

Theorem 2.2.1 page 81:

$$(j) \quad \emptyset - A = \emptyset$$

proof: Suppose on the contrary that $x \in \emptyset - A$, then $x \in \emptyset$, and $x \notin A$
this is a contradiction $\therefore \emptyset - A = \emptyset$ ■

$$(9) \quad \text{If } A \subseteq B, \text{ then } A \cup C \subseteq B \cup C.$$

proof: Suppose $x \in A \cup C$, then $x \in A$ or $x \in C$, since $A \subseteq B$
then $x \in B$ or $x \in C$
so $x \in B \cup C$ ■

Theorem 2.2.2 page 83:

$$(9) \quad (A \cap B)^c = A^c \cup B^c$$

$$x \in (A \cap B)^c \text{ iff } x \notin A \cap B$$

$$\text{iff } x \notin A \text{ or } x \notin B$$

$$\text{iff } x \in A^c \text{ or } x \in B^c$$

$$\text{iff } x \in A^c \cup B^c$$

Theorem 2.2.3 page 85:

$$(f) \quad (A \times B) \cap (B \times A) = (A \cap B) \times (A \cap B)$$

proof:

$$(x, y) \in (A \times B) \cap (B \times A) \text{ iff } (x, y) \in A \times B, \text{ and } (x, y) \in B \times A$$

$$\text{iff } x \in A, y \in B, \text{ and } x \in B, y \in A$$

$$\text{iff } x \in A \cap B, \text{ and } y \in A \cap B$$

$$\text{iff } (x, y) \in (A \cap B) \times (A \cap B)$$