

**Design and Analysis of Algorithms (CSC311) – Spring 2017**

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**Tutorial 6 (Analysis of Recursive Algorithms)**

Thu. Apr. 13th, 2017

1. Solve the following recurrence relations.

- (a)  $\begin{cases} T(n) = T(n-1) + 5 & \text{for } n > 1 \\ T(1) = 0 \end{cases}$
- (b)  $\begin{cases} T(n) = 3T(n-1) + 5 & \text{for } n > 1 \\ T(1) = 4 \end{cases}$
- (c)  $\begin{cases} T(n) = T(n-1) + n & \text{for } n > 0 \\ T(0) = 0 \end{cases}$
- (d)  $\begin{cases} T(n) = T(n/3) + 1 & \text{for } n > 1 \\ T(1) = 1 \end{cases}$

2. Consider the following recursive algorithm.

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**Algorithm 1**  $Q(n)$

▷ Input: A positive integer  $n$

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1: if  $n = 1$  then
2:   return 1
3: else
4:   return  $Q(n-1) + 2 * n - 1$ 
5: end if
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- (a) Set up a recurrence relation for this functions values and solve it to determine what this algorithm computes.
- (b) Set up a recurrence relation for the number of multiplications made by this algorithm and solve it.
- (c) Set up a recurrence relation for the number of additions/subtractions made by this algorithm and solve it.
3. (a) Design a recursive algorithm for computing  $2^n$  for any nonnegative integer  $n$  that is based on the formula:  $2^n = 2^{n-1} + 2^{n-1}$ .

- (b) Set up a recurrence relation for the number of additions made by the algorithm and solve it.
- (c) Draw a tree of recursive calls for this algorithm and count the number of calls made by the algorithm.
- (d) Is it a good algorithm for solving this problem?