

EE:211

Computational Techniques in Electrical Engineering

Lab#2

Polynomial Interpolation using Matlab-I

1. Use of Matlab command `polyfit ()` to implement polynomial interpolation and use of `polyval ()` to evaluate the polynomial.

To see what the function `polyfit()` does, type this at Matlab command window:

```
>> help polyfit
```

And it gives the following definition:

P = POLYFIT(X,Y,N) finds the coefficients of a polynomial P(X) of degree N that fits the data Y best in a least-squares sense. P is a row vector of length N+1 containing the polynomial coefficients in descending powers, P(1)*X^N + P(2)*X^(N-1) +...+ P(N)*X + P(N+1).

Let's implement the Example 4.1.1 on page: 119 of the textbook, which implement the linear interpolation for the data points, $x = [1, 4]$, $y = [1, 2]$. If we simplify the equation (4.2) then we get the following polynomial:

$$P_1(x) = 0.333x + 0.667 \quad \text{----- equation(1)}$$

To determine the above polynomial representation uses the following Matlab code:

```
>> x = [1, 4], y = [1, 2]
```

```
>> p1 = polyfit(x, y, 1)
```

```
p1 = 0.3333 0.6667
```

This give the coefficient for linear interpolation polynomial (use $n=1$) as given in equation (1), Suppose we want to evaluate this polynomial as given by equation (1) at $x=2$, i.e. $P_1(2) = 1.3333$. We can use the Matlab command `polyval ()` to evaluate the polynomial at any point x . For the $p1$ coefficient calculated above use the following code to evaluate the above polynomial at $x=2$.

```
>> y = polyval(p1, 2) y = 1.3333
```

Consider the Example 4.1.3 on page:121, which determine the quadratic polynomial for the data points $x = [0 1 2]$ and $y = [-1 -1 7]$. The simplified equation (4.9) is given below:

$$P_2(x)=4x^2-4x-1 \quad \text{----- equation(2)}$$

To find the $P_2(x)$ representation (in terms of coefficient) use the following code:

```
>> x=[ 0 1 2] , y=[-1 -1 7]
```

```
>> p2=polyfit(x,y,2)
```

```
p2 = 4 -4 -1
```

2. Constructing the Lagrange Interpolating Polynomial using Matlab

1. In order to construct the Lagrange Coefficients for the Lagrange Polynomial in MATLAB, we can use the built-in function **poly**, which constructs a polynomial with given roots.

Enter the following to construct a polynomial with roots 1 and 2 for example:

```
» poly([1 2])
```

```
ans =
```

```
1 -3 2
```

Thus, this is the polynomial $(x-1)(x-2) = x^2 - 3x + 2$ which has roots 1 and 2.

2. Consider the Example 4.1.3, page 121 which construct Lagrange interpolating polynomial of degree two (quadratic) approximating the data points $[(0,-1),(1,-1),(2,7)]$

Consider the Lagrange basis function $L_0(x)$ given as

$$L_0(x) = \frac{(x-1)(x-2)}{(0-1)(0-2)}$$

We can see that we need the numerator to be the polynomial with roots $x_1 = 1$, and $x_2 = 2$, i.e. $(x-1)(x-2)$ The denominator is the constant $(x_0 - x_1)(x_0 - x_2) = (0-1)(0-2) = 2$.

Assuming that we want to store the Lagrange coefficient polynomials in the 3x3 array (matrix) L (with the 1st row being the coefficients for $L_0(x)$, the 2nd row being the coefficients for $L_1(x)$, and the third row being the coefficients for $L_2(x)$), we proceed as follows:

```
>> L(1,:)= poly([1 2])/((0 - 1)*(0 - 2))
```

```
L = 0.5000 -1.5000 1.0000
```

```
>> L(2,:)= poly([0 2])/((1 - 0)*(1 - 2))
```

```
L = 0.5000 -1.5000 1.0000
```

```
-1.0000 2.0000 0
```

```
>> L(3,:)= poly([0 1])/((2 - 0)*(2 - 1))
```

```
L =
```

```
0.5000 -1.5000 1.0000
```

```
-1.0000 2.0000 0
```

```
0.5000 -0.5000 0
```

The final Lagrange polynomial is: $P_2(x) = y_0 * L_0(x) + y_1 * L_1(x) + y_2 * L_2(x)$. We compute the $P_2(x)$ as:

```
>> P = (-1)*L(1,:) + (-1)*L(2,:) + (7)*L(3,:)
```

```
P = 4 -4 -1
```

This has the same coefficient as equation (2) above.

To evaluate the polynomial at 2 we use:

```
>> polyval(P,2)
```

```
ans =7
```