Third Midterm Exam Year 1440-1441 H First Semester		
Course name & code	OPER 441 – Modeling and Simulation النمذجة والمحاكاة – 441 بحث	اسم ورمز المقرر
Date and Time	Wed. 4 – Dec.–2019 (12:00 pm 2 Hours)	الوقت والتاريخ
Instructor's Name	Dr. Khalid Alnowibet د. خالد النويبت	أستاذ المادة

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Section No.		رقم الشعبة
Serial No.		الرقم التسلسلي

Question #1:

A car repair workshop manager wants to develop a simulation model. For one particular repair, the times to completion can be represented by the following distribution (x in days):

$$f(x) = \begin{cases} \frac{x}{8} - \frac{1}{4} & ; \quad 2 \le x \le 4 \\ \frac{10}{24} - \frac{x}{24} & ; \quad 4 \le x \le 10 \end{cases}$$

(a) Compute the CDF of the function $f(x)$.

(b) Give the inverse transform to generate random numbers for repair time.

(c) Using U[0,1] random number in the following table, using the inverse transform in part (b) to determine the time of each car repair.

	1	2	3	4	5	6	7	8	9	10
U[0,1]	0.138	0.776	0.911	0.259	0.458	0.343	0.105	0.940	0.188	0.343
Repair Time										

(d) Let the time between car arrival is shifted binomial distribution with parameters n = 3 and p = 0.45 with shift value δ where the shift value is uniform [1,3]. Write the algorithm for generating the arrival time of job (n).

(e) Using U[0,1] random number in the following table and using the answer in part (d), determine the arrival time of each car for repair.

	1	2	3	4	5	6	7	8	9	10
U_1 [0,1]	0.301	0.120	0.491	0.145	0.448	0.048	0.049	0.846	0.590	0.509
U_2 [0,1]	0.138	0.776	0.911	0.259	0.458	0.343	0.105	0.940	0.188	0.343
Time bet. cars										
Arr. Time										

(f) From you answers, compute the average rate of car arrival to the repair shop per week.

(g) From you answers, compute the average repair time.

Question #2:

Busses arrive to a bus station at random. It is assumed that time between bus arrival is Erlang with parameters $k=2$ and $\lambda= 4$ busses/hour. Each bus has a maximum of 5 seats. Any bus arrives to the station carries a random number of passengers. Past data shows that the distribution of number of passengers is binomial distribution with mean 3.5 passengers.

(a) Write the steps and required functions for simulation of bus arrival.
(b) Write the steps and functions for simulation of number of passengers in the bus.
(c) Using the following random U[0,1], do simulation for bus arrivals during the first 1:30 hours and number of passenger in each bus.

BUS #	u_1 ~ U[0,1]	u_2 ~ U[0,1]	u_3 ~ U[0,1]	u_4 ~ U[0,1]				
1	0.150	0.130	0.176	0.614				
2	0.339	0.180	0.453	0.301				
3	0.220	0.306	0.484	0.139				
4	0.516	0.603	0.949	0.666				
5	0.188	0.213	0.504	0.324				
6	0.804	0.755	0.465	0.237				
7	0.795	0.347	0.548	0.072				
8	0.918	0.355	0.206	0.118				
9	0.742	0.050	0.873	0.463				
10	0.385	0.196	0.517	0.011				

NOTE: Use u_1, u_2, u_3, u_4, as needed for each bus.

Question #3:

Consider the following probability density function:

$$f(x) = \frac{4}{80}x^3 ; \quad 1 \le x \le 3$$

Assume that there are two types of breakdowns happen on a machine: BKD-1 and BKD-2. BKD-1 needs a random amount to repair and it follows the pdf in (a). BKD-2 needs a random amount to repair and it follows the exponential distribution with mean 2 hours. From past data 40% of the time BKD-1 happens.

(a) and the time Let Y be the repair time. Write the CDF of Y($F(y)$)

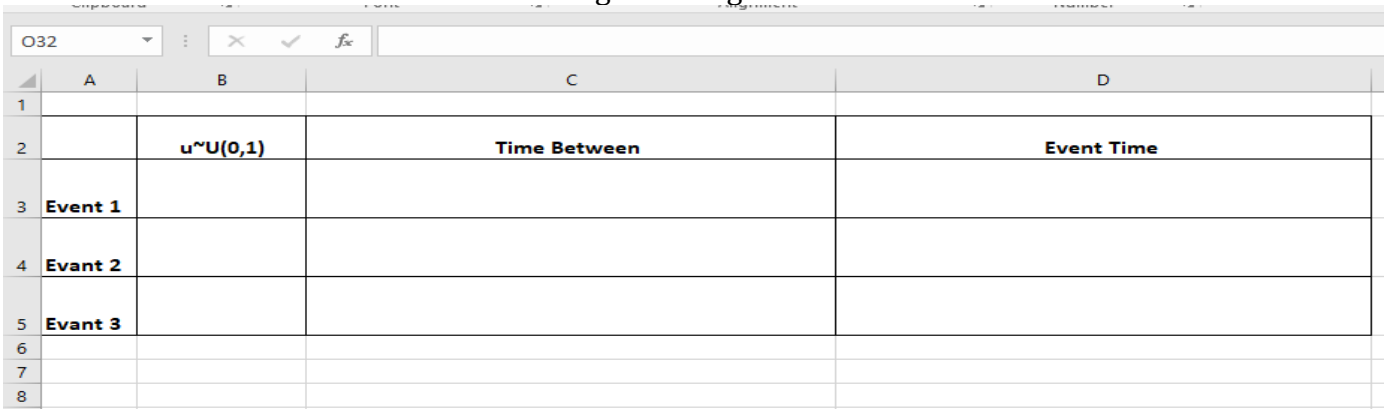
(b) Write the steps to generate observations for the repair time.

(c) Use the following table for simulation of 5 breakdowns in the machine.

	1	**2**	**3**	**4**	**5**
U₁[0,1]	0.0129	0.1164	0.6804	0.9513	0.2017
U₂[0,1]	0.804	0.755	0.465	0.237	0.1105
Type of breakdown					
Repair Time of BKD					

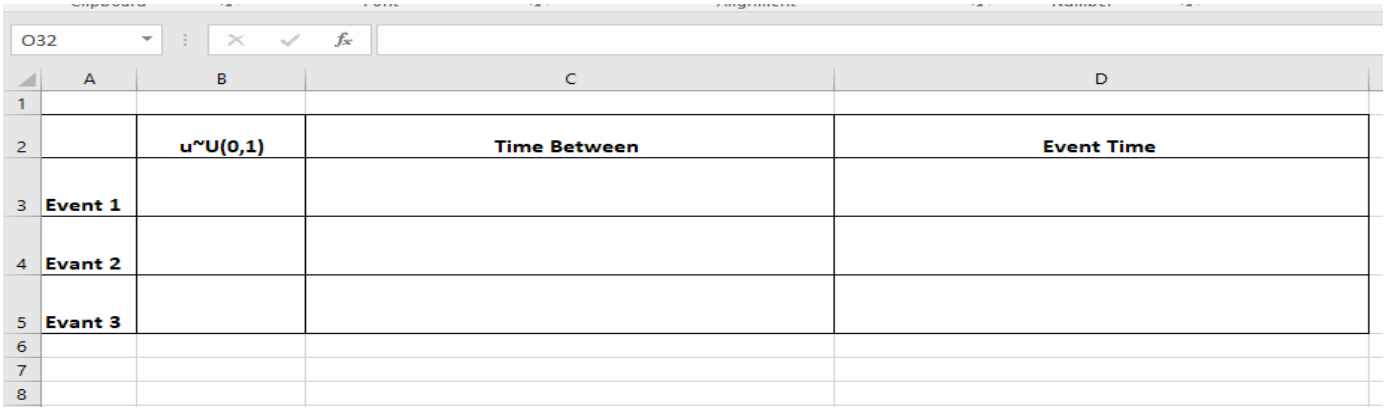
Question #4:

1. If time between event is integer random uniform between 5 min and 10 min. Write the Excel function in the screen shot for generating the time for 1st and 2nd events.



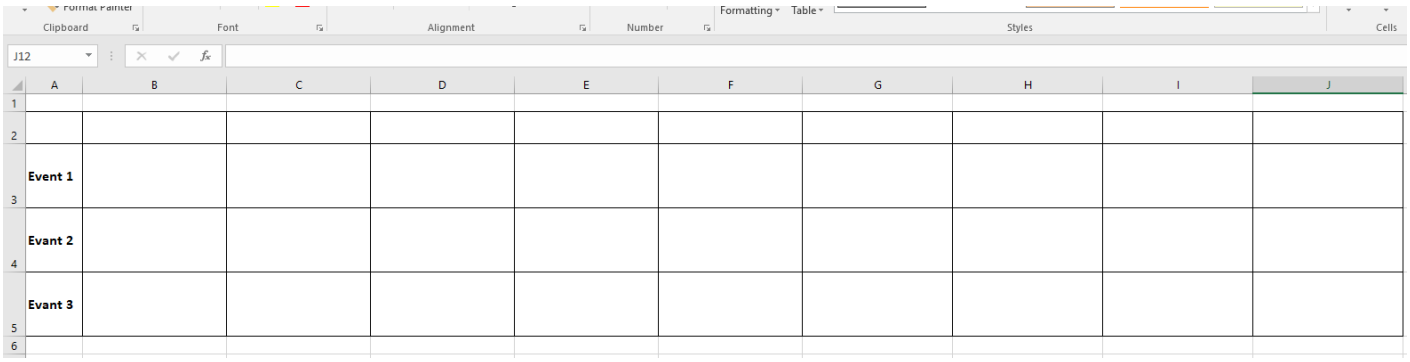
	A	B	C	D
1				
2		u~U(0,1)	Time Between	Event Time
3	Event 1			
4	Evant 2			
5	Evant 3			
6				
7				
8				

2. If time between events is continuous random uniform between 5 min and 10 min. Write the Excel function in the screen shot for generating the time for 1st , 2nd events and 3rd event.



	A	B	C	D
1				
2		u~U(0,1)	Time Between	Event Time
3	Event 1			
4	Evant 2			
5	Evant 3			
6				
7				
8				

3. If time between events is random with integer values from Normal distribution with positive values only and with parameters $\mu = 3$, $\sigma = 9$. Write the Excel function in the screen shot for generating the time for 1st , 2nd events and 3rd event.



	A	B	C	D	E	F	G	H	I	J
1										
2										
3	Event 1									
4	Evant 2									
5	Evant 3									
6										