

Name in Arabic :
Student Number:

Lecture time :

KING SAUD UNIVERSITY
COLLEGE OF ENGINEERING
CIVIL ENGINEERING DEPARTMENT

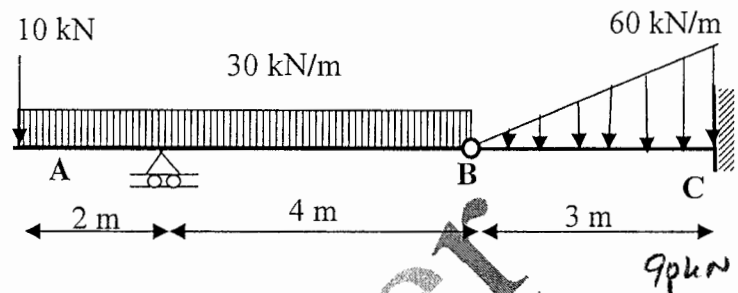
STRUCTURAL ANALYSIS : CE 361
SECOND SEMESTER, 1428/1429 H
TIME : 90 min

SECOND MID TERM EXAM

Problem 1: (12 points)

For the shown loaded beam it is required to;

- 1- Determine the reactions at supports
- 2- Draw S.F.D and B.M.D showing all necessary values and tangents on the diagrams with a reasonable scale.



$$\sum M_B = 0;$$

$$10(6) + 180(3) - R_A(4) = 0$$

$R_A = 150 \text{ kN}$
$R_B = 40 \text{ kN}$
$R_C = 130 \text{ kN}$

[2]

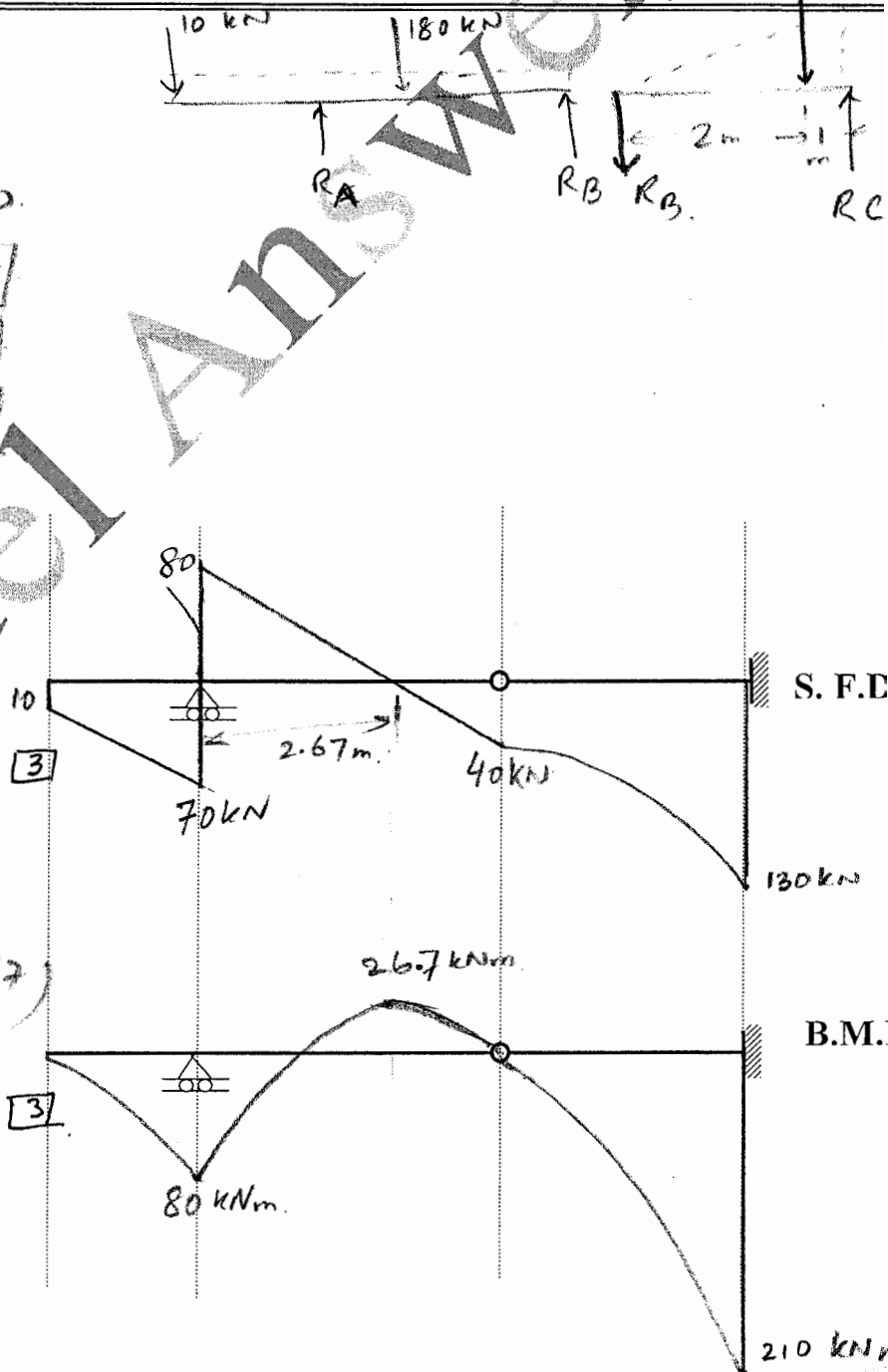
$$M_c + 90(1) + 40(3) = 0$$

$$M_c = 210 \text{ kNm}$$

Model Answer

M_{max}

$$\begin{aligned} &= 10(4.67) + (30 \times 4.67 \times \frac{4.67}{2}) \\ &\quad - 150(2.67) \\ &= 26.67 \\ &= \underline{26.7 \text{ kNm}} \end{aligned}$$



[3]

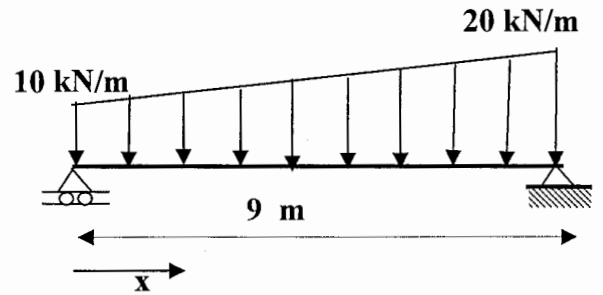
[3]

Problem 2: (8 points)

For the shown loaded beam, it is required to;

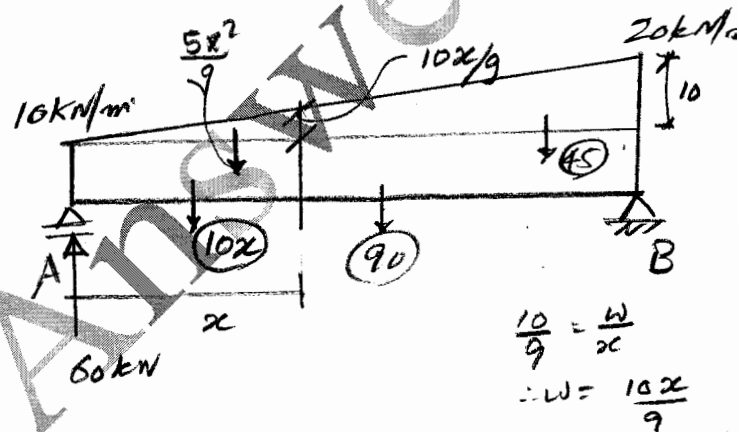
- 1- Write the shear force equation in terms of x
- 2- Write the bending moment equation in terms of x
- 3- Determine the maximum value of bending moment.

Show all necessary values and tangents on diagrams



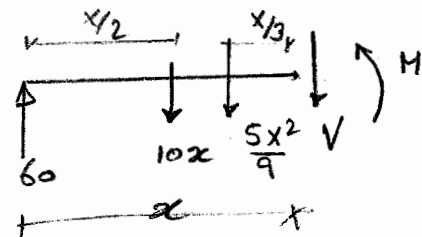
Reactions.

$$\begin{aligned} \sum M_A &= 90 \times 4.5 + 45 \times 6 - 9Y_B = 0 \\ \text{1) } Y_B &= 75 \text{ kN} \\ \sum M_B &= 45 \times 3 + 90 \times 4.5 - 9Y_A = 0 \\ Y_A &= 60 \text{ kN} \\ \text{Check } \sum Y &= 0 \quad 75 + 60 - 90 - 45 = 0 \end{aligned}$$



Shear Equation.

$$\begin{aligned} \sum F_y &= 0 \\ \text{2) } 60 - 10x - \frac{5x^2}{9} - V &= 0 \\ V &= 60 - 10x - \frac{5x^2}{9} \end{aligned}$$



Moment Equation.

$$\begin{aligned} \sum M &= 0 \\ \text{2) } 60x - 10x \cdot \frac{x}{2} - \frac{5x^2}{9} \cdot \frac{x}{3} - M &= 0 \\ M &= 60x - 5x^2 - \frac{5x^3}{27} \end{aligned}$$

Position of max Moment. at $V=0$

$$\begin{aligned} \text{OR } 0.556x^2 + 10x - 60 &= 0 \\ x^2 + 17.986x - 107.9 &= 0 \end{aligned}$$

$$60 - 10x - \frac{5x^2}{9} = 0$$

$$\begin{aligned} x &= \frac{-17.986 \pm \sqrt{(17.986)^2 + 4 \times 107.9}}{2} \\ x &= 4.747 \text{ m} \\ x &= -22.7 \text{ m (Rejected)} \end{aligned}$$

$$\text{2) } \therefore x = 4.747 \text{ m}$$

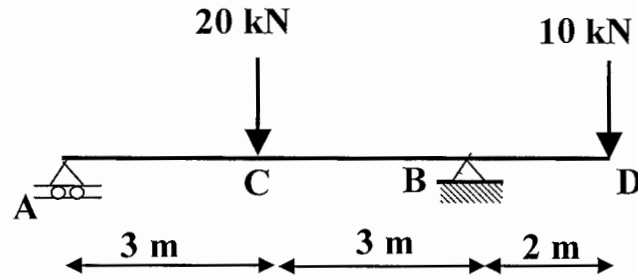
$$\begin{aligned} \therefore \text{Max Moment} = M_{\text{max}} &= 60(4.747) - 5(4.747)^2 - \frac{5}{27}(4.747)^3 \\ &= 152.34 \text{ kN.m} \end{aligned}$$

Problem 3: (10 points)

For the shown beam , Use Conjugate beam method to:

- 1- Determine the deflection at "C"
- 2- Determine the slope at "B"
- 3- Determine deflection at "D"
- 4- Sketch the elastic curve

Given that $I = 200 \times 10^6 \text{ mm}^4$ and $E = 200 \text{ GPa}$



Reactions for real beam.

$$\sum M_B = 20 \times 3 - 10 \times 2 - 6Y_A = 0 \quad Y_A = 6.67 \text{ kN.}$$

Reactions for conjugate beam.

$$\sum M_A =$$

$$\frac{30}{EI} \times 2 + \frac{15}{EI} \times 3.5 - \frac{15}{EI} (5.5) + 6Y_B = 0$$

$$Y_B = -\frac{5}{EI}$$

$$\sum M_B = \frac{15}{EI} (0.5) - \frac{15}{EI} (2.5) - \frac{30}{EI} (4) - 6Y_A = 0$$

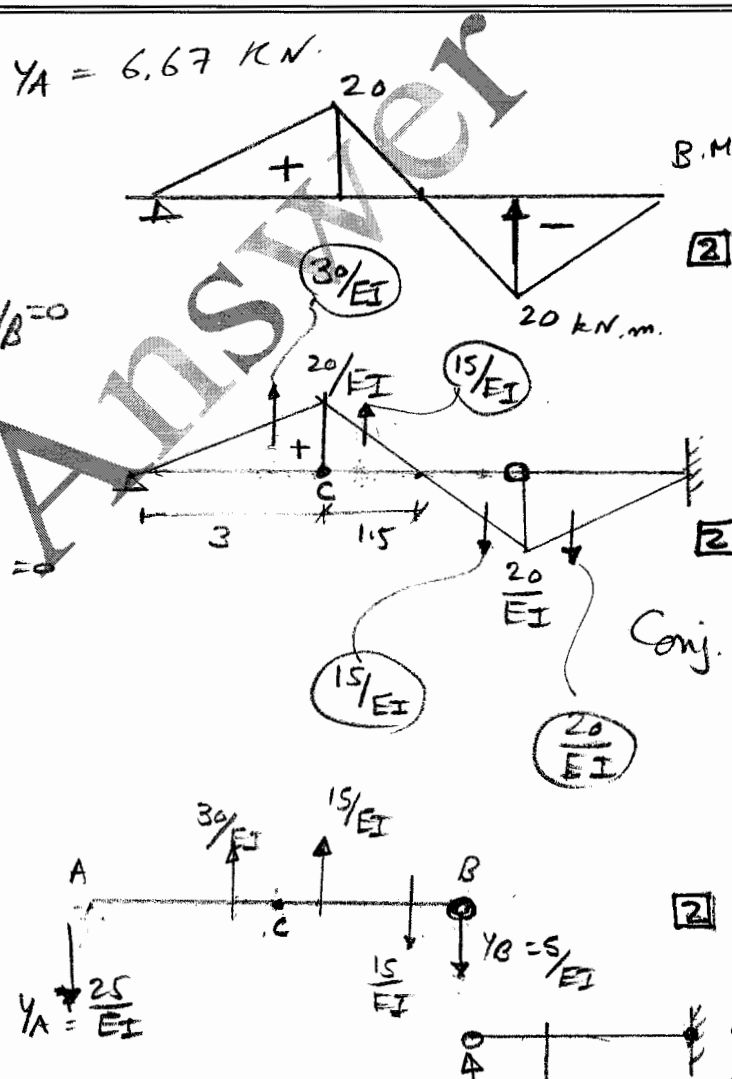
$$Y_A = -\frac{25}{EI}$$

Check $\sum Y = 0$

$$\sum M_D = 0$$

$$\frac{5}{EI} (2) - \frac{20}{EI} \frac{4}{3} - M = 0$$

$$\therefore M = +\frac{16.7}{EI}$$



Deflection at C = $M_C = -\frac{25}{EI} (3) + \frac{30}{EI} \times 1$

$$= -\frac{45}{EI} = \frac{-45}{200 \times 10^6 \times 200 \times 10^6 \times 10^{-12}} = -1.125 \times 10^{-4} \text{ m}$$

Slope at B = $V_B = +\frac{5}{EI} = \frac{5}{200 \times 10^6} = +1.25 \times 10^{-4} \text{ rad.}$

Deflection at D = $M_D = \frac{+16.7}{EI} = \frac{+16.7}{200 \times 10^6} = +4.175 \times 10^{-4} \text{ m}$

