

## MODERN PHYSICS LAB ( HW N<sup>o</sup> 1 )

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To be submitted before 22/02/2018

### PROBLEM (1) DEALING WITH DATA

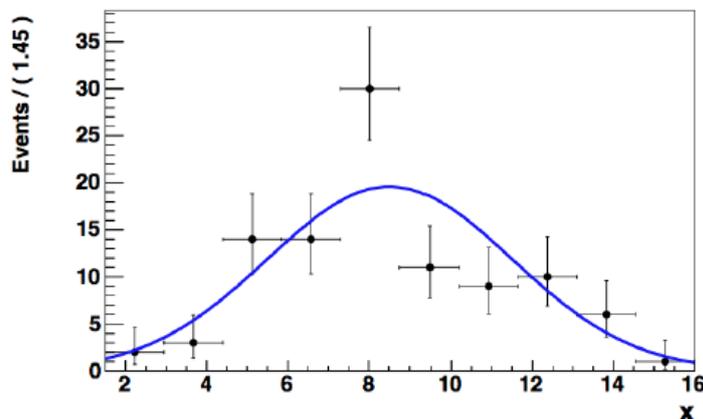
You are given a table of % of students marks in some subject.

ID	Course-work	Final
1	98%	90%
2	83%	65%
3	73,3%	40%
4	86,7%	57,5%
5	95%	95%

1. Add another column cantoning the total, and classify the student who fail or pass the course if the passing mark was 75%.
2. Compute the mean value and standard deviation for each column.
3. Plot the data (course-work and final), using a scatter plot, then fit the data to a line. ( you may draw it manually or by computer program.
4. Study the slop of the line drawn, is the slope positive or negative. Can you conclude that the course-work marks are correlated with the final marks ?

## PROBLEM (2) NORMAL DISTRIBUTION

You have the Gaussian plot (normal distribution) of some data collected from particle collisions at CERN.



1. What is the mean-value of the this distribution?
2. measure the width of this distribution, then find its standard-deviation.
3. Write the mathematical expression for this curve.

## PROBLEM (3) ERROR PROPAGATION FORMULA

If we have a function of several random variables  $f(x_1, x_2, \dots, x_n)$ , and we know the ‘uncertainty’ for each of these variables  $\sigma_{x_i}$  then the uncertainty of the function  $f$  is given by **the error propagation formula**

$$\sigma^2(f(x_1, x_2, \dots)) = \sum_{i=1}^n \frac{\partial^2 f}{\partial x_i^2} \sigma_{x_i}^2 \quad (0.1)$$

The relativistic relation between energy, momentum and mass is given by

$$E^2 = (mc^2)^2 + p^2 c^2 \quad (0.2)$$

We could measure  $p$  and  $E$  using a *calorimeter*, with uncertainties  $\sigma_p$  and  $\sigma_E$ , respectively. What is the uncertainty in the mass  $\sigma_m$  ?

## PROBLEM (4) ABSOLUTE AND RELATIVE ERRORS

We measured the radioactivity of  $Po^{210}$  and  $U^{ore}$  sources, we got the following intensities  $[I] = \text{count} / \text{min}$  Calculate the absolute  $\varepsilon$  and relative  $\eta$  errors.

Source Intensity (count/min)	$I_1$	$I_2$	$I_3$
$Po^{210}$	130	145	140
$U^{ore}$	100	98	99

### PROBLEM 5) THE Z BOSON

**(This is a bonus question)** In 1983, an interesting particle was discovered at CERN, called the Z boson. The discovery was made via colliding electron and anti-electron together at a very high energy. Sometimes, from these collisions the Z boson will be produced, and then quickly decay via the processes shown the diagram. Sometimes the Z boson decays into two

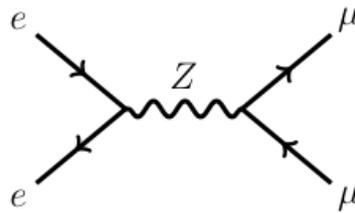


Figure 0.1: The event  $e^+e^- \rightarrow Z \rightarrow \mu^+\mu^-$

(heavier) versions of the electron and anti-electron called the muon particle  $\mu^-$ . Others, it decays into more complicated pattern of particles composed of other particles called Hadrons<sup>1</sup>. The shape of data collected from CERN UA(1) and UA(2) experiments that discovered the Z is given in the following figure .

1. What is the charge of the Z ?
2. Using the figure 0.2, what is the mass if the Z in GeV?
3. Consider the distribution of the Z mass as a Gaussian, what is the width  $\Gamma(Z \rightarrow \text{Hadrons})$  and  $\Gamma(Z \rightarrow \mu\mu)$  . Then calculate the total width. This was a very important measurement that you have reproduced !
4. The width of the Z help us understand the current model of particle physics and know the number of neutrino families, what is the number of neutrino families ?

<sup>1</sup>The proton is a hadron, it is composed of 3 subnuclear particles called quarks, the Z boson would decay into hadrons made from quark and anti-quark

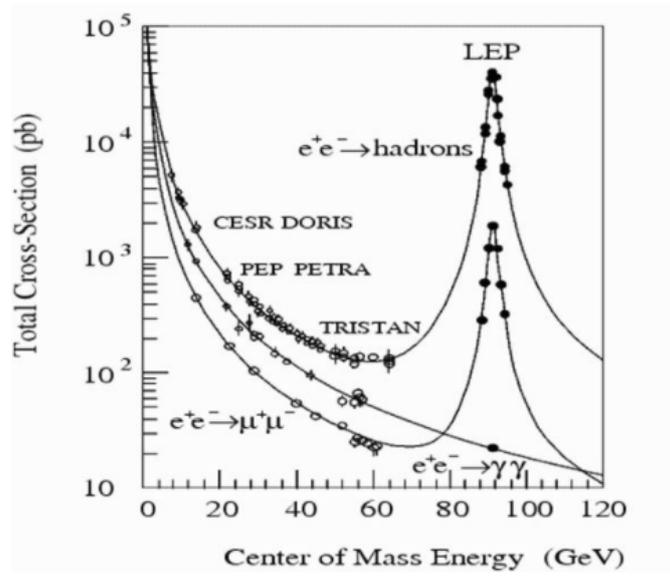


Figure 0.2: UA(1) and UA(2) experiments data showing the  $Z$  boson discovery

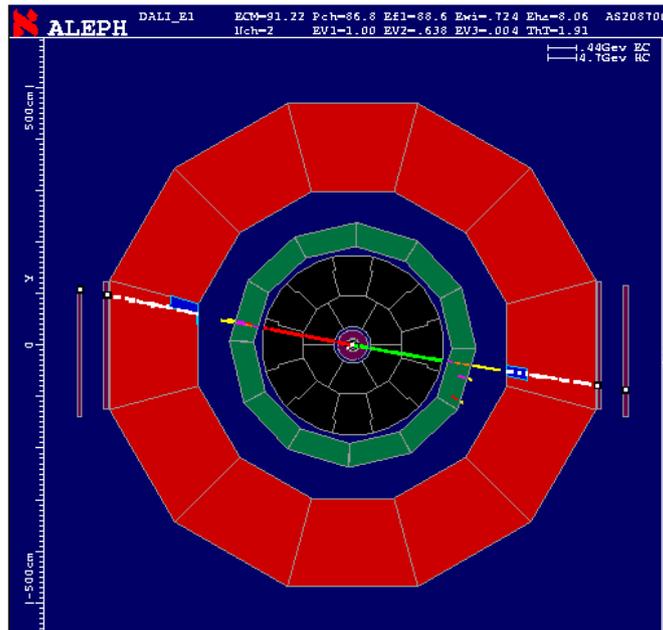


Figure 0.3: An actual  $Z \rightarrow \mu\mu$  event detected at the ALEPH experiment at LEP-CERN