PHYSICS 507 - SPRING 2020
$1^{\text {st }}$ HOMEWORK
Dr. V. Lempesis

## Hand in: Sunday $9^{\text {th }}$ of February at 23:59

1. The electric field of a distance $z$ above the center of a circular loop as shown in the figure, which carries a uniform line charge $\lambda$, is given by: $\mathbf{E}=\frac{1}{4 \pi \varepsilon_{0}} \frac{q z}{\left(r^{2}+z^{2}\right)^{3 / 2}} \hat{\mathbf{k}}$


What is the value of the field at a distance $z$ such that $z \ll r$.? Give a qualitative explanation of the result. (2 marks)
2. (a) Find the value of the electric flux through the surface of a sphere containing 12 protons and 10 electrons. $|e|=1.6 \times 10^{-19} \mathrm{C}, \varepsilon_{11}=8.85 \times 10^{-22} \mathrm{~F} / \mathrm{m}$.
(b) Does the size of the sphere matter in the answer of question (a)?
3. Two infinite parallel planes carry equal but opposite uniform charge densities $\pm \sigma$. Find the field in each of three regions: (i) to the left of both, (ii) between them, (iii) to the right of both. (5 marks)
4. An infinitely long wire carries positive charge with uniform linear charge density $\lambda$. As the figure shows there is an interruption of the wire of total length $2 L$. Find the total electric field at point A at a distance $z$ from the center of the interrupted region (5 marks).

5. Find the charge density $\rho$ if the electric field in the region is given by the relation

$$
\mathbf{E}=\frac{a z}{r} \hat{r}+b r \hat{\phi}+c r^{2} z^{2} \hat{k}
$$

where $a, b, c$ are known positive constants and the vectors shown are the unit vectors in spherical coordinates. ( 5 marks)

