

Chapter (7)

Continuous Probability Distributions

Examples

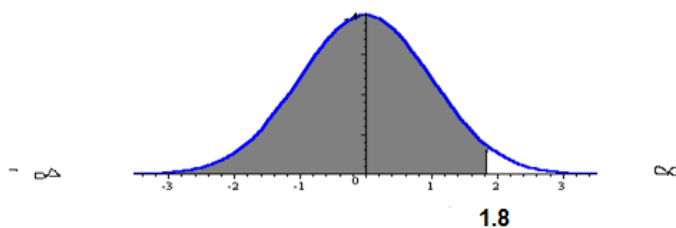
Normal probability distribution

How to find the area under the normal curve?

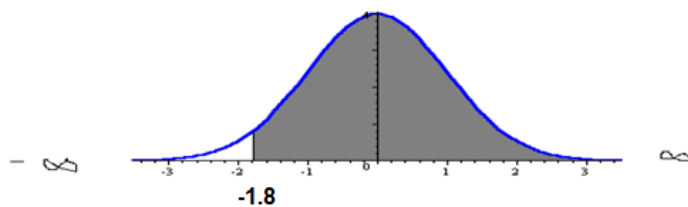
If $\mu = 50$ & $\sigma = 6$

Find

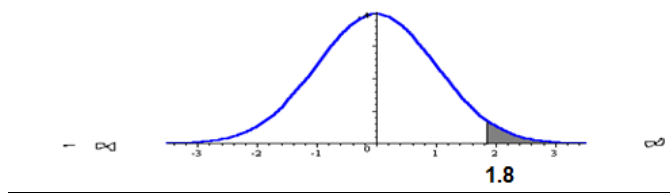
$$\begin{aligned}
 (1) P(X < 60.8) &= P\left(Z < \frac{60.8 - 50}{6}\right) \\
 &= P\left(Z < \frac{10.8}{6}\right) = P(Z < 1.8) = 0.5 + P(0 < Z < 1.8) \\
 &= 0.5 + 0.4641 = 0.9641
 \end{aligned}$$



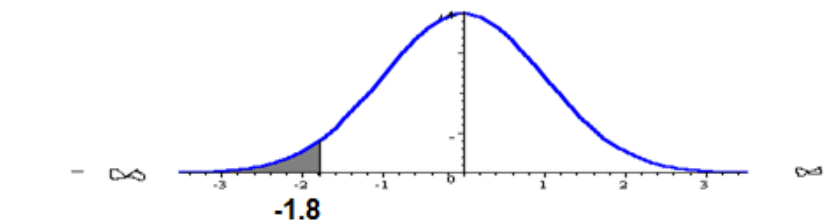
$$\begin{aligned}
 (2) P(X > 39.2) &= P\left(Z > \frac{39.2 - 50}{6}\right) \\
 &= P\left(Z > \frac{-10.8}{6}\right) = P(Z > -1.8) = 0.5 + P(-1.8 < Z < 0) \\
 &= 0.5 + 0.4641 = 0.9641
 \end{aligned}$$



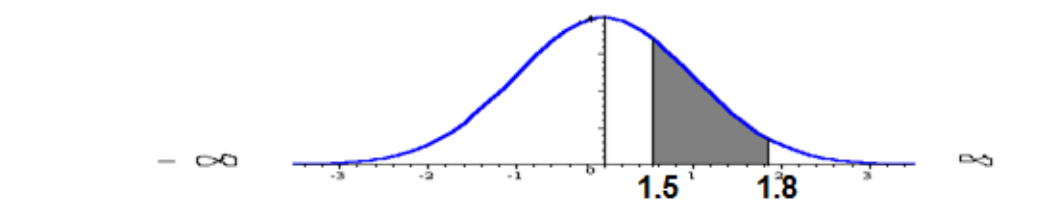
$$\begin{aligned}
 (3) P(X > 60.8) &= P\left(Z > \frac{60.8 - 50}{6}\right) \\
 &= P\left(Z > \frac{10.8}{6}\right) = P(Z > 1.8) = 0.5 - P(0 < Z < 1.8) \\
 &= 0.5 - 0.4641 = 0.0359
 \end{aligned}$$



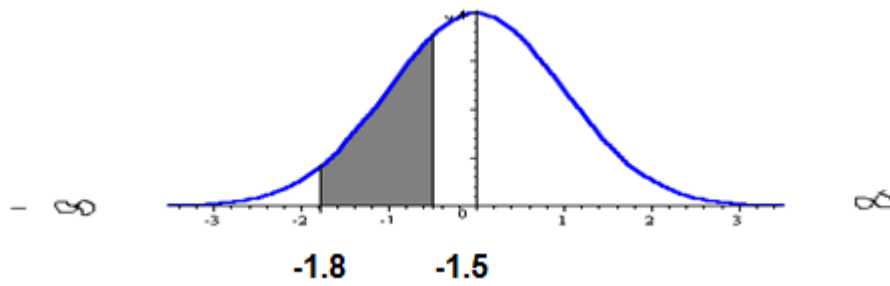
$$\begin{aligned}
 (4) P(X < 39.2) &= P\left(Z < \frac{39.2 - 50}{6}\right) \\
 &= P\left(Z < \frac{-10.8}{6}\right) = P(Z < -1.8) = 0.5 + P(-1.8 < Z < 0) \\
 &= 0.5 - 0.4641 = 0.0359
 \end{aligned}$$



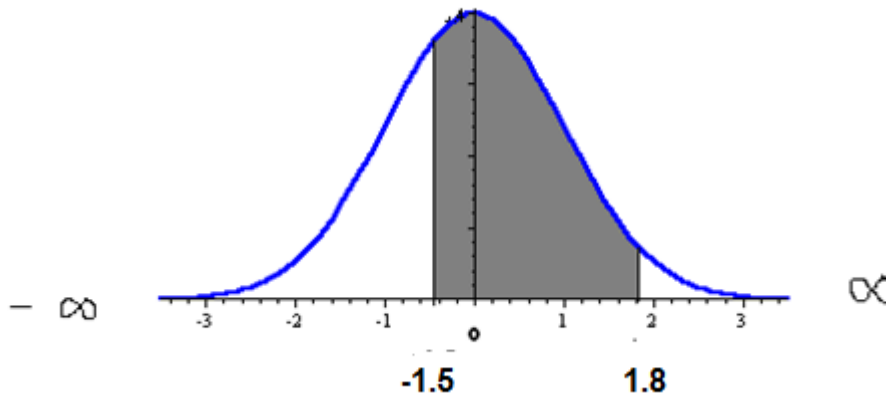
$$\begin{aligned}
 (5) P(59 < X < 60.8) &= P\left(\frac{59 - 50}{6} < Z < \frac{60.8 - 50}{6}\right) \\
 &= P\left(\frac{9}{6} < Z < \frac{10.8}{6}\right) = P(1.5 < Z < 1.8) = P(0 < Z < 1.8) - P(0 < Z < 1.5) \\
 &= 0.4641 - 0.4332 = 0.0309
 \end{aligned}$$



$$\begin{aligned}
 (6) P(39.2 < X < 41) &= P\left(\frac{39.2 - 50}{6} < Z < \frac{41 - 50}{6}\right) \\
 &= P\left(\frac{-10.8}{6} < Z < \frac{-9}{6}\right) = P(-1.8 < Z < -1.5) \\
 &= P(0 < Z < -1.8) - P(0 < Z < -1.5) \\
 &= 0.4641 - 0.4332 = 0.0309
 \end{aligned}$$



$$\begin{aligned}
 (7) P(41 < X < 60.8) &= P\left(\frac{41-50}{6} < Z < \frac{60.8-50}{6}\right) \\
 &= P\left(\frac{-9}{6} < Z < \frac{10.8}{6}\right) = P(-1.5 < Z < 1.8) = P(0 < Z < 1.8) - P(-1.5 < Z < 0) \\
 &= 0.4641 + 0.4332 = 0.8973
 \end{aligned}$$



Z-Table

	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.0000	0.0040	0.0080	0.0120	0.0160	0.0199	0.0239	0.0279	0.0319	0.0359
0.1	0.0398	0.0438	0.0478	0.0517	0.0557	0.0596	0.0636	0.0675	0.0714	0.0753
0.2	0.0793	0.0832	0.0871	0.0910	0.0948	0.0987	0.1026	0.1064	0.1103	0.1141
0.3	0.1179	0.1217	0.1255	0.1293	0.1331	0.1368	0.1406	0.1443	0.1480	0.1517
0.4	0.1554	0.1591	0.1628	0.1664	0.1700	0.1736	0.1772	0.1808	0.1844	0.1879
0.5	0.1915	0.1950	0.1985	0.2019	0.2054	0.2088	0.2123	0.2157	0.2190	0.2224
0.6	0.2257	0.2291	0.2324	0.2357	0.2389	0.2422	0.2454	0.2486	0.2517	0.2549
0.7	0.2580	0.2611	0.2642	0.2673	0.2704	0.2734	0.2764	0.2794	0.2823	0.2852
0.8	0.2881	0.2910	0.2939	0.2967	0.2995	0.3023	0.3051	0.3078	0.3106	0.3133
0.9	0.3159	0.3186	0.3212	0.3238	0.3264	0.3289	0.3315	0.3340	0.3365	0.3389
1.0	0.3413	0.3438	0.3461	0.3485	0.3508	0.3531	0.3554	0.3577	0.3599	0.3621
1.1	0.3643	0.3665	0.3686	0.3708	0.3729	0.3749	0.3770	0.3790	0.3810	0.3830
1.2	0.3849	0.3869	0.3888	0.3907	0.3925	0.3944	0.3962	0.3980	0.3997	0.4015
1.3	0.4032	0.4049	0.4066	0.4082	0.4099	0.4115	0.4131	0.4147	0.4162	0.4177
1.4	0.4192	0.4207	0.4222	0.4236	0.4251	0.4265	0.4279	0.4292	0.4306	0.4319
1.5	0.4332	0.4345	0.4357	0.4370	0.4382	0.4394	0.4406	0.4418	0.4429	0.4441
1.6	0.4452	0.4463	0.4474	0.4484	0.4495	0.4505	0.4515	0.4525	0.4535	0.4545
1.7	0.4554	0.4564	0.4573	0.4582	0.4591	0.4599	0.4608	0.4616	0.4625	0.4633
1.8	0.4641	0.4649	0.4656	0.4664	0.4671	0.4678	0.4686	0.4693	0.4699	0.4706
1.9	0.4713	0.4719	0.4726	0.4732	0.4738	0.4744	0.4750	0.4756	0.4761	0.4767
2.0	0.4772	0.4778	0.4783	0.4788	0.4793	0.4798	0.4803	0.4808	0.4812	0.4817
2.1	0.4821	0.4826	0.4830	0.4834	0.4838	0.4842	0.4846	0.4850	0.4854	0.4857
2.2	0.4861	0.4864	0.4868	0.4871	0.4875	0.4878	0.4881	0.4884	0.4887	0.4890
2.3	0.4893	0.4896	0.4898	0.4901	0.4904	0.4906	0.4909	0.4911	0.4913	0.4916
2.4	0.4918	0.4920	0.4922	0.4925	0.4927	0.4929	0.4931	0.4932	0.4934	0.4936
2.5	0.4938	0.4940	0.4941	0.4943	0.4945	0.4946	0.4948	0.4949	0.4951	0.4952
2.6	0.4953	0.4955	0.4956	0.4957	0.4959	0.4960	0.4961	0.4962	0.4963	0.4964
2.7	0.4965	0.4966	0.4967	0.4968	0.4969	0.4970	0.4971	0.4972	0.4973	0.4974
2.8	0.4974	0.4975	0.4976	0.4977	0.4977	0.4978	0.4979	0.4979	0.4980	0.4981
2.9	0.4981	0.4982	0.4982	0.4983	0.4984	0.4984	0.4985	0.4985	0.4986	0.4986
3.0	0.4987	0.4987	0.4987	0.4988	0.4988	0.4989	0.4989	0.4989	0.4990	0.4990

