

L(1) + 5 pages
in (R)

Arithmetic Operators

| Operator | Description |
|---------------|--|
| + | addition |
| - | subtraction |
| * | multiplication |
| / | division |
| ^ or ** | exponentiation |
| % or %% | modulus (x mod y) 5%%2 is 1 |
| x %/% y | integer division 5%/%2 is 2 |
| Pi | π |
| factorial(x) | $x!$ |
| | Applied Statistical Computing and Graphics |

addition

subtraction

multiplication

division

exponentiation

modulus (x mod y) 5%%2 is 1

integer division 5%/%2 is 2

π

Applied Statistical Computing and Graphics

factorial(x) $x!$

gamma(x) $\Gamma(x)$

$\left\lceil \frac{5}{2} \right\rceil$

Logical Operators

| Operator | Description |
|-----------|--------------------------|
| < | less than |
| <= | less than or equal to |
| > | greater than |
| >= | greater than or equal to |
| == | exactly equal to |
| != | not equal to |
| !x | Not x |
| x y | x OR y |
| x & y | x AND y |
| isTRUE(x) | test if x is TRUE |

Numeric Functions

| Function | Description |
|---|---|
| $\text{abs}(x)$ | absolute value |
| $\text{sqrt}(x)$ | square root |
| $\text{ceiling}(x)$ | $\text{ceiling}(3.475)$ is 4 |
| $\text{floor}(x)$ | $\text{floor}(3.475)$ is 3 |
| $\text{trunc}(x)$ | $\text{trunc}(5.99)$ is 5 |
| $\text{round}(x, \text{digits}=n)$ | $\text{round}(3.475, \text{digits}=2)$ is 3.48 |
| $\text{signif}(x, \text{digits}=n)$ | $\text{signif}(3.475, \text{digits}=2)$ is 3.5 |
| $\text{cos}(x), \text{sin}(x), \text{tan}(x)$ | also $\text{acos}(x), \text{cosh}(x), \text{acosh}(x)$, etc. |
| $\log(x) = \ln(x)$ | natural logarithm |
| $\log_{10}(x)$ | common logarithm |
| $\exp(x)$ | $e^x = e^x$ |
| $\log(x, \text{base})$ | $\log x$ to any base... |

(p.d.f) $f(x)$ \leftrightarrow **dnorm(x)**

(CDF) $F(x)$ \leftrightarrow **pnorm(q)**

normal inverse \leftrightarrow **qnorm(p)**

random sample
from normal distⁿ \leftrightarrow **rnorm(n, m=0, sd=1)**

\checkmark **dbinom(x, size, prob)**
 \checkmark **pbinom(q, size, prob)**
 \checkmark **qbinom(p, size, prob)**
 \checkmark **rbinom(n, size, prob)**

\checkmark **dpois(x, lambda)**
 \checkmark **ppois(q, lambda)**
 \checkmark **qpois(p, lambda)**
 \checkmark **rpois(n, lambda)**

\checkmark **dunif(x, min=0, max=1)**
 \checkmark **punif(q, min=0, max=1)**
 \checkmark **qunif(p, min=0, max=1)**
 \checkmark **runif(n, min=0, max=1)**

Description

normal density function (by default m=0 sd=1)
 # plot standard normal curve
 x <- pretty(c(-3,3), 30)

y <- dnorm(x)
 plot(x, y, type='l', xlab="Normal Deviate", ylab="Density", yaxp="1")

cumulative normal probability for q ^{left}
 (area under the normal curve to the ^{right} of q)
 pnorm(1.96) is 0.975

normal quantile.
 value at the p percentile of normal distribution
 qnorm(.9) is 1.28 # 90th percentile

n random deviates with mean(m) and standard deviation (sd)
 #50 random normal variates with mean=50, sd=10
 x <- rnorm(50, m=50, sd=10)

binomial distribution where size is the sample size
 and prob is the probability of a heads (pi)
 # prob of 0 to 5 heads of fair coin out of 10 flips
 dbinom(0:5, 10, .5)
 # prob of 5 or less heads of fair coin out of 10 flips
 pbinom(5, 10, .5)

poisson distribution with m=sd=lambda
 #probability of 0, 1, or 2 events with lambda=4
 dpois(0:2, 4)
 # probability of at least 3 events with lambda=4
 1 - ppois(2, 4)

uniform distribution, follows the same pattern
 as the normal distribution above.
 #10 uniform random variates
 x <- runif(10)

Function

**mean(x, trim=0,
na.rm=FALSE)**

sd(x)

median(x)

quantile(x, probs)

range(x)

sum(x)

diff(x, lag=1)

min(x)

max(x)

scale(x,

center=TRUE,

scale=TRUE)

Description

mean of object x

trimmed mean, removing any missing values and

5 percent of highest and lowest scores

`mx <- mean(x, trim=.05, na.rm=TRUE)`

standard deviation of object(x). also look at `var(x)` for variance and `mad(x)` for median absolute deviation.

median

quantiles where x is the numeric vector whose quantiles are desired and probs is a numeric vector with probabilities in [0,1].

30th and 84th percentiles of x

`y <- quantile(x, c(.3,.84))`

range

sum

lagged differences, with lag indicating which lag to use

minimum

maximum

column center or standardize a matrix.

Other Useful Functions

| Function | Description |
|--|--|
| seq(<i>from</i> , <i>to</i>, <i>by</i>) | generate a sequence indices <- seq(1,10,2) #indices is c(1, 3, 5, 7, 9) |
| rep(<i>x</i>, <i>ntimes</i>) | repeat <i>x</i> <i>n</i> times <i>y</i> <- rep(1:3, 2) # <i>y</i> is c(1, 2, 3, 1, 2, 3) |
| cut(<i>x</i>, <i>n</i>) | divide continuous variable in factor with <i>n</i> levels <i>y</i> <- cut(<i>x</i> , 5) |

> # 1) Mathematics as given in the power point ← 4

```
> x=2
> y=9
> z=x*y
> z
[1] 18
> print(z)
[1] 18
> K=c(1,2,5,3,10)
```

```
> K
[1] 1 2 5 3 10
```

```
> # print used for printing one variable
> # cat is used for printing more than one variable
> cat(x,y,z,K)
2 9 18 1 2 5 3 10>
> cat(x,y,z,K,"\n")
2 9 18 1 2 5 3 10
```

```
> # descriptive statistics
```

```
> #mean(x)
> # var(x)
> # sd(x)
> # median(x)
> #range(x)
> # Summary(x) gives minimum Q1 median mean Q3 max
> # coefficient of variation CV= sd(x)/mean(x)
```

```
> summary(x)
  Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
     2       2       2       2       2       2
```

```
> cv=sd(K)/mean(K)
> print(cv)
[1] 0.8485014
```

> # الاسهم تعطينا الاوامر السابقة او التالية
 > # نكتب بها الاوامر ثم نحدد R Editor تظهر لنا نافذة ---New script--- لفتح نافذة جديدة
 > # الاوامر حسابها ونضغط Ctrl+R
 > # وتم الحصول على النتائج R console نجدها تم نقلها لنافذة

```
> x=2
> y=3
> z=x*y
> print(z)
[1] 6
```

> # 3) Loop هو استخدام الاقواس { } وبينهما الامر المطلوب تكراره

```
>
> for(i in 1:10)
+ {
+   print(i)
+ }
[1] 1
[1] 2
[1] 3
[1] 4
[1] 5
[1] 6
[1] 7
[1] 8
[1] 9
[1] 10
```

> # file----save as لحفظ الملف نقف بالمؤشر داخل الصفحة ومن

> # file----open script لفتح ملف قديم

```
> for(i in 0:10)
+ {
+   cat(i,i^2,i*3)
+ }
0 0 01 1 32 4 63 9 94 16 125 25 156 36 187 49 218 64 249 81 2710 100 30> for(i in 0:10)
+ {
+   cat(i,i^2,i*3)
```

```

+ cat(i,i^2,i*3,"\n")
+ }
0 0 0 0
1 1 1 3
2 4 2 6
3 9 3 9
4 16 4 12
5 25 5 15
6 36 6 18
7 49 7 21
8 64 8 24
9 81 9 27
10 100 10 30

```

```

> for(i in 0:10)
+ {
+ cat(i,i^2,i*3,"\n")
+ }

```

```

0 0 0
1 1 3
2 4 6
3 9 9
4 16 12
5 25 15
6 36 18
7 49 21
8 64 24
9 81 27
10 100 30

```

```

> # "\n" معناها ضع النتائج بنفس السطر
> for(i in 0:10)

```

```

+ {
+ x1=i+2
+ x2=sqrt(i)
+ x3=i^3+2*i
+ cat(i," ",x1," ",x2," ",x3,"\n")
+ }

```

```

0 2 0 0
1 3 1 3
2 4 1.414214 12
3 5 1.732051 33
4 6 2 72
5 7 2.236068 135
6 8 2.44949 228
7 9 2.645751 357
8 10 2.828427 528
9 11 3 747
10 12 3.162278 1020

```

```

> # " " لوضع مسافة بين الاعمدة لتكون متباعدة
>

```

```

> # Distributions
>

```

```

> ## dnorm-----calculate normal f(x)
> ## pnorm-----normal F(x) CDF
> ## qnorm-----normal inverse (find the value of x)
> ## rnorm-----normal random sample
>

```

```

> ## Examples
>

```

```

> # if X has N(2,9). find f(x=1.5), F(0.75), p(x> 1.5)
> # f(1.5)=dnorm(1.5,2,sqrt(9))

```

```

> dnorm(1.5,2,sqrt(9))
[1] 0.1311466

```

```

> # F(0.75)=pnorm(0.75,2,3)
> pnorm(0.75,2,3)
[1] 0.3384611

```

```

> ## p(x>1.5)=1-pnorm(1.5,2,3)
> 1-pnorm(1.5,2,3)
[1] 0.5661838

```

```

> ## if x has standard normal N(0,1), we need not to put the values 0, 1 in the command as follows:

```



```
> ## let x has N(0,1) , find p(x<2) and find a if p(x<a)=0.975
> # P(x<2)=pnorm(2) and a= qnorm(0.975)
```

```
> pnorm(2)
[1] 0.9772499
```

```
> qnorm(0.975)
[1] 1.959964
```

```
> ### find random sample from normal (1,4)has size 10
```

```
> rnorm(10,1,2)
```

```
[1] -1.0219220 -2.2359595 -0.9670488 1.7617904 2.6505148 0.2426578 -0.8236448 2.3430551
4.9988127 -0.2156232
```

```
> rnorm(10)
```

```
[1] -1.3424810 -1.1931046 -0.4511279 -3.6477612 0.0843024 -0.9119739 1.3767376 -0.7590830
1.4619257 0.0967894
```

```
> ##### to construct standard normal table, we have to use loop
```

```
> for(z in 0:34)
```

```
+ {
```

```
+ Z=z/10
```

```
+ pz=pnorm(z)
```

```
+ cat(Z," ",pz,"\n")
```

```
+ }
```

```
0 0.5
```

```
0.1 0.8413447
```

```
0.2 0.9772499
```

```
0.3 0.9986501
```

```
0.4 0.9999683
```

```
0.5 0.9999997
```

```
0.6 1
```

```
0.7 1
```

```
0.8 1
```

```
0.9 1
```

```
1 1
```

```
1.1 1
```

```
1.2 1
```

```
1.3 1
```

```
1.4 1
```

```
1.5 1
```

```
1.6 1
```

```
1.7 1
```

```
1.8 1
```

```
1.9 1
```

```
2 1
```

```
2.1 1
```

```
2.2 1
```

```
2.3 1
```

```
2.4 1
```

```
2.5 1
```

```
2.6 1
```

```
2.7 1
```

```
2.8 1
```

```
2.9 1
```

```
3 1
```

```
3.1 1
```

```
3.2 1
```

```
3.3 1
```

```
3.4 1
```

```
> options(digits=4)
```

```
>
```

```
> for(z in 0:34)
```

```
+ {
```

```
+ Z=z/10
```

```
+ pz=pnorm(Z)
```

```
+ cat(Z," ",pz,"\n")
```

```
+ }
```

```
0 0.5
```

```
0.1 0.5398
```

```
0.2 0.5793
```

```
0.3 0.6179
```

نظر القيمة Z

نظر القيمة Z

```

0.4 0.6554
0.5 0.6915
0.6 0.7257
0.7 0.758
0.8 0.7881
0.9 0.8159
1 0.8413
1.1 0.8643
1.2 0.8849
1.3 0.9032
1.4 0.9192
1.5 0.9332
1.6 0.9452
1.7 0.9554
1.8 0.9641
1.9 0.9713
2 0.9772
2.1 0.9821
2.2 0.9861
2.3 0.9893
2.4 0.9918
2.5 0.9938
2.6 0.9953
2.7 0.9965
2.8 0.9974
2.9 0.9981
3 0.9987
3.1 0.999
3.2 0.9993
3.3 0.9995
3.4 0.9997

```

```

> for(z in 0:34)
+ {
+ Z=z/10
+ p=pnorm(Z)
+ p1=pnorm(Z+0.01)
+ p2=pnorm(Z+0.02)
+ p3=pnorm(Z+0.03)
+ cat(Z," ",p," ",p1," ",p2," ",p3,"\n")
+ }
0 0.5 0.504 0.508 0.512
0.1 0.5398 0.5438 0.5478 0.5517
0.2 0.5793 0.5832 0.5871 0.591
0.3 0.6179 0.6217 0.6255 0.6293
0.4 0.6554 0.6591 0.6628 0.6664
0.5 0.6915 0.695 0.6985 0.7019
0.6 0.7257 0.7291 0.7324 0.7357
0.7 0.758 0.7611 0.7642 0.7673
0.8 0.7881 0.791 0.7939 0.7967
0.9 0.8159 0.8186 0.8212 0.8238
1 0.8413 0.8438 0.8461 0.8485
1.1 0.8643 0.8665 0.8686 0.8708
1.2 0.8849 0.8869 0.8888 0.8907
1.3 0.9032 0.9049 0.9066 0.9082
1.4 0.9192 0.9207 0.9222 0.9236
1.5 0.9332 0.9345 0.9357 0.937
1.6 0.9452 0.9463 0.9474 0.9484
1.7 0.9554 0.9564 0.9573 0.9582
1.8 0.9641 0.9649 0.9656 0.9664
1.9 0.9713 0.9719 0.9726 0.9732
2 0.9772 0.9778 0.9783 0.9788
2.1 0.9821 0.9826 0.983 0.9834
2.2 0.9861 0.9864 0.9868 0.9871
2.3 0.9893 0.9896 0.9898 0.9901
2.4 0.9918 0.992 0.9922 0.9925
2.5 0.9938 0.994 0.9941 0.9943
2.6 0.9953 0.9955 0.9956 0.9957
2.7 0.9965 0.9966 0.9967 0.9968
2.8 0.9974 0.9975 0.9976 0.9977
2.9 0.9981 0.9982 0.9982 0.9983
3 0.9987 0.9987 0.9987 0.9988
3.1 0.999 0.9991 0.9991 0.9991
3.2 0.9993 0.9993 0.9994 0.9994

```

```
3.3 0.9995 0.9995 0.9995 0.9996
3.4 0.9997 0.9997 0.9997 0.9997
```

```
>
> ### another method (code 2)
```

أفضل الطرق البديلة

```
> i=seq(0,3.49,by=0.01)
> p=pnorm(i)
> m=matrix(p,ncol=10,byrow=TRUE)
> rownames(m)=seq(0,3.4,by=0.1)
> colnames(m)=seq(0,0.09,by=0.01)
> options(digits=4)
```

الصفوف
الأعمدة

```
> m
      0      0.01      0.02      0.03      0.04      0.05      0.06      0.07      0.08      0.09
0      0.5000 0.5040 0.5080 0.5120 0.5160 0.5199 0.5239 0.5279 0.5319 0.5359
0.1    0.5398 0.5438 0.5478 0.5517 0.5557 0.5596 0.5636 0.5675 0.5714 0.5753
0.2    0.5793 0.5832 0.5871 0.5910 0.5948 0.5987 0.6026 0.6064 0.6103 0.6141
0.3    0.6179 0.6217 0.6255 0.6293 0.6331 0.6368 0.6406 0.6443 0.6480 0.6517
0.4    0.6554 0.6591 0.6628 0.6664 0.6700 0.6736 0.6772 0.6808 0.6844 0.6879
0.5    0.6915 0.6950 0.6985 0.7019 0.7054 0.7088 0.7123 0.7157 0.7190 0.7224
0.6    0.7257 0.7291 0.7324 0.7357 0.7389 0.7422 0.7454 0.7486 0.7517 0.7549
0.7    0.7580 0.7611 0.7642 0.7673 0.7704 0.7734 0.7764 0.7794 0.7823 0.7852
0.8    0.7881 0.7910 0.7939 0.7967 0.7995 0.8023 0.8051 0.8078 0.8106 0.8133
0.9    0.8159 0.8186 0.8212 0.8238 0.8264 0.8289 0.8315 0.8340 0.8365 0.8389
1      0.8413 0.8438 0.8461 0.8485 0.8508 0.8531 0.8554 0.8577 0.8599 0.8621
1.1    0.8643 0.8665 0.8686 0.8708 0.8729 0.8749 0.8770 0.8790 0.8810 0.8830
1.2    0.8849 0.8869 0.8888 0.8907 0.8925 0.8944 0.8962 0.8980 0.8997 0.9015
1.3    0.9032 0.9049 0.9066 0.9082 0.9099 0.9115 0.9131 0.9147 0.9162 0.9177
1.4    0.9192 0.9207 0.9222 0.9236 0.9251 0.9265 0.9279 0.9292 0.9306 0.9319
1.5    0.9332 0.9345 0.9357 0.9370 0.9382 0.9394 0.9406 0.9418 0.9429 0.9441
1.6    0.9452 0.9463 0.9474 0.9484 0.9495 0.9505 0.9515 0.9525 0.9535 0.9545
1.7    0.9554 0.9564 0.9573 0.9582 0.9591 0.9599 0.9608 0.9616 0.9625 0.9633
1.8    0.9641 0.9649 0.9656 0.9664 0.9671 0.9678 0.9686 0.9693 0.9699 0.9706
1.9    0.9713 0.9719 0.9726 0.9732 0.9738 0.9744 0.9750 0.9756 0.9761 0.9767
2      0.9772 0.9778 0.9783 0.9788 0.9793 0.9798 0.9803 0.9808 0.9812 0.9817
2.1    0.9821 0.9826 0.9830 0.9834 0.9838 0.9842 0.9846 0.9850 0.9854 0.9857
2.2    0.9861 0.9864 0.9868 0.9871 0.9875 0.9878 0.9881 0.9884 0.9887 0.9890
2.3    0.9893 0.9896 0.9898 0.9901 0.9904 0.9906 0.9909 0.9911 0.9913 0.9916
2.4    0.9918 0.9920 0.9922 0.9925 0.9927 0.9929 0.9931 0.9932 0.9934 0.9936
2.5    0.9938 0.9940 0.9941 0.9943 0.9945 0.9946 0.9948 0.9949 0.9951 0.9952
2.6    0.9953 0.9955 0.9956 0.9957 0.9959 0.9960 0.9961 0.9962 0.9963 0.9964
2.7    0.9965 0.9966 0.9967 0.9968 0.9969 0.9970 0.9971 0.9972 0.9973 0.9974
2.8    0.9974 0.9975 0.9976 0.9977 0.9977 0.9977 0.9978 0.9979 0.9979 0.9980
2.9    0.9981 0.9982 0.9982 0.9983 0.9984 0.9984 0.9985 0.9985 0.9986 0.9986
3      0.9987 0.9987 0.9987 0.9988 0.9988 0.9989 0.9989 0.9989 0.9990 0.9990
3.1    0.9990 0.9991 0.9991 0.9991 0.9992 0.9992 0.9992 0.9992 0.9993 0.9993
3.2    0.9993 0.9993 0.9994 0.9994 0.9994 0.9994 0.9994 0.9995 0.9995 0.9995
3.3    0.9995 0.9995 0.9995 0.9996 0.9996 0.9996 0.9996 0.9996 0.9996 0.9997
3.4    0.9997 0.9997 0.9997 0.9997 0.9997 0.9997 0.9997 0.9997 0.9997 0.9998
```