

TIME: 90 min

KING SAUD UNIVERSITY

FULL MARKS:

40

M - 107

DEPARTMENT OF MATHEMATICS

II MID TERM EXAM (SEM II) 1421-1422

NOTE: Attempt all Questions.

21/4/2002

Question: 1 . (i) Find the distance of $(0,0,0)$ from the line $\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}$. [4]

(ii) Find the equation of the plane determined by lines :

$$\frac{x-2}{2} = \frac{y-3}{3} = \frac{z-4}{4} \quad \text{and} \quad x = y = z. \quad [6]$$

Question: 2 . (i) Let $A(1, -1, 2)$, $B(2, -3, 1)$, and $C(-1, 5, -2)$ be the points in a plane, find the area of triangle ABC. [4]

(ii) If the planes $ax + 2y + z = 4$ and $2x - y - az = 1$ are perpendicular to each other, find a and also find equation of the line of intersection. [6]

Question: 3 . (i) Check whether lines $x = 1 + 2t$, $y = 2 - t$, $z = 3t$ and $\frac{x-2}{3} = \frac{1-y}{1} = \frac{z+5}{1}$ intersect, if they intersect find the point of intersection. [6]

(ii) Identify the surface $4 - x^2 + 2y^2 - z^2 = 0$. Find its traces on the coordinate planes and then sketch the surface. [3]

Question: 4 . (i) Let a curve C be given by $r(t) = t \cos t i + t \sin t j + t k$

(a) Find a unit tangent vector to C at $t = \frac{\pi}{2}$,

(b) Find the equation of the tangent line to C at point $\left(0, \frac{\pi}{2}, \frac{\pi}{2}\right)$ [5]

(a) Let $r(t) = t i + t^2 j + t^3 k$ be the position vector of moving point P , determine tangential and normal components of acceleration and curvature at the point $(1, 1, 1)$. [6]