
OR 441: Simulation and Modeling
Tutorial Handout #6 : Spreadsheet Simulation

Question 1:

Question 2:

Write a one line spreadsheet formula to generate Bernoulli random variables with success probability, 0.35

=IF(RAND()<0.35,1,0)

Question 3:

Write a one line spreadsheet formula to generate random variables from a Normal distribution with mean 10.0 and variance 4.0

=NORM.INV(RAND(),10,2)

Question 4:

Write a one line spreadsheet formula to generate random variables from an exponential distribution with a rate parameter of 5 per hour.

=-1*(1/5)*LN(1-RAND())

Question 5:

The service times for an automated storage and retrieval system has a shifted exponential distribution. It is known that it takes a minimum of 15 seconds for any retrieval. The parameter of the exponential distribution is $\lambda = 45$. Setup a spreadsheet that will generate 20 observations of the service times.

=15 + (-1*(1/45)*LN(1-RAND()))

Question 6:

The time to failure for a computer printer fan has a Weibull distribution with shape parameter $\alpha = 2$ and scale parameter $\beta = 3$. Setup a spreadsheet that will generate 10 failure times for the computer printer fan.

=3*(-1*LN(1-RAND()))^(1/2)

| | A | B | C | |
|---|-----------|------------------------------|------------------------------|--|
| 1 | alpha | 2 | | |
| 2 | beta | 3 | | |
| 3 | | 1 | 2 | |
| 4 | U | =RAND() | =RAND() | |
| 5 | Finv(U) = | =B\$2*(-1*LN(1-B4))^(1/B\$1) | =B\$2*(-1*LN(1-C4))^(1/B\$1) | |

Question 7:

The time to failure for a computer printer fan has a Weibull distribution with shape parameter $\alpha = 2$ and scale parameter $\beta = 3$. Testing has indicated that the distribution is limited to the range from 1.5 to 4.5.

Set up a spreadsheet to generate 100 observations from this truncated distribution.

| | | | | | | | | | | | | | | | | | | | | | | | |
|-----|-------------------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------------------------------|--|--|--|--|--|--|--|--|--|--|--|
| B10 | | | | | | | | | | | | = \$B\$2*(-1*LN(1-B9))^(1/\$B\$1) | | | | | | | | | | | |
| | A | B | C | D | E | F | G | H | I | J | K | | | | | | | | | | | | |
| 1 | alpha | 2 | | | | | | | | | | | | | | | | | | | | | |
| 2 | beta | 3 | | | | | | | | | | | | | | | | | | | | | |
| 3 | | a | b | | | | | | | | | | | | | | | | | | | | |
| 4 | x | 1.5 | 4.5 | | | | | | | | | | | | | | | | | | | | |
| 5 | F(x) | 0.2211992 | 0.8946008 | | | | | | | | | | | | | | | | | | | | |
| 6 | U1 = | 0.9881067 | 0.0850069 | 0.3482762 | 0.7370312 | 0.7492657 | 0.7358131 | 0.6653051 | 0.4506082 | 0.3754529 | 0.1921705 | | | | | | | | | | | | |
| 7 | U2 = | 0.7825538 | 0.5704779 | 0.3188728 | 0.0462038 | 0.0221733 | 0.4938492 | 0.9744858 | 0.3775647 | 0.7109281 | 0.768194 | | | | | | | | | | | | |
| 8 | | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | | | | | | | | | | | | |
| 9 | U ~ U(F(a), F(b)) | 0.8865918 | 0.278443 | 0.4557289 | 0.7175171 | 0.7257559 | 0.7166969 | 0.6692167 | 0.5246395 | 0.4740298 | 0.3506071 | | | | | | | | | | | | |
| 10 | Finv(U) = | 4.4261555 | 1.7137954 | 2.3398228 | 3.373016 | 3.4122765 | 3.3691454 | 3.1554122 | 2.5871097 | 2.4047031 | 1.9711561 | | | | | | | | | | | | |

| | A | B | C |
|----|-------------------|----------------------------------|----------------------------------|
| 1 | alpha | 2 | |
| 2 | beta | 3 | |
| 3 | | a | b |
| 4 | x | 1.5 | 4.5 |
| 5 | F(x) | =1-EXP(-1*(B4/\$B\$2)^\$B\$1) | =1-EXP(-1*(C4/\$B\$2)^\$B\$1) |
| 6 | U1 = | =RAND() | =RAND() |
| 7 | U2 = | =RAND() | =RAND() |
| 8 | | 1 | 2 |
| 9 | U ~ U(F(a), F(b)) | =\$B\$5+(\$C\$5-\$B\$5)*B6 | =\$B\$5+(\$C\$5-\$B\$5)*C6 |
| 10 | Finv(U) = | =\$B\$2*(-1*LN(1-B9))^(1/\$B\$1) | =\$B\$2*(-1*LN(1-C9))^(1/\$B\$1) |
| 11 | | | |

Question 8:

The interest rate for a capital project is unknown. An accountant has estimated that the minimum interest rate will be between 2% and 5% within the next year. The accountant believes that any interest rate in this range is equally likely. You are tasked with generating interest rates for a cash flow analysis of the project. Setup a spreadsheet that will generate 5 interest rate values for the capital project analysis.

| | A | B | C | D |
|---|-----------|----------------------|----------------------|----------------------|
| 1 | a= | 0.02 | | |
| 2 | b = | 0.05 | | |
| 3 | U = | =RAND() | =RAND() | =RAND() |
| 4 | Finv(U) = | =B\$1+(B\$2-B\$1)*B3 | =B\$1+(B\$2-B\$1)*C3 | =B\$1+(B\$2-B\$1)*D3 |
| 5 | | | | |

Question 9:

Setup a spreadsheet to generate 30 observations from the following probability density function:

$$f(x) = \begin{cases} \frac{3x^2}{2} & -1 \leq x \leq 1 \\ 0 & \text{otherwise} \end{cases}$$

| | A | B | C |
|----|----|---------|------------------|
| 1 | | U | Finv(U) |
| 2 | 1 | =RAND() | =(2*B2-1)^(1/3) |
| 3 | 2 | =RAND() | =(2*B3-1)^(1/3) |
| 4 | 3 | =RAND() | =(2*B4-1)^(1/3) |
| 5 | 4 | =RAND() | =(2*B5-1)^(1/3) |
| 6 | 5 | =RAND() | =(2*B6-1)^(1/3) |
| 7 | 6 | =RAND() | =(2*B7-1)^(1/3) |
| 8 | 7 | =RAND() | =(2*B8-1)^(1/3) |
| 9 | 8 | =RAND() | =(2*B9-1)^(1/3) |
| 10 | 9 | =RAND() | =(2*B10-1)^(1/3) |
| 11 | 10 | =RAND() | =(2*B11-1)^(1/3) |
| 12 | 11 | =RAND() | =(2*B12-1)^(1/3) |
| 13 | 12 | =RAND() | =(2*B13-1)^(1/3) |
| 14 | 13 | =RAND() | =(2*B14-1)^(1/3) |
| 15 | 14 | =RAND() | =(2*B15-1)^(1/3) |
| 16 | 15 | =RAND() | =(2*B16-1)^(1/3) |
| 17 | 16 | =RAND() | =(2*B17-1)^(1/3) |
| 18 | 17 | =RAND() | =(2*B18-1)^(1/3) |
| 19 | 18 | =RAND() | =(2*B19-1)^(1/3) |
| 20 | 19 | =RAND() | =(2*B20-1)^(1/3) |
| 21 | 20 | =RAND() | =(2*B21-1)^(1/3) |
| 22 | 21 | =RAND() | =(2*B22-1)^(1/3) |
| 23 | 22 | =RAND() | =(2*B23-1)^(1/3) |
| 24 | 23 | =RAND() | =(2*B24-1)^(1/3) |
| 25 | 24 | =RAND() | =(2*B25-1)^(1/3) |
| 26 | 25 | =RAND() | =(2*B26-1)^(1/3) |
| 27 | 26 | =RAND() | =(2*B27-1)^(1/3) |
| 28 | 27 | =RAND() | =(2*B28-1)^(1/3) |
| 29 | 28 | =RAND() | =(2*B29-1)^(1/3) |
| 30 | 29 | =RAND() | =(2*B30-1)^(1/3) |
| 31 | 30 | =RAND() | =(2*B31-1)^(1/3) |