

# Thermal & Statistical Physics

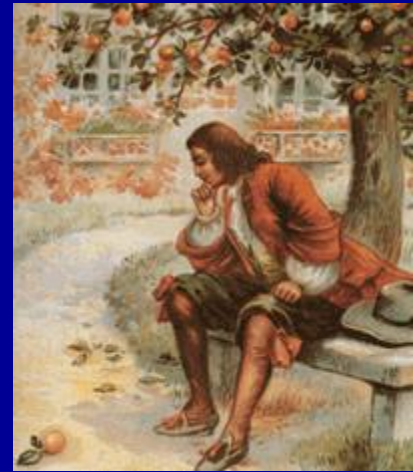
PHYS 343

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# LECTURE 5



*Kinetic Theory of Gases*

*Ideal Gas Model*

*Ideal Gas Model*

*Gas Laws*

# Gas Laws

- (1) When temperature is held constant, the density of a gas is proportional to pressure, and volume is inversely proportional to pressure. Accordingly, an increase in pressure will cause an increase in density of the gas and a decrease in its volume. - **Boyles's Law**
- (2) If volume is kept constant, the pressure of a unit mass of gas is proportional to temperature. If temperature increase so will pressure, assuming no change in the volume of the gas.
- (3) Holding pressure constant, causes the temperature of a gas to be proportional to volume, and inversely proportional to density. Thus, increasing temperature of a unit mass of gas causes its volume to expand and its density to decrease as long as there is no change in pressure. - **Charles's Law**

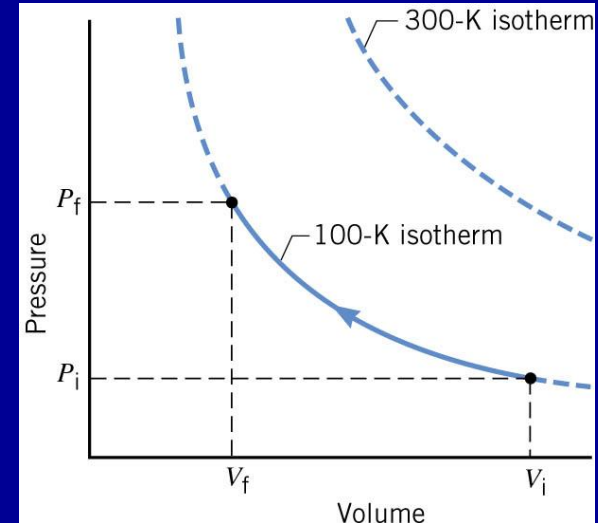
# Boyle's law

At constant temperature, the pressure is inversely proportional to the volume.

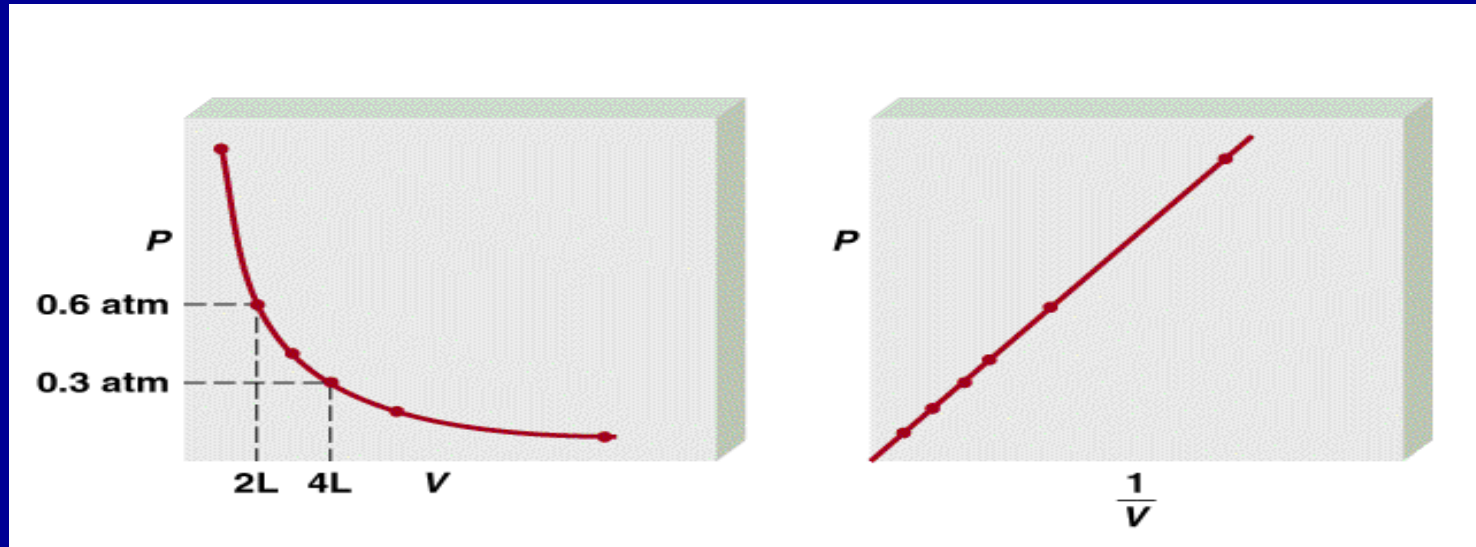
$$P \propto 1/V$$

The pressure is also proportional to the amount of gas.

$$P \propto n$$



# Boyle's law



$$P \propto 1/V$$

$$P \times V = \text{constant}$$

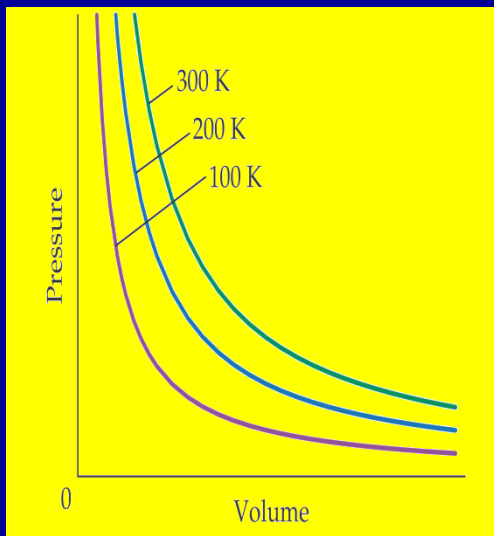
$$P_1 \times V_1 = P_2 \times V_2$$



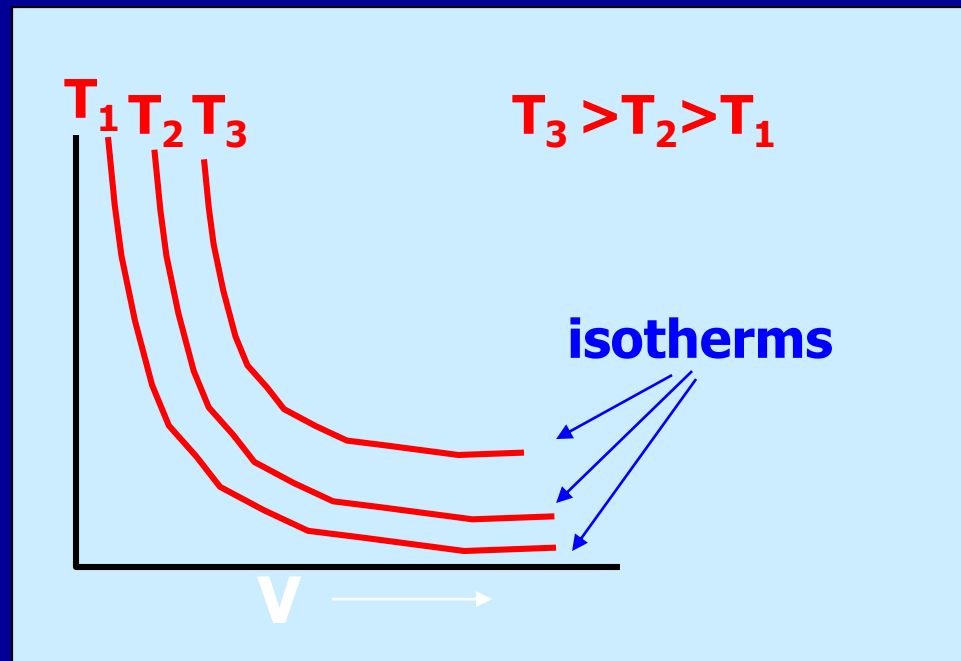
Constant temperature  
Constant amount of gas

# Boyle's Law

- Hyperbolic Relation Between Pressure and Volume



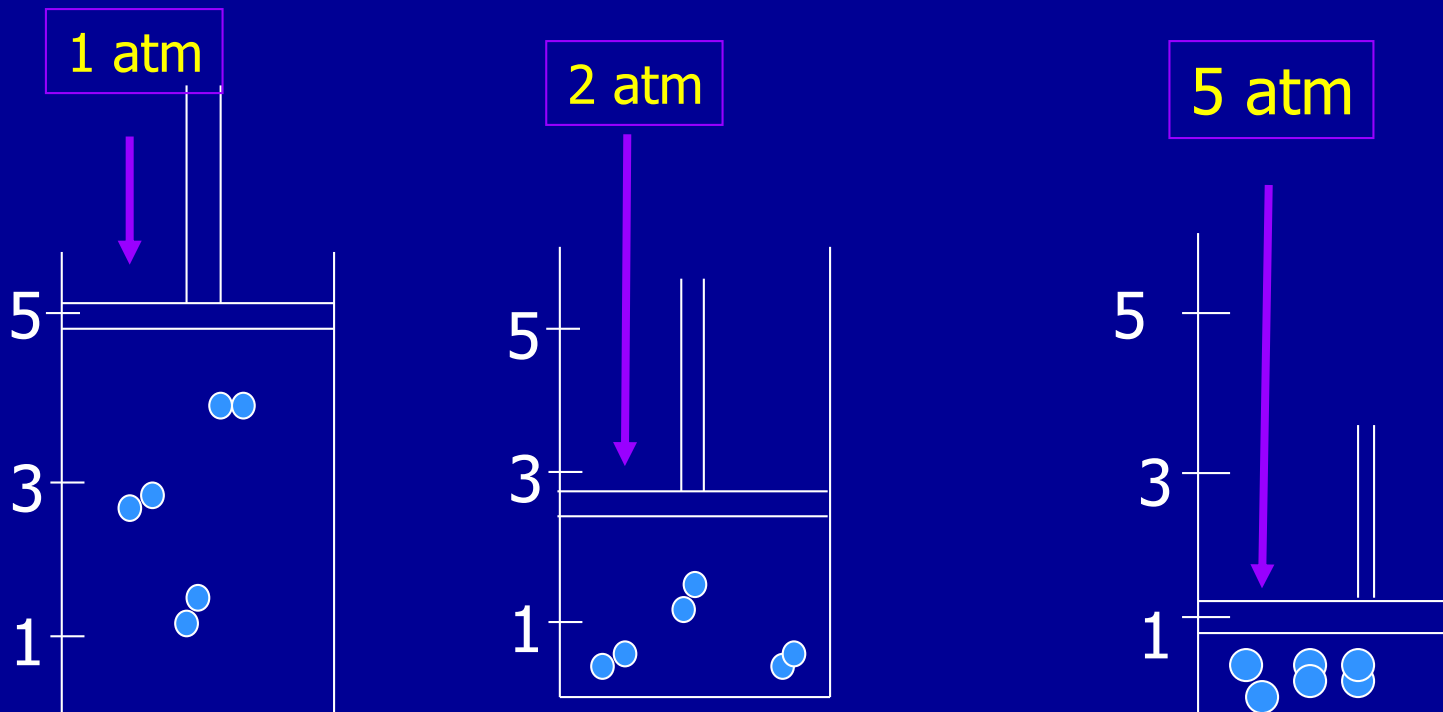
↑  
**p**



**p - V Diagram**

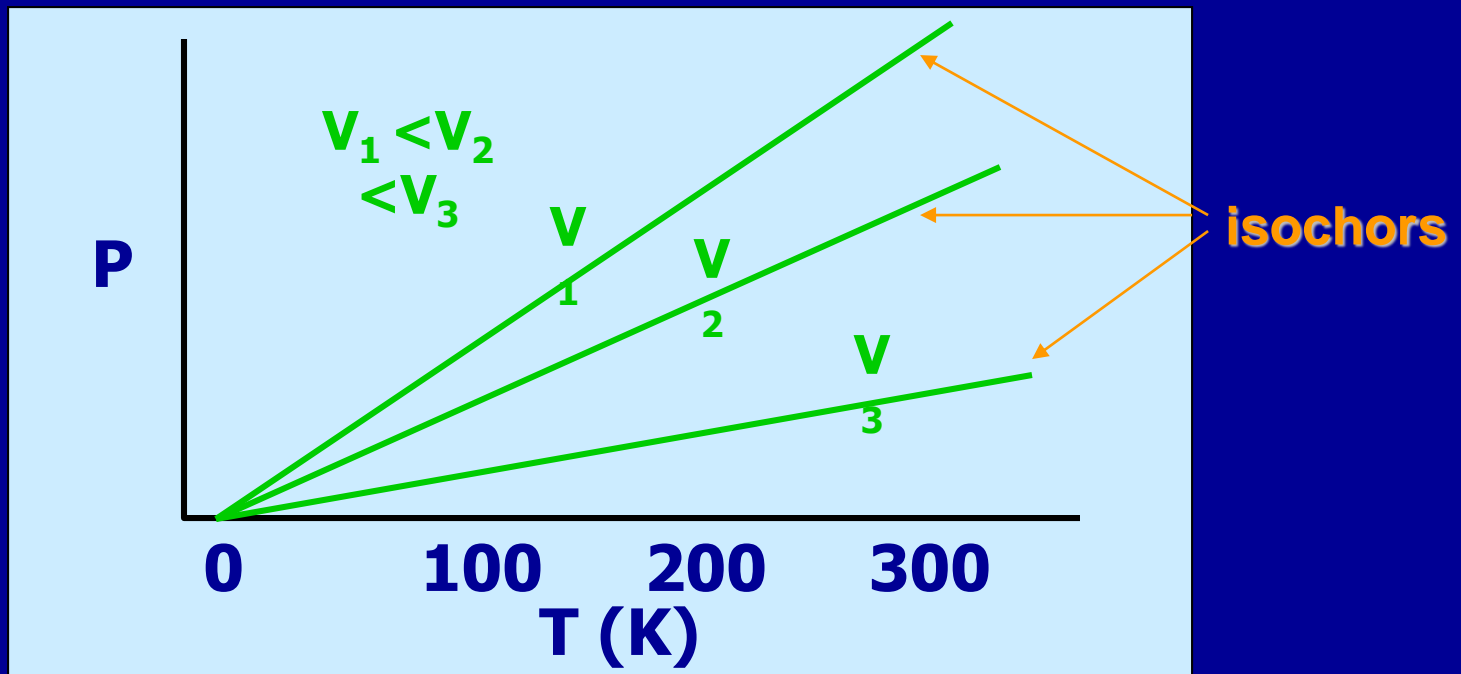
# *Effect of Pressure on Volume*

## *Boyle's Law*



# Charles' Law

- Linear Relation Between Temperature and Pressure

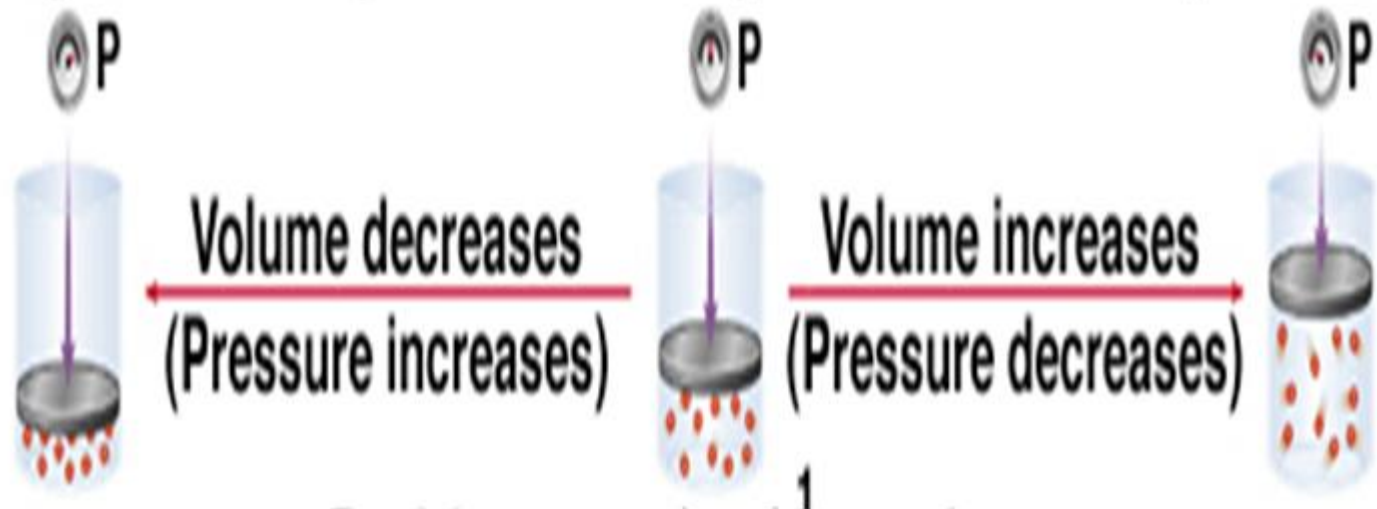


P – T Diagram

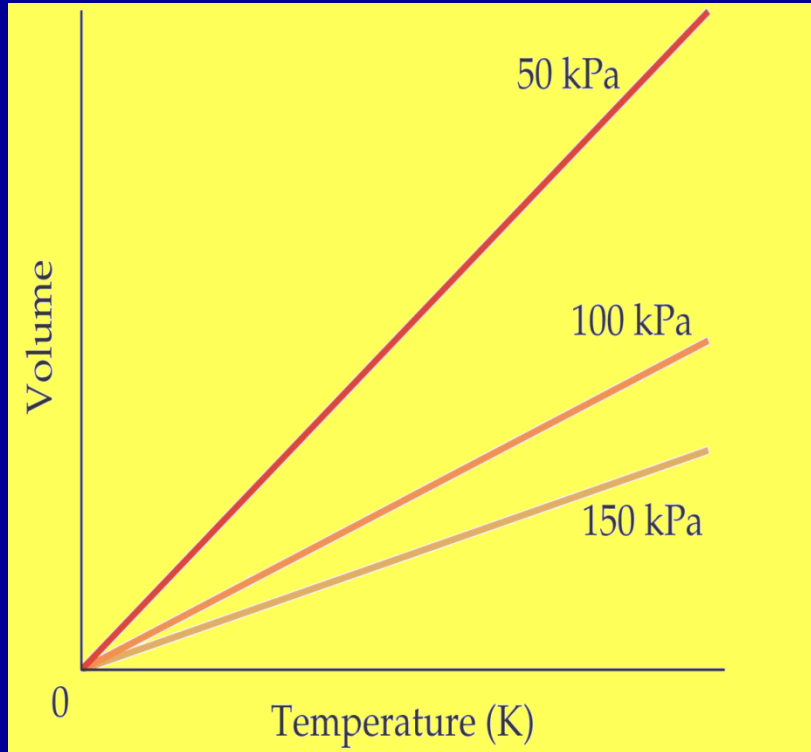


# Charles' Law

Increasing or decreasing the volume of a gas at a constant temperature



# Charles' Law



Real data must be obtained above liquefaction temperature.

Experimental curves for **different gasses, different masses, different pressures** all extrapolate to a **common zero**.

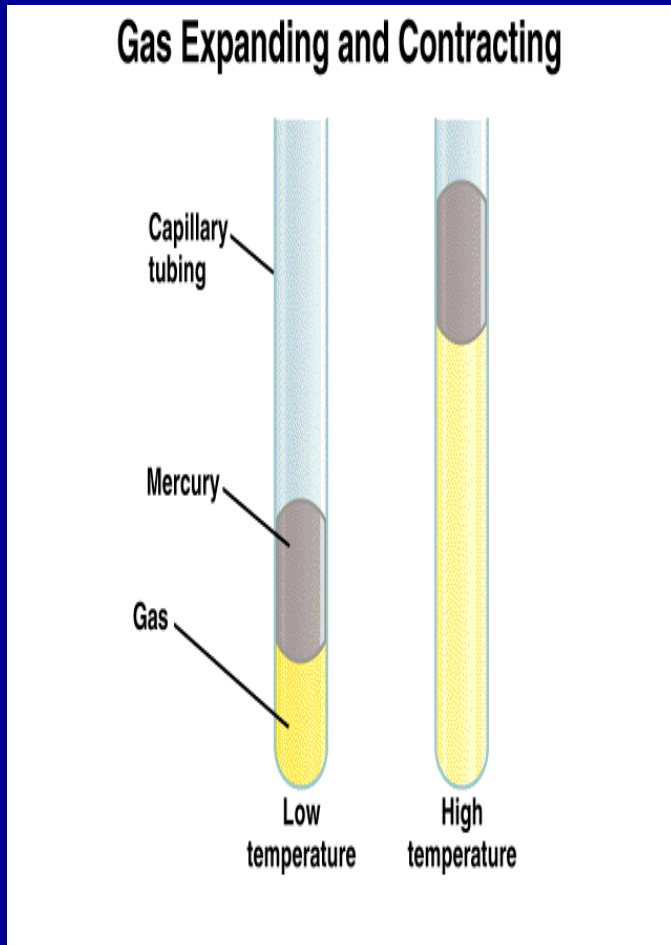
# Charles' Law

$$V \propto T$$

$$V = kT$$

$$V/T = k$$

$$V_1/T_1 = V_2/T_2$$



Constant pressure  
Constant amount  
of gas

As  $T$  increases,  $V$  increases

# Charles' Law

Lower temperature  
(Volume decreases)

Higher temperature  
(Volume increases)

Charles's Law  $V = \left(\frac{nR}{P}\right)T$   $\frac{nR}{P}$  is constant

Heating or cooling a gas at constant volume

Lower temperature  
(Pressure decreases)

Higher temperature  
(Pressure increases)

The diagram consists of two rows of three gas cylinders each. Each cylinder has a piston and a pressure gauge labeled 'P'. In the top row, the cylinders are connected by a horizontal line, and arrows indicate transitions between them. The first cylinder is at a lower temperature and lower volume. An arrow points to the second cylinder, labeled 'Lower temperature (Volume decreases)'. Another arrow points to the third cylinder, labeled 'Higher temperature (Volume increases)'. The bottom row follows a similar pattern, with arrows labeled 'Lower temperature (Pressure decreases)' and 'Higher temperature (Pressure increases)'. The text 'Charles's Law  $V = \left(\frac{nR}{P}\right)T$   $\frac{nR}{P}$  is constant' is centered between the two rows. Below the top row, the text 'Heating or cooling a gas at constant volume' is written.

# *Effect of Temperature on Volume*

## *Charles' Law*



Low Temperature



High Temperature

***The Volume of a gas increases with and increase in temperature.***

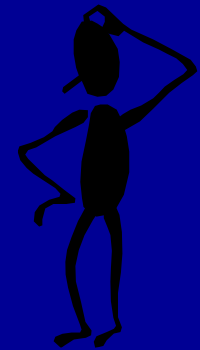


A sample of chlorine gas occupies a volume of 946 mL at a pressure of 726 mmHg. What is the pressure of the gas (in mmHg) if the volume is reduced at constant temperature to 154 mL?

$$P_1 \times V_1 = P_2 \times V_2$$

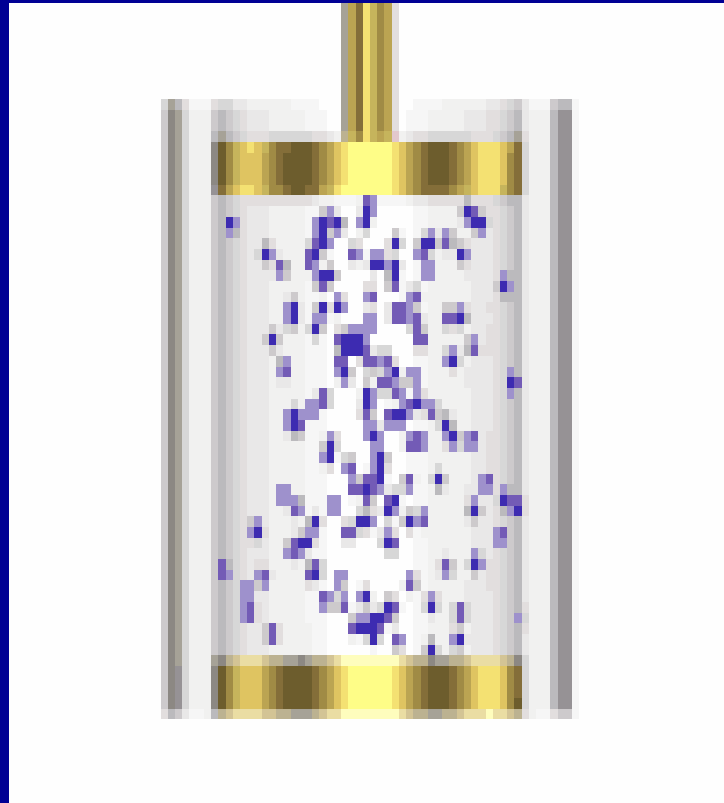
$$P_1 = 726 \text{ mmHg} \quad P_2 = ?$$

$$V_1 = 946 \text{ mL} \quad V_2 = 154 \text{ mL}$$



$$P_2 = \frac{P_1 \times V_1}{V_2} = \frac{726 \text{ mmHg} \times 946 \text{ mL}}{154 \text{ mL}} = 4460 \text{ mmHg}$$

**Compression and expansion of adiabatically isolated gas is accompanied by its heating and cooling.**





# ***Dalton's Law***

Pressure each gas in a mixture would exert if it were the only gas in the container

## **Dalton's Law of Partial Pressures**

The total pressure exerted by a gas mixture is the sum of the partial pressures of the gases in that mixture.

$$P_T = P_1 + P_2 + P_3 + \dots$$

# *Partial Pressures*

The total pressure of a gas mixture depends on the total number of gas particles, not on the types of particles.

**STP**

**P = 1.00 atm**

**P = 1.00 atm**

**1.0 mol He**

**0.50 mol O<sub>2</sub>  
+ 0.20 mol He  
+ 0.30 mol N<sub>2</sub>**

## *Dalton's Law...*

Suppose we have two gases in a container:  $n_A$  moles of gas A and  $n_B$  moles of gas B.

We can define individual **partial pressures**

$$p_A = n_A RT/V \text{ and } p_B = n_B RT/V .$$

Dalton's Law is that the measured total pressure  $p$  is the sum of the partial pressures of all the components:

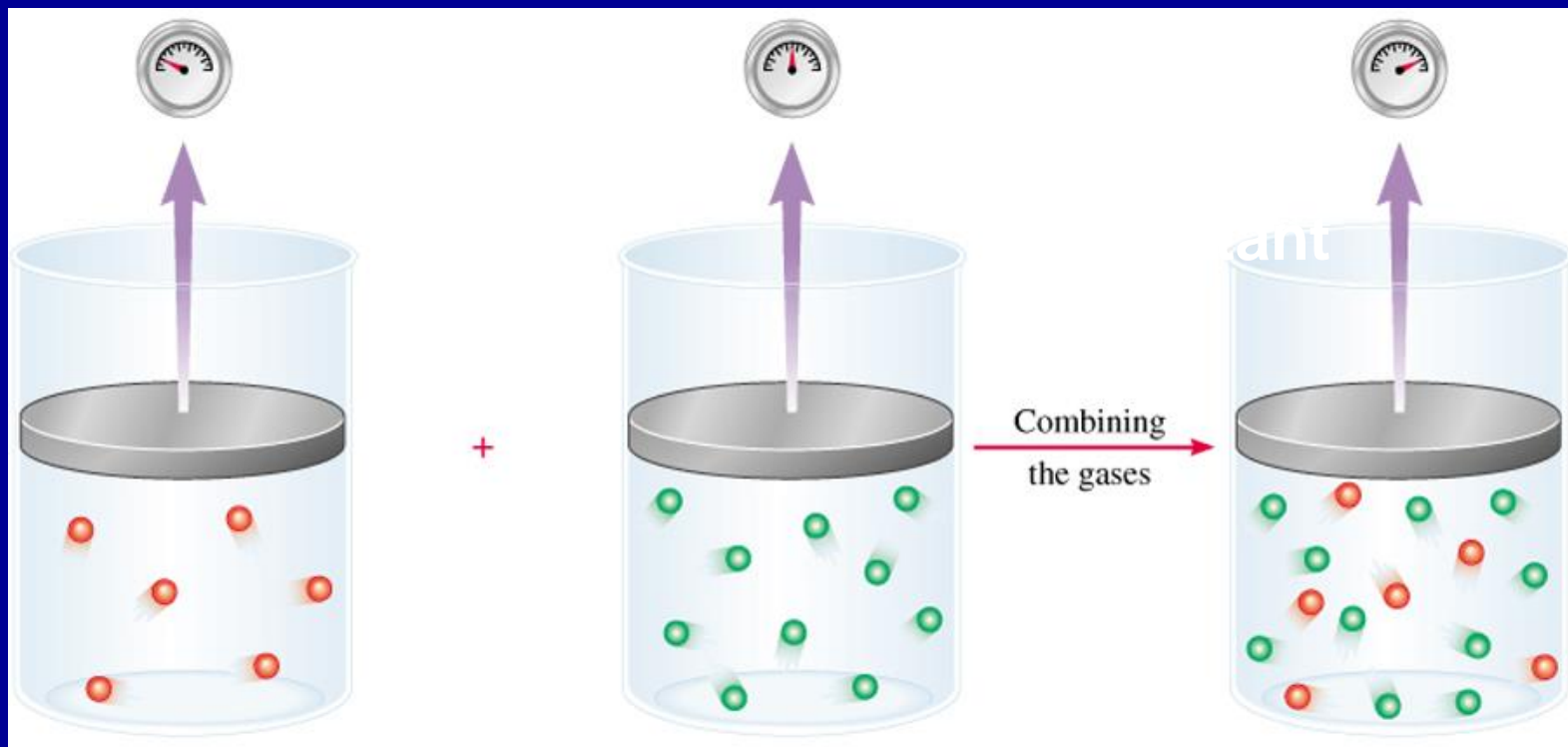
$$p = p_A + p_B + \dots = (n_A + n_B + \dots) RT/V.$$

**Mole fractions:** define  $x_J$  for species J as  $n_J/n$

where  $n = (n_A + n_B + \dots)$ .

Then,  $x_A + x_B + \dots = 1$  and  $p_J = p x_J$

# Dalton's Law of Partial...



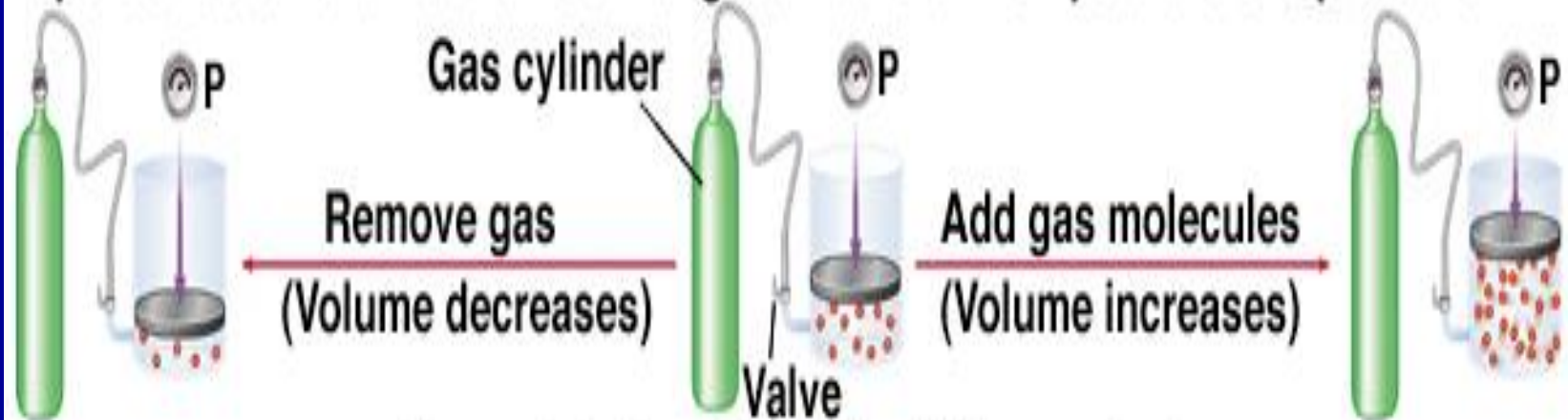
$P_1$

$P_2$

$$P_{\text{total}} = P_1 + P_2$$

# Avogadro' Law

Dependence of volume on amount of gas at constant temperature and pressure



Avogadro's Law  $V = \left(\frac{RT}{P}\right)n$   $\frac{RT}{P}$  is constant

# Avogadro's Law

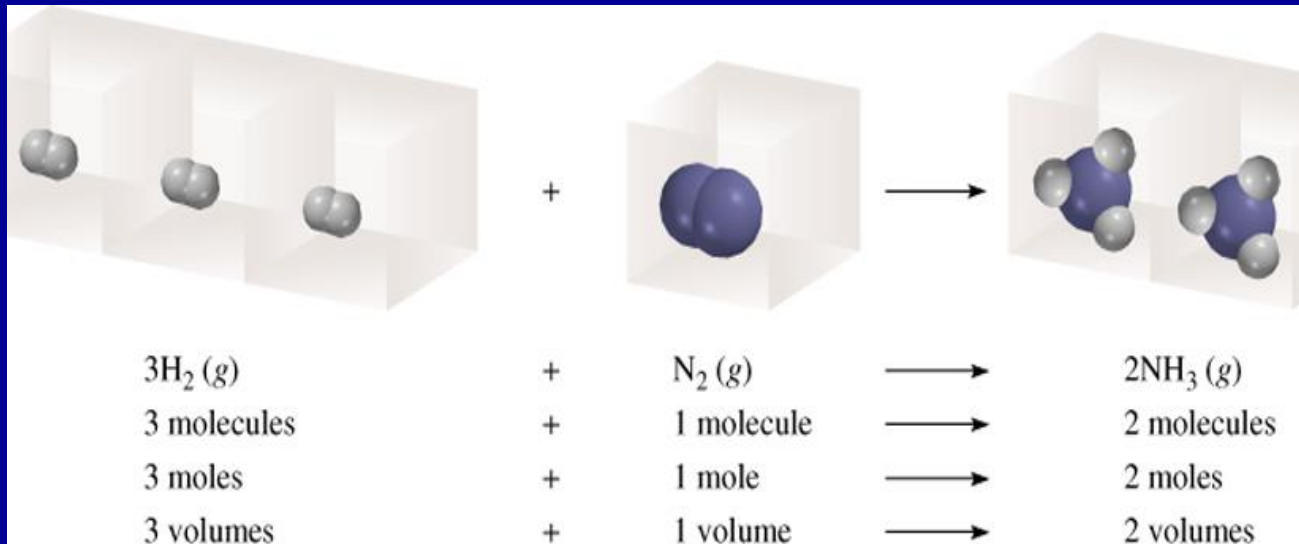
$V \propto$  number of moles ( $n$ )

$V = \text{constant} \times n$

$V_1/n_1 = V_2/n_2$



Constant temperature  
Constant pressure



## Learning Check

A 5.00 L scuba tank contains 1.05 mole of O<sub>2</sub> and 0.418 mole He at 25°C. What is the partial pressure of each gas, and what is the total pressure in the tank?

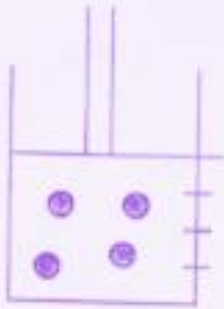
### ■ Solution

$$P = \frac{nRT}{V}$$

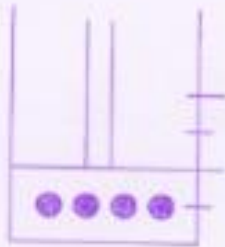
$$P_T = P_{O_2} + P_{He}$$

$$\begin{aligned} P_T &= \frac{1.47 \text{ mol} \times 0.0821 \text{ L-atm} \times 298 \text{ K}}{5.00 \text{ L} \quad (\text{K mol})} \\ &= 7.19 \text{ atm} \end{aligned}$$

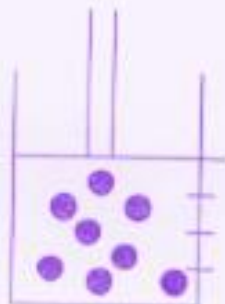
Which picture represents what the gas will look like when the moles of gas is doubled?  
(Assume constant P, T)



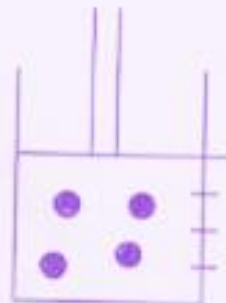
Before



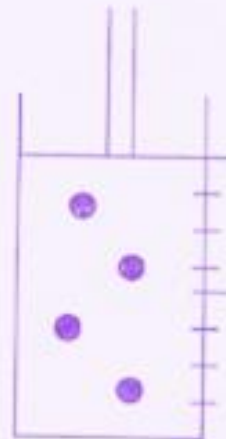
A



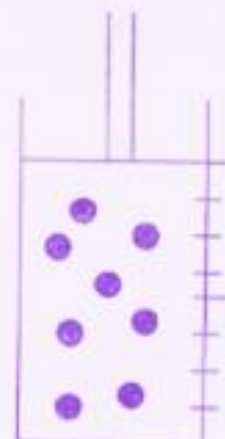
B



C



D



E



*Air bag*



# *Conclusion*

## *Gas Laws*

- When a gas is kept at a constant temperature, its pressure is inversely proportional to its volume (Boyle's law)
- When a gas is kept at a constant pressure, its volume is directly proportional to its temperature (Charles and Gay-Lussac's law)
- When the volume of the gas is kept constant, the pressure is directly proportional to the temperature (Guy-Lussac's law)

