

**Department of Computer Science,  
Data Structures (CSC212),  
Tutorial 13  
Hashing**

**Question 1.**

Use the hash function  $H(\text{key}) = \text{key} \bmod 11$  to store the sequence of integers: 82, 31, 28, 4, 45, 27, 59, 79, 35 in the hash table of  $\text{TableSize} = 11$ . (a) Use linear rehashing (b) Use external chaining (c) Use coalesced chaining with a cellular size of four and the hash function  $H(\text{key}) = \text{key} \bmod 7$ .

For each of the collision resolution strategies determine (after the values have been inserted into the table) the following:

- 1) The average number of probes needed to find a value that is in the table
- 2) The average number of probes needed to find a value that is not in the table.

**Question 2.**

Assuming the keys are integers, denoted by  $d_n d_{n-1} \dots d_k \dots d_2 d_1$  where  $d_i$  is the  $i$ -th decimal digit in the key,  $d_n$  being the leftmost decimal digit. The hash function  $H(\text{key})$  is given by:

$$H(\text{key}) = (d_1 d_2 + d_{n-1} d_n + d_k) \bmod 11$$

where  $d_1 d_2$  is a two digit number (composed by swapping the rightmost two digits),  $d_{n-1} d_n$  is also a two digit number (composed by swapping the leftmost two digits), and  $k = \lceil n/2 \rceil$

. For example:

$$H(70934) = (43 + 07 + 9) \bmod 11 = 59 \bmod 11 = 4.$$

Assume the keys are: 1234, 519, 911, 7346, 0, 999, 99834, 54 and 40015.

- (a) Compute  $H(\text{key})$  for each of the above keys.
- (b) Insert the above keys (in exactly the same order) in a hash table with open addressing (linear rehashing).
- (c) Find the number of probes required to search for keys 54 and 11 in the above hash table.
- (d) Repeat part (b) using an external chaining hash table.

**Question 3.**

Develop a hashing function to convert a character key of 15 characters into integers in the range of 0 to 999.