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## $I O\left(X^{2} \Pi\right)-A r$ cluster: ab initio potential energy surface and dynamical computations

S. Marzouk, Y. Ajili, F. Lique, M. Ben El Hadj Rhouma, M. Mogren Al Mogren and M. Hochlaf*
lodine oxide $(\mathrm{IO})$ is an important tropospheric molecule.

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# $I O\left(X^{2} \Pi\right)-A r$ cluster: ab initio potential energy surface and dynamical computations $\dagger$ 

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#### Abstract

lodine oxide $(\mathrm{IO})$ is an important tropospheric molecule. In the present paper, we mapped the potential energy surfaces (PESs) of the doubly degenerate $I O\left(X^{2} \Pi\right)-A r$ van der Waals system using single- and double-excitation coupled cluster approaches with non-iterative perturbation treatment of triple excitations [RCCSD(T)] extrapolated to the complete basis set (CBS) limit. In addition to bent local minima, we identified a linear Ar-IO complex as a global minimum. Afterwards, we performed scattering calculations on these PESs, considering the non-zero spin-orbit contribution and the Renner-Teller effect. The integral cross-sections exhibit an oscillatory structure vs. the final rotational state, as already observed for the $\mathrm{NO}\left(\mathrm{X}^{2} \Pi\right)-A r$ system. Moreover, computations reveal that the Ar -IO complex is stable toward dissociation into IO and Ar. Therefore, it can be found in the atmosphere and participates in iodine compound physical chemical processes occurring there.


budget in the atmosphere via its implication in the photochemistry of tropospheric $\mathrm{HO}_{x}$ and $\mathrm{NO}_{x}$ (production/destruction).

Several details on IO spectroscopy and its gas phase reactivity can be found in ref. 9 and 10 . For instance, the kinetics and mechanisms of reactions involving the IO molecule have been studied in a large number of laboratory studies. ${ }^{11-19}$ Experimental data on the thermochemistry of the IO molecule are also available. ${ }^{20}$ Moreover, the physical properties of the isolated molecule are also available. ${ }^{21-24}$ Its spectroscopy was investigated by a multitude of experimental and theoretical ${ }^{25-29}$ approaches. These include $\mu w,{ }^{21}$ rotational, ${ }^{30}$ laser magnetic resonance, ${ }^{31}$ cavity ring-down, ${ }^{32}$ high-resolution laser-rf, ${ }^{33}$ laser induced fluorescence ${ }^{11,12}$ and absorption and emission spectroscopies ${ }^{34-36}$ as well as spin-orbit configuration interaction calculations. ${ }^{37-39}$ These studies established that the ground state of IO is of ${ }^{2} \Pi$ symmetry species. ${ }^{33}$ It is a Hund's case (a) radical with a negative spin-orbit constant ( $A_{\text {SO }}$ $=-2091 \mathrm{~cm}^{-122}$ ). The electronic orbital angular momentum and the electron spin have well-defined projection onto the internuclear axis of $\Lambda= \pm 1$ and $\Sigma= \pm 1 / 2$, respectively. Therefore, there are two spin-orbit manifolds: the lowest component is the ${ }^{2} \Pi_{3 / 2}$ with $|\Omega|=|\Lambda+\Sigma|=3 / 2$ (labeled $\mathrm{F}_{1}$ ), and the higherenergy is the ${ }^{2} \Pi_{1 / 2}$ with $|\Omega|=1 / 2$ (labeled $\mathrm{F}_{2}$ ). Each rotational $j$ splits into two close lying $\Lambda$-doublet levels labeled e (total parity + as $\left.(-1)^{j-1 / 2}\right)$ and $\mathrm{f}\left(\right.$ total parity - as $\left.(-1)^{j-1 / 2}\right) .{ }^{42}$ The energies of the rotational levels, including the spin-orbit and $\Lambda^{-}$ doubling fine structure, are given by:

$$
\begin{equation*}
E_{j, \Omega=1 / 2, \varepsilon}=1 / 2 A_{\mathrm{SO}}+B_{\mathrm{e}}[j(j+1)+1 / 4]+\frac{\varepsilon}{2} p(j+1 / 2) \tag{1}
\end{equation*}
$$

$$
\begin{align*}
E_{j, \Omega=3 / 2, \varepsilon}= & -1 / 2 A_{\mathrm{SO}}+B_{\mathrm{e}}[j(j+1)-7 / 4]+\frac{\varepsilon B_{\mathrm{e}}}{2 A_{\mathrm{SO}}} \\
& \times\left(2 q+\frac{p B_{\mathrm{e}}}{A_{\mathrm{SO}}}\right)(j-1 / 2)(j+1 / 2)(j+3 / 2) \tag{2}
\end{align*}
$$

where $\varepsilon$ is the parity. $\varepsilon=+1$ and $\varepsilon=-1$ correspond to e-labelled and f-labelled levels respectively. $B_{\mathrm{e}}\left(=0.3388 \mathrm{~cm}^{-133}\right)$ is the rotational constant at equilibrium of IO $\left(\mathrm{X}^{2} \Pi_{3 / 2}\right)$. p $(=0.1094212$ $\left.\mathrm{cm}^{-130}\right)$ and $q\left(=-0.0000166 \mathrm{~cm}^{-130}\right)$ are the two $\Lambda$-doubling parameters (see ref. 30 for more details).

The present contribution deals with the investigation of the IO-Ar van der Waals complex. Ar is the third most abundant gas of the Earth's atmosphere. This complex may be formed in the troposphere/low stratosphere after collision between IO and argon. These collisional processes may participate in the modification of the radiation budget of the atmosphere. The implication in atmospheric processes of other IO-M complexes was noticed. For instance, the formation of the IO-water complex was suspected to be at the origin of the inhibition of the polymerization of IO leading to the atmospheric IO aerosols. ${ }^{41}$ The existence of a stable IO-water complex was confirmed later by $a b$ initio computations. ${ }^{42}$ Also, the implication of the IO-CO van der Waals complex was suggested during the oxidation of IO by CO to form $\mathrm{I}+\mathrm{CO}_{2} \cdot{ }^{43}$ In the other hand, molecules containing iodine are prototype molecular systems for fundamental photophysical studies (see, for instance, the studies by Zewail and co-workers ${ }^{44}$ ). This is also true for the specific case of iodine van der Waals complexes such as those studied by Bogomolov et al. ${ }^{45}$

To date, nothing is available in the literature concerning the IO-Ar molecular species that may help its identification or elucidating its possible role in the physical chemical atmospheric phenomena. At present, we predict a stable $\mathrm{IO}-\mathrm{Ar}$ complex. We derived its dissociation energy, which may help its identification in the laboratory. For that purpose, we generated the 2 D potential energy surfaces (2D PESs) of the $I O\left(X^{2} \Pi\right)-$ Ar interacting system. These PESs are mapped in the Jacobi coordinates (Fig. 1) using the coupled cluster approach extrapolated to the complete basis set (CBS) limit. Afterwards, these PESs are incorporated into full quantum treatment of the nuclear motions. Because of the ${ }^{2} \Pi$ nature of IO, the ground state of the IO-Ar complex is doubly degenerate for linear configurations with non-zero spin-orbit contribution. This results in a Renner-Teller system, ${ }^{46}$ which complicates the dynamics of such colliding systems. Such treatments are


Fig. 1 Definition of the Jacobi coordinates of the IO-Ar complex.
challenging and rare. For instance, we can cite the spectroscopic and dynamical investigations of the $\mathrm{OH} / \mathrm{OD}-\mathrm{Rg}(\mathrm{Rg}=$ $\mathrm{He}, \mathrm{Ne}, \mathrm{Ar}, \mathrm{Kr}, \mathrm{Xe}),{ }^{47-53} \mathrm{PO}-\mathrm{He},{ }^{54} \mathrm{NO}-\mathrm{Rg}(\mathrm{Rg}=\mathrm{He}, \mathrm{Ne}, \mathrm{Ar}),{ }^{55-67}$ $\mathrm{NO}-\mathrm{D}_{2},{ }^{60}$ and $\mathrm{SH} / \mathrm{SD}-\mathrm{Ar}^{68}$ colliding systems.

## II. Generation of the PESs of the IO ( $\mathrm{X}^{2} \Pi$ )-Ar interacting system

## 1. Electronic structure computations

The IO-Ar van der Waals system is described using the Jacobi coordinates as specified in Fig. 1. They correspond to the IO internuclear distance $(r)$, the distance from the center of mass of the IO molecule to the $\operatorname{Ar}$ atom $(R)$ and the angle between R and the IO bond axis $(\theta)$, with $\theta=0^{\circ}$ for the collinear $\mathrm{I}-\mathrm{O}-\mathrm{Ar}$ arrangement. In the present study, the IO diatomic is considered as rigid. The IO bond distance was kept fixed at its experimental equilibrium value $(r=1.872 \AA=3.538$ Bohr $) .{ }^{33}$ All electronic calculations were performed using the MOLPRO 2015 package ${ }^{69}$ in the $C_{\text {s }}$ symmetry point group.

When the $\mathrm{IO}\left(\mathrm{X}^{2} \Pi\right)$ radical interacts with a spherical structure-less target (such as the Ar atom), the doublydegenerate ${ }^{2} \Pi$ electronic state splits into two components: one of ${ }^{2} \mathrm{~A}^{\prime}$ symmetry and one of ${ }^{2} \mathrm{~A}^{\prime \prime}$ symmetry. $A b$ initio calculations of the PESs of $\operatorname{Ar}-\mathrm{IO}\left(\mathrm{X}^{2} \Pi\right)$ van der Waals complex being in the ${ }^{2} \mathrm{~A}^{\prime}$ or the ${ }^{2} \mathrm{~A}^{\prime \prime}$ electronic states were carried out using the partially spin-restricted coupled clusters with the single, double and perturbative triple excitations $(\operatorname{RCCSD}(\mathrm{T}))^{70,71}$ approach as implemented in the MOLPRO 2015 package. ${ }^{69}$ For both components, the electronic structure computations were carried out for $\theta$ angle values from $0^{\circ}$ to $180^{\circ}$ by steps of $10^{\circ}$. The $R$ distances were varied from 6 to 22 Bohr yielding 30 points for each angular orientation. Nevertheless, for $R>14$ Bohr, some irregular behaviors were noticed. Thus, only the points where $R \leq 14$ Bohr were considered during the fitting of the PESs. For $R>14$, the PESs were extrapolated (cf. infra).

For oxygen and argon atoms, we used the aug-cc-pVXZ (X = $\mathrm{D}, \mathrm{T}, \mathrm{Q})$ basis sets of Dunning and co-workers. ${ }^{72,73}$ The iodine was described using the corresponding aug-cc-pVXZ-PP ( $\mathrm{X}=\mathrm{D}$, $\mathrm{T}, \mathrm{Q})$ correlation consistent basis sets together with the appropriate Stuttgart/Koeln ECP28MDF pseudopotential. ${ }^{38}$ Throughout the calculations of the IO-Ar interaction potentials, $V(R, \theta)$, the basis set superposition error (BSSE) was corrected at all geometries using the Boys and Bernardi ${ }^{74}$ counterpoise scheme, as follows

$$
\begin{equation*}
V(R, \theta)=E_{\mathrm{IO}-\mathrm{Ar}}(R, \theta)-E_{\mathrm{IO}}(R, \theta)-E_{\mathrm{Ar}}(R, \theta) \tag{3}
\end{equation*}
$$

where the energies of the IO and Ar monomers are computed in the full basis set of the complex.

Afterwards, the ab initio energies were extrapolated to the Complete Basis Set (CBS) limit, employing the mixed exponential and Gaussian formula of Peterson et al. ${ }^{75}$

$$
\begin{equation*}
E=E_{\mathrm{CBS}}+A \mathrm{e}^{-(X-1)}+B \mathrm{e}^{-(X-1)^{2}} \tag{4}
\end{equation*}
$$ energy extrapolated to the CBS limit. $A$ and $B$ are parameters to adjust. In the following, we will discuss the $\operatorname{RCCSD}(T) /$ CBS PESs.

## 2. Analytic forms of the 2D-PESs

For the representation of the $I O-A r{ }^{2} \mathrm{~A}^{\prime}$ and ${ }^{2} \mathrm{~A}^{\prime \prime}$ 2D-PESs, we derived analytical expressions. We thus adopted the fitting procedure described by Werner et al. ${ }^{76}$ for the $\mathrm{CN}-\mathrm{He}$ complex. Such a procedure leads us to generate the $V(R, \theta)$ numerical expansion routine for each component:

$$
\begin{equation*}
V(R, \theta)=\sum_{l=1}^{L} A_{l}(R) d_{m, 0}^{l+m-1}(\cos \theta) \tag{5}
\end{equation*}
$$

where the $d_{m, 0}^{l+m-1}$ are the reduced rotation matrix elements of Wigner and $L$ represents the total number of the ab initio angles. The $A_{l}(R)$ are given by

$$
\begin{align*}
A_{l}(R)= & \mathrm{e}^{-a_{l}\left(R-R_{l}^{(0)}\right)}\left(\sum_{i=0}^{2} b_{l}^{(i)} R_{i}\right) \\
& -\frac{1}{2}\left(1+\tanh \frac{R-R_{l}^{(1)}}{R_{l}^{\mathrm{Ref}}}\right) \sum_{j=6,8,10} \frac{c_{l}^{(j)}}{R^{j}} \tag{6}
\end{align*}
$$

The analytic potentials were found to reproduce the calculated energies quite well. Over the entire grid, the mean difference between the analytic fit and the ab initio computed interaction energies is less than $2-3 \%$. The major deviations between the fitted potential values and the $a b$ initio points are concentrated in the long-range part of the PESs. The long-range part of the PES was extrapolated assuming a $C_{n} / R^{n}(n=6,8,10)$ multipolar expansion. The $C_{n}$ coefficients were obtained from the $a b$ initio energies computed for distances larger than $R=12$ $a_{0}$. The corresponding expansions are given in the ESI. $\dagger$

In the scattering calculations, it is more convenient to use the average and the difference of the $V_{\mathrm{A}^{\prime}}$ and $V_{\mathrm{A}^{\prime \prime}}$ potential energy surfaces which we define as:

$$
\begin{align*}
& V_{\text {sum }}=1 / 2\left(V_{\mathrm{A}^{\prime \prime}}+V_{\mathrm{A}^{\prime}}\right)  \tag{7}\\
& V_{\mathrm{diff}}=1 / 2\left(V_{\mathrm{A}^{\prime \prime}}-V_{\mathrm{A}^{\prime}}\right) \tag{8}
\end{align*}
$$

These two adiabatic potentials are usually expanded in a series of reduced Wigner functions $d_{\mu}(\cos \theta),{ }^{77}$

$$
\begin{align*}
& V_{\text {sum }}(R, \theta)=\sum_{l=0}^{l_{\max }} V_{l 0}(R) d_{l 0}(\cos \theta)  \tag{9}\\
& V_{\text {diff }}(R, \theta)=\sum_{l=0}^{l_{\max }} V_{l 2}(R) d_{l 2}(\cos \theta) \tag{10}
\end{align*}
$$

where $V_{l 0}(R)$ and $V_{l 2}(R)$ correspond to the radial dependence of the potentials as expressed in ref. 77. $l_{\text {max }}$ was set to 18 .

In the pure Hund's case (a), $V_{\text {sum }}$ is responsible for inducing inelastic collisions within a given spin manifold, and $V_{\text {diff }}$ for inducing inelastic collisions between the ${ }^{2} \Pi_{1 / 2}$ and ${ }^{2} \Pi_{3 / 2}$ spin- orbit manifolds.

## 3. Features of the ${ }^{2} \mathbf{A}^{\prime}$ and ${ }^{2} \mathbf{A}^{\prime \prime}$ 2D-PESs

Fig. 2 shows the 2 D contour plots of the ${ }^{2} \mathrm{~A}^{\prime}$ and ${ }^{2} \mathrm{~A}^{\prime \prime}$ PESs along the $R$ and $\theta$ Jacobi coordinates. Table 1 gives the main characteristics of these PESs including the geometric parameters of the stationary points, their well depths and isomerization barrier heights. Fig. 3 shows the minimum energy paths of the ${ }^{2} \mathrm{~A}^{\prime}\left(V_{\mathrm{A}^{\prime}}\right)$ and ${ }^{2} \mathrm{~A}^{\prime \prime}\left(V_{\mathrm{A}^{\prime \prime}}\right)$ components along the bending angle. For linear configurations, both components are degenerate and then split for bent structures. They form hence a linear-linear Renner-Teller system for $\theta=180^{\circ}$ and a linear-bent RennerTeller system for $\theta=00^{\circ}{ }^{46}$ For both components, the global minimum occurs at a linear configuration, where the Ar is located at the iodine side of IO (i.e. $\theta=180^{\circ}$ ) and for $R=7.31$ Bohr. The associated well depth is $D_{\mathrm{e}}=273.58 \mathrm{~cm}^{-1}$. For the ${ }^{2} \mathrm{~A}^{\prime}$ state, we found a second local minimum for bent structures $(\theta=$ $56^{\circ}, R=7.67 \mathrm{Bohr}$ ) with a well depth of $D_{\mathrm{e}}=197.90 \mathrm{~cm}^{-1}$. This minimum correlates with a transition state for $\theta=0^{\circ}$ and is separated by a transition state with the global minimum located at $\theta=107^{\circ}$ and $R=7.94$ Bohr (Table 1). For the ${ }^{2} \mathrm{~A}^{\prime \prime}$ state, two secondary minima are found: (i) at bent structures i.e. $R=7.46 \mathrm{Bohr}, \theta=63^{\circ}, D_{\mathrm{e}}=217.49 \mathrm{~cm}^{-1}$; and (ii) at a linear $\mathrm{Ar}^{-}$



Table 1 Characteristics of the IO-Ar PESs. We give the well depths ( $D_{\mathrm{e}}$, in $\mathrm{cm}^{-1}$ ), equilibrium distances ( $R$, in Bohr) and angles ( $\theta$ in degrees) and the energies of the transition state ( $E^{\star}$ in $\mathrm{cm}^{-1}$ ) with respect to the IO and Ar separated species

| ${ }^{2} \mathrm{~A}^{\prime \prime}$ component |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Ar}-\mathrm{IO}$ |  |  | Transition state |  |  | Bent IO-Ar |  |  | Transition state |  |  | IO-Ar |  |  |
| $D_{\text {e }}$ | $R$ | $\theta$ | $E^{*}$ | $R$ | $\theta$ | $D_{\text {e }}$ | $R$ | $\theta$ | $E^{*}$ | $R$ | $\theta$ | $D_{\text {e }}$ | $R$ | $\theta$ |
| 273.58 | 7.31 | $180^{\circ}$ | -107.55 | 8.32 | 114 | 217.49 | 7.46 | $63^{\circ}$ | -144.31 | 9.08 | 29 | 157.52 | 9.46 | $0^{\circ}$ |

${ }^{2} \mathrm{~A}^{\prime}$ component

| $\underline{\mathrm{Ar}-\mathrm{IO}}$ |  |  | $\underline{\text { Transition state }}$ |  |  | Bent IO-Ar |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $D_{\text {e }}$ | $R$ | $\theta$ | $E^{*}$ | $R$ | $\theta$ | $D_{\text {e }}$ | $R$ | $\theta$ |
| 273.58 | 7.31 | $180^{\circ}$ | -134.42 | 7.94 | $107^{\circ}$ | 197.90 | 7.67 | $56^{\circ}$ | and $V_{\text {sum }}=-272.8 \mathrm{~cm}^{-1}$; and (ii) for the bent structure, where $\theta$ $=62^{\circ}$ and $R=7.52 \mathrm{~cm}^{-1}$ Bohr and $V_{\text {sum }}=-204.7 \mathrm{~cm}^{-1}$; whereas $\theta=0^{\circ}$ corresponds to a transition state. Fig. 4 shows also that $V_{\text {diff }}$ exhibits small variations along the $R$ and $\theta$ coordinates.



Fig. 3 Minimum energy paths of the ${ }^{2} \mathrm{~A}^{\prime}\left(V_{\mathrm{A}^{\prime}}\right)$ and ${ }^{2} \mathrm{~A}^{\prime \prime}\left(V_{\mathrm{A}^{\prime \prime}}\right)$ components of the IO-Ar PES as a function of the $\theta$ angle.

O-I configuration i.e. $R=9.46, \theta=0^{\circ}, D_{\mathrm{e}}=157.52 \mathrm{~cm}^{-1}$. As for the ${ }^{2} \mathrm{~A}^{\prime}$ component, the transition states connecting these minima are located below the dissociation of the complex ( $c f$. Table 1). As discussed for other weakly bound complexes, complex quantum effects, including quantum tunneling, vibrational memory and quantum localization effects are expected to take place. ${ }^{78,79}$ These effects together with the Renner-Teller coupling complicate the spectroscopy and the dynamics of the IO-Ar colliding system. Note that the features described here for the ${ }^{2} \mathrm{~A}^{\prime \prime}$ PES are similar to those found for other van der Waals complexes such as $\mathrm{ICl}-\mathrm{Ar}^{80}$ and $\mathrm{HI}-\mathrm{Ar}^{81}$

## 4. Features of the $V_{\text {sum }}$ and $V_{\text {diff }}$ 2D-PESs

Fig. 4 presents the 2D contour plots of the $V_{\text {sum }}$ and $V_{\text {diff. }}$ As can be seen there, the average potential $V_{\text {sum }}$ has two minima: (i) for the linear configuration, where $\theta=180^{\circ}$ and $R=7.31 \mathrm{~cm}^{-1} \mathrm{Bohr}$ Thus, inelastic collisions between the ${ }^{2} \Pi_{1 / 2}$ and ${ }^{2} \Pi_{3 / 2}$ spinorbit manifolds are not expected to take place.



Fig. 4 2D contour plots of $V_{\text {sum }}$ (top) and of $V_{\text {diff }}$ (bottom) along the $R$ and $\theta$ coordinates. The blue (red) contours are for positive (negative) energies. Energies are in $\mathrm{cm}^{-1}$.

## III. Dissociation energy of the IO-Ar complex

We carried out fully quantum close coupling calculations of the lowest bound states for total angular momentum $J=0.5$, for the set of IO-Ar PESs determined here. In these calculations, the $V_{\text {sum }}$ and $V_{\text {diff }}$ were incorporated. The open-shell electronic

1 structure of the IO molecule was taken into account. We employed the HIBRIDON suite of codes. ${ }^{82}$

The radial part of the wave functions in the bound-state calculations is expanded in a replicated Gaussian basis dis-

## IV. Integral cross-section calculations for the scattering of IO by collision with Ar

20 In the scattering calculations, we assume that the spin-orbit constant is independent of the IO-Ar intermolecular separaconstant is independent of the IO-Ar intermolecular separa-
tion. The latter approximation is commonly employed in scattering calculations because of the moderate-to-large intermolecular separations at typical atmospheric collision
energies. The quantum scattering calculations of integral intermolecular separations at typical atmospheric collision
energies. The quantum scattering calculations of integral cross-sections for the scattering of IO by collision with Ar were performed using the quantum Coupled States (CS)
approximation. ${ }^{83}$ We also performed some costly close couperformed using the quantum Coupled States (CS)
approximation. ${ }^{83}$ We also performed some costly close coupling (CC) computations for comparison. Both techniques are implemented in the HIBRIDON package. ${ }^{82}$

The numerical accuracy of the integration procedure with respect to the number of partial waves and rotational basis functions and the integration parameters were tested to meet convergence criteria better than 2 percent for the crosssections.

Using eqn (1) and (2), we give in Table 2 the energies of the first fine structure levels of IO. The dynamical calculations were performed on a grid of energies up to a total energy of $E_{\text {tot }}=500$ $\mathrm{cm}^{-1}$. The maximum values of the total angular momentum tributed between $R=5.5$ and 20 Bohr. The IO-Ar reduced mass was 31.22 amu . The channel basis included all rotational levels of IO up to $j_{\text {max }}=18.5$.

The calculated dissociation energy of IO-Ar, $D_{0}$, is $\sim 228$ $\mathrm{cm}^{-1}$. Such a large value is explained by the relatively large well depth of both ${ }^{2} \mathrm{~A}^{\prime}$ and ${ }^{2} \mathrm{~A}^{\prime \prime}$ PESs of the IO-Ar complex. This shows that the IO-Ar complex is expected to be stable under atmospheric conditions where it is also expected to be efficiently formed during collisions between IO and Ar. 44.5, respectively. For a better description of the resonances, the energy steps were spanned as follow: 0.1 for $E_{\text {tot }} \leq 100,0.2$ for $100 \leq E_{\text {tot }} \leq 200$, and 0.5 for $200 \leq E_{\text {tot }} \leq 300$ and $1 \mathrm{~cm}^{-1}$ for $E_{\text {tot }} \geq 300$ (all values are in $\mathrm{cm}^{-1}$ ).

In order to check the accuracy of the CS approximation, a comparison with the exact close coupling (CC) approach has been carried out. Table 3 gives the comparison with the two methods for some transitions where the collision energy, $E_{\text {tot }}$ is equal to $50 \mathrm{~cm}^{-1}$ and $300 \mathrm{~cm}^{-1}$. As expected, the CS crosssections differ significantly from those obtained using exact CC calculations at very low collision energies. This difference however vanishes while increasing the total energy. Indeed, Table 3 shows that the CS approach can lead to inaccuracies of $20-50$ percent at total energy of $50 \mathrm{~cm}^{-1}$, whereas the agreement improves significantly between CC and CS cross sections for $E_{\text {tot }}=300 \mathrm{~cm}^{-1}$. The relative accuracy of the CS

Table 2 Pattern of the rotational levels $(j)$ of $I O\left(X^{2} \Pi\right)$ for $\Omega=1 / 2$ and $3 / 2$. Energies ( $E_{\Omega=3 / 2}$ and $E_{\Omega=1 / 2}$ ) are in $\mathrm{cm}^{-1} . \varepsilon$ is the parity. The reference energy is that of the $E_{\Omega=3 / 2} j=1.5$ level

| $j$ | $\varepsilon$ | $E_{\Omega=3 / 2}$ | $E_{\Omega=1 / 2}$ |
| :---: | :---: | :---: | :---: |
| 0.5 | e |  | 2090.771 |
| 0.5 | f |  | 2090.661 |
| 1.5 | e | 0.000 | 2091.842 |
| 1.5 | f | 0.000 | 2091.623 |
| 2.5 | e | 1.694 | 2093.591 |
| 2.5 | f | 1.694 | 2093.263 |
| 3.5 | e | 4.065 | 2096.018 |
| 3.5 | f | 4.065 | 2095.580 |
| 4.5 | e | 7.113 | 2099.122 |
| 4.5 | f | 7.113 | 2098.575 |
| 5.5 | e | 10.839 | 2102.904 |
| 5.5 | f | 10.839 | 2102.248 |
| 6.5 | e | 15.243 | 2107.364 |
| 6.5 | f | 15.243 | 2106.598 |
| 7.5 | e | 20.324 | 2112.502 |
| 7.5 | f | 20.324 | 2111.626 |
| 8.5 | e | 26.082 | 2118.317 |
| 8.5 | f | 26.082 | 2117.332 |
| 9.5 | e | 32.518 | 2124.810 |
| 9.5 | f | 32.518 | 2123.716 |
| 10.5 | e | 39.631 | 2131.980 |
| 10.5 | f | 39.631 | 2130.777 |
| 11.5 | e | 47.422 | 2139.829 |
| 11.5 | f | 47.422 | 2138.516 |
| 12.5 | e | 55.890 | 2148.355 |
| 12.5 | f | 55.890 | 2146.933 |
| 13.5 | e | 65.036 | 2157.559 |
| 13.5 | f | 65.036 | 2156.027 |
| 14.5 | e | 74.859 | 2167.440 |
| 14.5 | f | 74.859 | 2165.799 |
| 15.5 | e | 85.359 | 2177.999 |
| 15.5 | f | 85.359 | 2176.249 |

Table 3 Comparison between CC and CS IO-Ar cross-sections (in Å) for total energies $E_{\text {tot }}=50 \mathrm{~cm}^{-1}$ and $E_{\text {tot }}=300 \mathrm{~cm}^{-1}$. Transitions were chosen among levels in the $F_{1}$ spin-orbit manifold

| Transition | $E_{\text {tot }}=50 \mathrm{~cm}^{-1}$ |  | $E_{\text {tot }}=300 \mathrm{~cm}^{-1}$ |  |
| :---: | :---: | :---: | :---: | :---: |
|  | CC | CS | CC | CS |
| $1.5 \mathrm{e} \rightarrow 1.5 \mathrm{f}$ | 22.71 | 46.81 | 10.46 | 14.17 |
| $1.5 \mathrm{e} \rightarrow 3.5 \mathrm{e}$ | 7.130 | 4.808 | 2.786 | 3.136 |
| $1.5 \mathrm{e} \rightarrow 3.5 \mathrm{f}$ | 7.136 | 7.865 | 3.333 | 3.880 |
| $1.5 \mathrm{e} \rightarrow 4.5 \mathrm{e}$ | 5.386 | 4.830 | 2.170 | 2.187 |
| $1.5 \mathrm{e} \rightarrow 4.5 \mathrm{f}$ | 4.920 | 3.787 | 1.311 | 1.529 |
| $1.5 \mathrm{e} \rightarrow 5.5 \mathrm{e}$ | 4.644 | 3.323 | 0.978 | 0.936 |
| $1.5 \mathrm{e} \rightarrow 5.5 \mathrm{f}$ | 4.289 | 3.305 | 1.373 | 1.315 |
| $2.5 \mathrm{e} \rightarrow 6.5 \mathrm{e}$ | 6.623 | 6.191 | 1.297 | 1.137 |
| $2.5 \mathrm{e} \rightarrow 6.5 \mathrm{f}$ | 5.685 | 4.867 | 1.479 | 1.554 |
| $3.5 \mathrm{e} \rightarrow 8.5 \mathrm{e}$ | 4.849 | 7.023 | 1.579 | 1.389 |
| $4.5 \mathrm{e} \rightarrow 6.5 \mathrm{e}$ | 9.774 | 9.213 | 4.319 | 3.865 |
| $7.5 \mathrm{e} \rightarrow 10.5 \mathrm{e}$ | 15.64 | 12.39 | 3.549 | 4.123 |
| $10.5 \mathrm{e} \rightarrow 11.5 \mathrm{e}$ | 30.23 | 28.80 | 10.16 | 9.762 |
| $10.5 \mathrm{e} \rightarrow 15.5 \mathrm{e}$ | - ${ }^{a}$ | - ${ }^{a}$ | 2.435 | 2.610 |

${ }^{a}$ Energetically inaccessible transition.
approximation compared to the full CC approach can be explained by the relatively small energy spacing between IO rotational levels (Table 2).

As mentioned above, the IO molecule can be described in the Hund's case (a) with a large spin-orbit splitting (of 2091


Fig. 5 Variation of the cross-sections vs. the collision energy for transitions out of the ( $j=1.5, \mathrm{e}, \mathrm{F}_{1}$ ) fine structure level to the $\left(j^{\prime}, \mathrm{e} / \mathrm{f}, \mathrm{F}_{1}\right)$ spinorbit level manifold.
$\mathrm{cm}^{-1}$ ) between $\Omega=3 / 2$ and $\Omega=1 / 2$ states. As expected, no spinorbit changing transitions occur during the collisions between the $\Omega=3 / 2$ and $\Omega=1 / 2$ manifolds, which are induced by $V_{\text {diff }}$. Whereas $V_{\text {sum }}$ potential, which is responsible for the collisional excitation within a given spin-orbit manifold, shows large variations (Fig. 4).

Fig. 5 displays the integral cross-sections of IO induced by collision with Ar as a function of the collision energy for transitions out of the rotational level $\left(j=1.5\right.$, e) of the $\mathrm{F}_{1}$ spin-orbit manifold to some selected rotational levels ( $j^{\prime}$, e/f) within the $F_{1}$ manifold. As may be seen, regardless of the transition considered, the cross-sections show a dense resonance structure at low energies $\left(E<200 \mathrm{~cm}^{-1}\right)$. They correspond to both shape resonances and Feshbach resonances resulting from the decay of bound and quasi-bound states supported by the IO-Ar weakly bound wells in the ${ }^{2} \mathrm{~A}^{\prime}$ and ${ }^{2} \mathrm{~A}^{\prime \prime}$ potentials. It is clear also that the cross-sections for spin-orbit conserving transitions present a strong propensity in favor of the parity conserving e $\rightarrow \mathrm{e}$ and with $\Delta j=1$.


Fig. 6 Variation of the cross sections for the $e \rightarrow e, f \rightarrow f, e \rightarrow f$ and $f \rightarrow e$ transitions vs. the $j$ quantum number.

As explained by Dagdigian et al., ${ }^{84}$ the values of the integral cross sections for $e \rightarrow e$ and $e \rightarrow f$ collisions should be identical to those of $f \rightarrow f$ and $f \rightarrow e$, respectively ${ }^{84}$ in the limit case of a pure Hund's case (a). This is the case here. Indeed, these e/f conserving and changing cross-sections are illustrated in Fig. 6, which shows the integral cross sections obtained for $\mathrm{IO}\left(\mathrm{X}^{2} \Pi\right)$ colliding with Ar at $E_{\text {tot }}=500 \mathrm{~cm}^{-1}$ for spin-orbit conserving collisions, resolved into initial and final $\Lambda$-doublet levels. Fig. 6 shows also that the integral cross sections exhibit an oscillatory structure as a function of the final rotational state. This predicted alternation in the case of IO-Ar for the spin-orbit conserving transition was already noticed for the NO-Ar scattering system. ${ }^{85}$

## V. Conclusions

We mapped the 2D PESs of the $\mathrm{IO}\left(\mathrm{X}^{2} \Pi\right)$-Ar colliding system along the $R$ and $\theta$ Jacobi coordinates. These PESs are incorporated later to treat the nuclear motions using quantum formalism. Computations show that the IO-Ar complex possesses a relatively large dissociation energy and thus it can be formed in the atmosphere. We also deduced the cross-sections of the excitation of IO colliding with Ar. Our calculations reveal that the integral cross sections present an oscillatory structure along the final rotational state. Such behavior was already noticed for the $\mathrm{NO}\left(\mathrm{X}^{2} \Pi\right)$-Ar colliding system, for which several experimental and theoretical studies were devoted.

As said in the introduction, IO is playing an important role in the atmosphere. The present work should motivate new experimental investigations in the laboratory to characterize the IO ( $\mathrm{X}^{2} \Pi$ )-Ar van der Waals system. Also, it should help in identifying this complex in the atmosphere and to understand the physical chemical processes involving IO there and more generally the iodine compounds.

## Conflicts of interest

There are no conflicts to declare.

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