

Example 5.4.1

$$\bar{x}_1 = 92, \bar{x}_2 = 105, \sigma_{\bar{x}_1} = 20, \sigma_{\bar{x}_2} = 20, n_1 = 15, n_2 = 15$$

$$\bar{x}_1 - \bar{x}_2 \sim N\left(0, \frac{2(20)^2}{15}\right) \equiv N(0, 53.333).$$

$$\begin{aligned} P(\bar{x}_1 - \bar{x}_2 > 13) &= P\left(z > \frac{13}{7.30297}\right) = P(z > 1.78) \\ &= P(z < -1.78) = 0.0375 \end{aligned}$$

Example 5.4.2

$$\mu_1 = 45, \mu_2 = 30, \sigma_{\bar{x}_1} = 15, \sigma_{\bar{x}_2} = 20, n_1 = 35, n_2 = 40$$

$$\bar{x}_1 - \bar{x}_2 \cong N\left(45-30, \frac{(15)^2}{35} + \frac{(20)^2}{40}\right) \equiv N(15, 16.4286).$$

$$\begin{aligned} P(\bar{x}_1 - \bar{x}_2 > 20) &= P\left(z > \frac{20-15}{4.05322}\right) = P(z > 1.23359) \\ &= P(z < -1.23) = 0.1093 \end{aligned}$$

5.4.1 :

$$\bar{x}_1 = 183, \bar{x}_2 = 189, \sigma_{\bar{x}_1} = 37.2, \sigma_{\bar{x}_2} = 34.7, n_1 = n_2 = 50$$

$$\bar{x}_1 - \bar{x}_2 \cong N\left(189 - 183, \frac{(37.2)^2 + (34.7)^2}{50}\right) \equiv N(6, 51.7586).$$

$$\begin{aligned} P(\bar{x}_1 - \bar{x}_2 > 8) &= P\left(z > \frac{8-6}{7.19435}\right) = P(z > 0.277996) \\ &= P(z < -0.28) = 0.389739 \end{aligned}$$

5.4.2 :

$$\bar{x}_1 = 797, \bar{x}_2 = 660, \sigma_{\bar{x}_1} = 482, \sigma_{\bar{x}_2} = 414, n_1 = 40, n_2 = 35$$

$$\bar{x}_1 - \bar{x}_2 \cong N\left(797-660, \frac{(482)^2}{40} + \frac{(414)^2}{35}\right) \equiv N(137, 10705.1).$$

$$\begin{aligned} P(\bar{x}_1 - \bar{x}_2 > 100) &= P\left(z > \frac{100-137}{103.466}\right) = P(z > -0.357605) \\ &= P(z > -0.36) = P(z < -0.36) = 0.6406 \end{aligned}$$

5.4.3 :

$$\mu_1 = \mu_2, \quad \sigma_1^2 = 100, \quad \sigma_2^2 = 80, \quad n_1 = 25, \quad n_2 = 16.$$

$$\bar{x}_1 - \bar{x}_2 \sim N(0, 4 + 5) \equiv N(0, 9)$$

$$P(\bar{x}_1 - \bar{x}_2 > 8) = P(z > \frac{8}{3}) = P(z > 2.67) = P(z < -2.67) = 0.0037926$$

5.4.4 :

$$\mu_1 = \mu_2, \quad \sigma_1^2 = 240, \quad \sigma_2^2 = 350, \quad n_1 = 40, \quad n_2 = 35.$$

$$\bar{x}_1 - \bar{x}_2 \sim N(0, 6 + 10) \equiv N(0, 16)$$

$$P(\bar{x}_1 - \bar{x}_2 > 12) = P(z > \frac{12}{4}) = P(z > 3) = P(z < -3) = 0.0013499$$

Example 5.5.1

$$p = \frac{X}{N}, \quad \hat{p} = \frac{x}{n}.$$

$$\hat{p} \cong N(p, \frac{pq}{n}), \quad \hat{p} \cong N(0.31, \frac{(0.31)(0.69)}{150}), \quad \hat{p} \cong N(0.31, 0.001426)$$

$$P(\hat{p} > 0.4) = P(z > \frac{0.09}{0.0377624}) = P(z > 2.38332)$$

$$P(z > 2.38) = P(z < -2.38) = 0.0086563$$

Example 5.5.2

$$\hat{p} \cong N(p, \frac{pq}{n}), \quad \hat{p} \cong N(0.51, \frac{(0.51)(0.49)}{200}), \quad \hat{p} \cong N(0.51, 0.0012495)$$

$$P(\hat{p} < 0.45) = P(z < \frac{-0.06}{0.0353483}) = P(z < -1.6974)$$

$$P(z < -1.7) = 0.0445655$$

5.5.1

$P = 0.3$, $n = 50$,

$$P(\hat{p} > 0.4) = P\left(z > \frac{(0.4-0.3)\sqrt{50}}{\sqrt{(0.3)(0.7)}}\right) = P(z > 1.54) = P(z < -1.54) = 0.0617802$$

Or, using c.f. = $P(z > 1.39) = P(z < -1.39) = 0.0822644$

5.5.2

$P = 0.13$, $n = 70$,

$$P(\hat{p} < 0.1) = P\left(z > \frac{(0.1-0.13)\sqrt{70}}{\sqrt{(0.13)(0.87)}}\right) = P(z < -0.75) = 0.226627$$

$$\hat{P}_1 - \hat{P}_2 \sim N\left(P_1 - P_2, \sqrt{\frac{P_1 Q_1}{n_1} + \frac{P_2 Q_2}{n_2}}\right)$$

Example 5.6.1

$P_1 = 0.28$, $P_2 = 0.21$, $n_1 = n_2 = 100$

$$P(\hat{P}_1 - \hat{P}_2 > 0.1) = P\left(z > \frac{0.1 - (0.28 - 0.21)}{\sqrt{\frac{0.28 \cdot 0.72}{100} + \frac{0.21 \cdot 0.79}{100}}}\right) = P\left(z > \frac{.03}{.003675}\right) = P(z >$$

$$0.49) = P(z < -0.49) = 0.3121$$