

### Chapter 3:

Q1: In article entitled "Bucket-Handle Meniscal Tears of the Knee: Sensitivity and Specificity of MRI signs" Dorsay and Helms (A-6) performed a retrospective study of 72 knees scanned by MRI. One of the indicators they examined was the absence of the "bow tie sign" in the MRI as evidence of a bucket-handle or "bucket-handle type" tear of the meniscus. In the study, surgery confirmed that 43 of the 73 cases were bucket-handle tears. The cases may be cross-classified by "bow tie sign" status and surgical results as follows:

|   | Tears Surgically Confirmed (D) | Tears Surgically confirmed as not Present ( $D^C$ ) | Total |
|---|--------------------------------|---|-------|
| Positive Test (absent bow tie sign (T))         | 38                             | 10  | 48    |
| Negative Test ( bow tie sign Present) ( $T^C$ ) | 5                              | 15  | 23    |
| Total   | 43                             | 28  | 71    |

1. what is false negative?

- (A) Probability that result of the test is positive given that patient has disease.
- (B) Probability** that result of the test is negative given that patient has disease.
- (C) Probability that result of the test is positive given that patient doesn't have disease.
- (D) Probability that result of the test is negative given that patient doesn't have disease.

2. What is false positive?

- (A) Probability that result of the test is positive given that patient has disease.
- (B) Probability that result of the test is negative given that patient has disease.
- (C) Probability that** result of the test is positive given that patient doesn't have disease.
- (D) Probability that result of the test is negative given that patient doesn't have disease.

3. Compute the sensitivity of the symptom?

$$P(T/D) = 38/43 = 0.8837$$

4. Compute the specificity of the symptom?

$$P(T^C/D^C) = 18/28 = 0.6229$$

5. Suppose it is known that the rate of the disease in the general population is 0.1. What is the predictive value positive of the symptom?

$$P(D/T) = \frac{\text{Sens.} \cdot P(D)}{\text{Sens.} \cdot P(D) + (1 - \text{Spec.}) \cdot P(D^C)} = 0.2066$$

6. What is the predictive value negative of the symptom?

$$P(D^C/T^C) = \frac{\text{Spec.} \cdot P(D^C)}{\text{Spec.} \cdot P(D^C) + (1 - \text{Sens.}) \cdot P(D)} = 0.9797$$

#### **Chapter 4:**

Q1: Given the following probability distribution of a discrete random variable X representing the number of defective teeth of the patient visiting a certain dental clinic

1. The value of the k is ...0.05...
2.  $P(x < 3) = 0.6$
3.  $P(X \leq 3) = 0.8$
4.  $P(X < 6) = 1$
5.  $P(X = 3.5) = 0$
6. Probability that the patient has at least 4 defective Teeth .....0.20.....
7. Probability that the patient has at most 2 defective Teeth .....0.6.....
8. The expected number of defective teeth (Mean) = 2.4
9. The variance of X is .....1.34.....

| X | P(X= x) |
|---|---------|
| 1 | 0.25    |
| 2 | 0.35    |
| 3 | 0.20    |
| 4 | 0.15    |
| 5 | K       |

#### **Chapter 5:**

Q1: The same survey data base cited shows that 32 % of U.S. adults indicated that they have tested for HIV at some point in their life. Consider a simple random sample of 15 adults selected at that time. Find the probability that the number of adults who have been tested for HIV in the sample would be:

1. Three .

$$P(X = 3) = 0.14574$$

2. Less than five.

$$\begin{aligned} P(X < 5) &= P(X=0) + P(X=1) + P(X=2) + P(X=3) + P(X=4) \\ &= 0.00307 + 0.0217 + 0.0715 + 0.1457 + 0.2057 = 0.4477 \end{aligned}$$

3. Between five and nine. Inclusive.

$$\begin{aligned} P(5 \leq X \leq 9) &= P(X=5) + P(X=6) + P(X=7) + P(X=8) + P(X=9) \\ &= 0.0174 + 0.0476 + 0.1011 + 0.1671 + 0.2130 = 0.5462 \end{aligned}$$

4. More than five, but less than 10.

$$\begin{aligned} P(5 < X < 10) &= P(X=6) + P(X=7) + P(X=8) + P(X=9) \\ &= 0.0174 + 0.0476 + 0.1011 + 0.1671 = 0.3332 \end{aligned}$$

5. Six or more.

$$\begin{aligned} P(X \geq 6) &= 1 - P(X < 6) \\ &= 1 - [P(X=0) + P(X=1) + P(X=2) + P(X=3) + P(X=4) + P(X=5)] = 1 - 0.6607 = 0.3393 \end{aligned}$$

6. Mean equals ... $\mu = np = 15(0.32) = 4.8$ .....

7. Variance equals ...  $\sigma^2 = npq = 15(0.32)(0.68) = 3.264 \dots$

Q2: Singh et al. (A-7) Looked at the occurrence of retinal capillary hemangioma patients with von Hippel-Lindau (VHL) disease. RCH is a benign vascular tumor of the retina. Using a retrospective consecutive case series review, the researchers found that the number of RCH tumor incidents followed a Poisson distribution with  $\lambda = 4$  tumors per eye for patients with VHL. Using this model.

The probability that in a randomly patient with VHL

1. There will be exactly five occurrences of tumors per eye equals...

$$(\lambda = 4): f(x) = e^{-4} 4^x / x!$$

$$P(X=5) = 0.1563$$

2. There are more than five occurrences of tumors per 2-eyes equals...

$$(\lambda = (4)(2)=8) : f(x) = e^{-8} 8^x / x!$$

$$P(X > 5) = 1 - P(X \leq 5) = 1 - 0.19124 = 0.80876$$

3. There are between five and seven occurrences tumors per eye, inclusive.....

$$(\lambda = 4) : f(x) = e^{-4} 4^x / x!$$

$$P(5 \leq X \leq 7) = 0.320$$

4. The mean (per eye) =  $\lambda = 4$

5. The variance (Per 2-eyes) =  $\lambda = (4)(2) = 8$