

Math106 Midterm2

Question 1(2+3+3)

- a) Find $\lim_{x \rightarrow 0} (1 + 8x^2)^{\frac{1}{x^2}}$
- b) Compute the integral $\int e^{4x} \sin x dx$
- c) Evaluate $\int (\sin x)^2 (\cos x)^2 dx$

Question 2(3+3+2)

- a) Evaluate the integral $\int \frac{\sqrt{x^2-25}}{x} dx$
- b) Find $\int \frac{3x^2+7x+2}{(x+1)^2(x+3)} dx$
- c) Compute $\int \frac{dx}{\sqrt{x(x+1)+1}}$

Question 3(3+3+3)

- a) Find $\int \frac{dx}{x^{1/2}+x^{1/3}}$
- b) Does the integral $\int_0^{\infty} \frac{x dx}{1+x^4}$ converge? Find its value if it does.
- c) Compute the area of the region bounded by the curves: $y = x^2$, $y = x - 1$
 $y = 0$, and $y = 4$.