

Name of the Student: \_\_\_\_\_ I.D. No. \_\_\_\_\_

Name of the Teacher: \_\_\_\_\_ Section No. \_\_\_\_\_

**Note: Check the total number of pages are Six (6).**  
 (15 Multiple choice questions and Two (2) Full questions)

The Answer Tables for Q.1 to Q.15 : Marks: 2 for each one ( $2 \times 15 = 30$ )

Ps. : Mark {a, b, c or d} for the correct answer in the box.

Q. No.	1	2	3	4	5	6	7	8	9	10
a,b,c,d										

Q. No.	11	12	13	14	15
a,b,c,d					

Quest. No.	Marks Obtained	Marks for Questions
Q. 1 to Q. 15		30
Q. 16		5
Q. 17		5
Total		40

**Question 1:** If  $x_{n+1} = \frac{a}{b - \cos(x_n)}$ ,  $n \geq 0$ , is the fixed-point iterative form of the nonlinear equation  $\frac{2}{x} + \cos(x) - 3 = 0$ , then the value of the constants  $a$  and  $b$  are:

- (a)  $a = 2, b = 3$       (b)  $a = 3, b = 2$       (c)  $a = 2, b = 1$       (d) None of these

**Question 2:** The next iterative value of the root of  $x^3 = 3x - 2$  using the secant method, if the initial guesses are  $-2.6$  and  $-2.4$  is:

- (a)  $-2.3066$       (b)  $-2.2066$       (c)  $-2.1066$       (d) None of these

**Question 3:** If the iterative scheme  $x_{n+1} = x_n - k \frac{f(x_n)}{f'(x_n)}$ ,  $n \geq 0$ , converges at least quadratic to a simple root  $\alpha$ , then the value of  $k$  is:

- (a)  $k=2$       (b)  $k=1$       (c)  $k=3$       (d) None of these

**Question 4:** The  $l_\infty$ -norm of the inverse of the Jacobian matrix for the nonlinear system  $x^2 + y^2 = 4$ ,  $2x - y^2 = 0$  using  $[x_0, y_0]^t = [1, 1]^t$  is:

- (a) 0.5      (b) 2      (c) 4      (d) None of these

**Question 5:** Let  $A = \begin{bmatrix} 1.001 & 1.5 \\ 2 & 3 \end{bmatrix}$ , then the determinant of a lower-triangular matrix  $L$  of the LU factorization using Crouts method is:

- (a) 0.300      (b) 0.003      (c) 1.001      (d) None of these

**Question 6:** The  $l_\infty$ -norm of the Jacobi iteration matrix of the following linear system  $4x_1 - x_2 + x_3 = 7$ ,  $4x_1 - 8x_2 + x_3 = -21$ ,  $-2x_1 + x_2 + 5x_3 = 15$  is:

- (a) 0.4      (b) 0.5      (c) 0.625      (d) None of these

**Question 7:** Using Gauss-Seidel method and starting with  $\mathbf{x}^{(0)} = [1.200, 0.467, 1.033]^t$ , then the first approximation of the solution for the following linear system is:  
 $5x_1 + 2x_2 - x_3 = 6$ ,  $x_1 + 6x_2 - 3x_3 = 4$ ,  $2x_1 + x_2 + 4x_3 = 7$  is:

- (a)  $\mathbf{x}^{(1)} = \begin{pmatrix} 1.220 \\ 0.980 \\ 0.895 \end{pmatrix}$       (b)  $\mathbf{x}^{(1)} = \begin{pmatrix} 0.897 \\ 0.950 \\ 1.019 \end{pmatrix}$       (c)  $\mathbf{x}^{(1)} = \begin{pmatrix} 1.024 \\ 1.006 \\ 0.987 \end{pmatrix}$       (d) None of these

**Question 8:** Let  $A = \begin{bmatrix} 0 & \alpha \\ 1 & 1 \end{bmatrix}$  and  $1 < \alpha < 2$ . If the condition number  $k(A)$  of the matrix  $A$  is 6, then  $\alpha$  equals to

- (a) 0.2      (b) 0.8      (c) 0.5      (d) None of these

**Question 9:** Let  $x_0 = 2$ ,  $x_1 = 2.5$ ,  $x_2 = 4$  and  $x_3 = 5.5$ . If the best approximation of  $f(x) = \frac{1}{x}$  at  $x = 3$  using quadratic interpolation formula is  $P_2(3) = 0.325$ , then the value of the unknown point  $\eta$  in the error formula is equal to :

- (a) 2.7859      (b) 2.9201      (c) 3.1472      (d) None of these

**Question 10:** If  $x_0 = 0$ ,  $x_1 = 1$ ,  $x_2 = 3$  and for a function  $f(x)$ , the divided differences are  $f[x_1] = 2$ ,  $f[x_2] = 3$ ,  $f[x_0, x_1] = 1$ ,  $f[x_1, x_2] = \frac{1}{2}$ ,  $f[x_0, x_1, x_2] = -\frac{1}{6}$ . Then the approximation of  $f(\frac{1}{2})$  using quadratic interpolation Newton formula is:

- (a) 4.1232      (b) 1.5417      (c) 2.3481      (d) None of these

**Question 11:** Let  $f(x) = x^3$  and  $h = 0.1$ . The absolute error for the approximation of  $f'(0.2)$  using 2-point forward difference formula is:

- (a) 0.0711      (b) 0.0700      (c) 0.0722      (d) None of these

**Question 12:** The absolute error for the approximation of the integral  $\int_1^2 \frac{1}{x+1} dx$  using simple Trapezoidal's rule is:

- (a) 0.0012      (b) 0.1120      (c) 0.0112      (d) None of these

**Question 13:** The approximation to the integral  $\int_0^2 e^x dx$  using simple Simpson's rule is:

- (a) 6.4207      (b) 7.4207      (c) 8.4207      (d) None of these

**Question 14:** For the initial value problem,  $(x+1)y' + y^2 = 0$ ,  $y(0) = 1$ ,  $n = 1$ , if the actual solution of the differential equation is  $y(x) = \frac{1}{(1 + \ln(x+1))}$ , then the absolute error by using Euler's method for the approximation of  $y(0.05)$  is:

- (a) 0.0042      (b) 0.0350      (c) 0.0035      (d) None of these

**Question 15:** Using the Taylor's method of order 2 to find the approximate value of  $y(0.1)$  for the initial-value problem,  $y' = e^{-2x} - 2y$ ,  $y(0) = 0.1$ ,  $n = 1$ , is:

- (a) 0.1846      (b) 0.1983      (c) 0.1620      (d) None of these

**Question 16:** Let  $f(x) = \frac{3^x}{x}$  and  $h = 0.1$ . Compute the approximate value of  $f''(3)$  and the absolute error. If  $\max |f^{(4)}| = 6.1022$ , then find the number of subintervals required to obtain the approximate value of  $f''(3)$  within the accuracy  $10^{-4}$ .

**Question 17:** Determine the number of subintervals required to approximate the integral  $\int_0^2 \frac{1}{x+4} dx$ , with an error less than  $10^{-4}$  using composite Simpson's rule. Then approximate the given integral and compute the absolute error.

