:**

#### <u>Case 1:</u> The Confidence Interval for the Population Mean $\mu$ :



<u>Case 2:</u> The Confidence Interval for the Difference between two Population Means  $\mu_1 - \mu_{2:}$ 



#### **<u>Case 3:</u>** The Confidence Interval for the Population Proportion *p*:

When  $n \ge 30$ , np > 5, nq > 5 and  $\hat{p} = \frac{x}{n}$ .

Then the  $(1 - \alpha)100\%$  confidence interval for *p* is

$$\hat{p} \pm Z_{1-\frac{\alpha}{2}} \sqrt{\frac{\hat{p}\hat{q}}{n}}$$

## <u>Case 4:</u> The Confidence Interval for the Difference between two Population Proportions $p_1 - p_2$ :

When  $n_1 \ge 30$ ,  $n_2 \ge 30$ ,  $n_1 p_1 > 5$ ,  $n_1 q_1 > 5$ ,  $n_2 p_2 > 5$ ,  $n_2 q_2 > 5$  and  $\hat{p}_1 = \frac{x_1}{n_1}$ ,  $\hat{p}_2 = \frac{x_2}{n_2}$ ,  $\hat{p}_1 - \hat{p}_2 = \frac{x_1}{n_1} - \frac{x_2}{n_2}$ .

Then the  $(1 - \alpha)100\%$  confidence interval for  $p_1 - p_2$  is

$$(\hat{p}_1 - \hat{p}_2) \pm Z_{1-\frac{\alpha}{2}} \sqrt{\frac{\hat{p}_1\hat{q}_1}{n_1} + \frac{\hat{p}_2\hat{q}_2}{n_2}}$$

**The General Formulas:** 

$$Z = \frac{value - mean}{standard\ error}$$

 $estimator \pm (reliability \ cofficient \times standard \ error)$ 

Where

Standard error = standard deviation

Estimator = Point estimate

Reliability coefficient = table value =  $Z_{1-\frac{\alpha}{2}}$  or  $t_{1-\frac{\alpha}{2}}$