

- **Step Response:-**

if the input to system is a unit step  $u(t)$ , the output is called step response.  $s[n] = u[n] * h[n]$

Its relationship with  $h(t)$ ;  $h(t) = \frac{ds(t)}{dt}$  ||  $h[n] = s[n] - s[n-1]$

Sometimes it's easier to measure the step response then calculate the impulse response.

- **Causal LTI systems described by differential & difference equations:-**

Differential equations such as  $[dy(t)/dt + 2y(t) = x(t)]$  are solved traditionally by dividing the complete solution to a sum of particular and homogeneous solution;  $y(t) = y_p(t) + y_h(t)$ . However, later we'll solve them using Laplace transform.

If a difference equation is given, we could insert an impulse as an input and find a form for the impulse response. (we'll consider causal systems; their initially at rest).

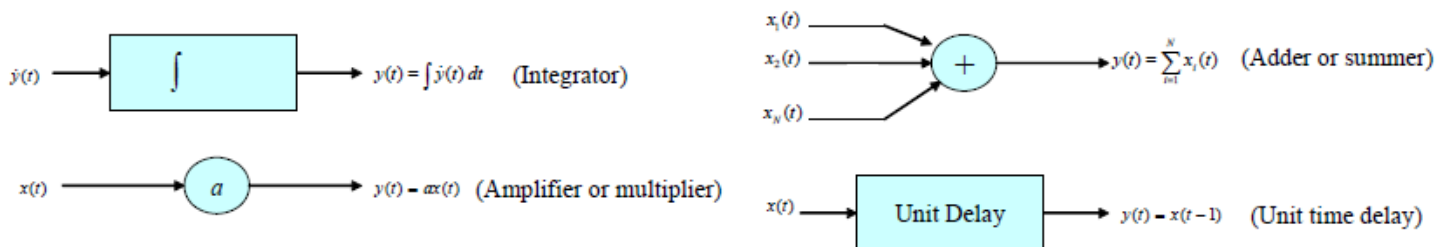
Note:- If we have  $\sum_{k=0}^N a_k y(n-K) = \sum_{k=0}^M b_k x(n-k)$  ;

If  $N \geq 1$ ;  $h[n]$  is called infinite impulse response system (IIR)

If  $N = 0$ ;  $h[n]$  is called finite impulse response system (FIR)

- **Block Diagrams:-**

It could be used to represent systems or circuits.



Q1] The step response of an LTI system is given. Calculate the impulse response.

a)  $s(t) = 1 + e^{-0.5t} u(t)$

b)  $s(n) = 0.5^n u[n]$

Q2] The impulse response of an LTI system is given. Calculate the step response.

a)  $h(t) = e^{3t} u(t)$

b)  $h[n] = \delta[n] - 0.5 \delta[n - 1]$

Q3] Given the difference equation;  $y(n) = 2x(n) + (1/3) y(n-1)$

Find the impulse response, state whether it's FIR or IIR, and find the response if the input is  $2\delta[n - 1]$ .

Q4] Draw a block diagram for the following LTI systems

a)  $y[n] - (1/3) y[n-1] = 0.5 x[n]$

b)  $y(t) = -0.5 dy(t)/dt + 4x(t)$