

King Saud University  
Faculty of Sciences  
Department of Mathematics

First Examination    Math 106    Semester I    1441-1442  
Time: 2H

1. Use Simpson's rule with  $n = 6$  to approximate the integral  $\int_0^{2\pi} \sin^4(x) dx$ .
2. Compute the integral  $\int \frac{\ln(x) + 1}{1 + (x \ln x)^2} dx$ .
3. Evaluate the integral  $\int \frac{x + \sin^{-1} x}{\sqrt{1 - x^2}} dx$ .
4. Compute the integral  $\int \frac{x^2}{\sqrt{1 + x^6}} dx$ .
5. Evaluate the integral  $\int \frac{dx}{\sqrt{4 - e^x}} dx$ .
6. Compute the integral  $\int \sin^5 x \cos^2 x dx$ .
7. Find the limit  $\lim_{x \rightarrow +\infty} \left(1 + \frac{7}{x}\right)^{5x}$ .
8. Evaluate the integral  $\int x^2 \log_3 x dx$ .
9. Compute  $\int \frac{x^2}{\sqrt{3 - x^2}} dx$ .
10. Compute  $\frac{dy}{dx}$  if  $y = (\cos x)^x$ .
11. Evaluate  $\int \frac{7x + 10}{(x + 1)(x^2 - 4)} dx$ .