

Code Generation

- We focus on generating code for a stack machine with accumulator
- We want to run the resulting code on a real machine – e.g., the MIPS processor (or simulator)
- We simulate stack machine instructions using MIPS instructions and registers

- The accumulator is kept in MIPS register $\$a0$
- The stack is kept in memory
 - The stack grows towards lower addresses
 - Standard convention on MIPS
- The address of the next location on the stack is kept in MIPS register $\$sp$
 - The top of the stack is at address $\$sp + 4$

Notice that $\$sp$ points to the next unused memory, and since the stack grows towards lower addresses the top of the stack is at $\$sp+4$

MIPS architecture

- Prototypical Reduced Instruction Set Computer (RISC)
- Most operations use registers for operands & results
- Use load & store instructions to use values in memory
- 32 general purpose registers (32 bits each)
 - We use `$sp`, `$a0` and `$t1` (a temporary register)
- Read the SPIM documentation for details

SPIM is the simulator that we can use to execute our generated code.

5 MIPS instructions that we will need for our first example :

- lw reg_1 offset(reg_2)
 - Load 32-bit word from address $reg_2 + \text{offset}$ into reg_1
- add reg_1 reg_2 reg_3
 - $reg_1 \leftarrow reg_2 + reg_3$
- sw reg_1 offset(reg_2)
 - Store 32-bit word in reg_1 at address $reg_2 + \text{offset}$
- addiu reg_1 reg_2 imm
 - $reg_1 \leftarrow reg_2 + \text{imm}$
 - “u” means overflow is not checked
- li reg imm
 - $reg \leftarrow \text{imm}$

The stack-machine code for $7 + 5$ in MIPS:

$acc \leftarrow 7$

push acc

$acc \leftarrow 5$

$acc \leftarrow acc + \text{top_of_stack}$

pop

The stack-machine code for $7 + 5$ in MIPS:

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push acc

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$acc \leftarrow acc + \text{top_of_stack}$

pop

li \$a0 7

sw \$a0 0(\$sp)

addiu \$sp \$sp -4

li \$a0 5

lw \$t1 4(\$sp)

add \$a0 \$a0 \$t1

addiu \$sp \$sp 4

A language with integers and integer operations

$$P \rightarrow D; P \mid D$$
$$D \rightarrow \text{def id(ARGS) = E};$$
$$\text{ARGS} \rightarrow \text{id, ARGS} \mid \text{id}$$
$$E \rightarrow \text{int} \mid \text{id} \mid \text{if } E_1 = E_2 \text{ then } E_3 \text{ else } E_4 \\ \mid E_1 + E_2 \mid E_1 - E_2 \mid \text{id}(E_1, \dots, E_n)$$

- The first function definition `f` is the entry point
 - The “main” routine
- Program for computing the Fibonacci numbers:

```
def fib(x) = if x = 1 then 0 else
             if x = 2 then 1 else
             fib(x - 1) + fib(x - 2)
```

- For each expression e we generate MIPS code that:
 - Computes the value of e in $\$a0$
 - Preserves $\$sp$ and the contents of the stack
- We define a code generation function $cgen(e)$ whose result is the code generated for e

- The code to evaluate a constant simply copies it into the accumulator:

`cgen(j) = li $a0 i`

- This preserves the stack, as required
- Color key:
 - RED: compile time
 - BLUE: run time

```
cgen(e1 + e2) =  
    cgen(e1)  
    sw $a0 0($sp)  
    addiu $sp $sp -4  
    cgen(e2)  
    lw $t1 4($sp)  
    add $a0 $t1 $a0  
    addiu $sp $sp 4
```

```
cgen(e1 + e2) =  
  cgen(e1)  
  sw $a0 0($sp)  
  addiu $sp $sp -4  
  cgen(e2)  
  lw $t1 4($sp)  
  add $a0 $t1 $a0  
  addiu $sp $sp 4
```

These two statements store
the result of e₁ into the
stack

cgen($e_1 + e_2$) =

cgen(e_1)

sw \$a0 0(\$sp)

addiu \$sp \$sp -4

cgen(e_2)

lw \$t1 4(\$sp)

add \$a0 \$t1 \$a0

addiu \$sp \$sp 4

These two statements store
the result of e_1 into the
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This instruction load the result of
 e_1 into the temporary reg t1

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cgen(e1 + e2) =  
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  cgen(e2)  
  lw $t1 4($sp)  
  add $a0 $t1 $a0  
  addiu $sp $sp 4
```

These two statements store
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This instruction load the result of
e₁ into the temporary reg t1

accu = e₁+e₁

```
cgen(e1 + e2) =  
  cgen(e1)  
  sw $a0 0($sp)  
  addiu $sp $sp -4  
  cgen(e2)  
  lw $t1 4($sp)  
  add $a0 $t1 $a0  
  addiu $sp $sp 4
```

These two statements store
the result of e₁ into the
stack

This instruction load the result of
e₁ into the temporary reg t1

accu = e₁+e₂

pops the stack


```
cgen(e1 + e2) =  
  cgen(e1)  
  sw $a0 0($sp)  
  addiu $sp $sp -4  
  cgen(e2)  
  lw $t1 4($sp)  
  add $a0 $t1 $a0  
  addiu $sp $sp 4
```

These two statements store
the result of e₁ into the
stack

This instruction load the result of
e₁ into the temporary reg t1

accu = e₁+e₁

pops the stack

Actually the code generator creates a file containing the instructions that will be executed at run time.

```
cgen(e1 + e2) =  
  cgen(e1)  
  print "sw $a0 0($sp)"  
  print "addiu $sp $sp -4"  
  cgen(e2)  
  print "lw $t1 4($sp)"  
  print "add $a0 $t1 $a0"  
  print "addiu $sp $sp 4"
```

- The code for $+$ is a template with “holes” for code for evaluating e_1 and e_2
- Stack machine code generation is recursive
 - Code for $e_1 + e_2$ is code for e_1 and e_2 glued together
- Code generation can be written as a recursive-descent of the AST
 - At least for expressions

- New instruction: `sub reg1 reg2 reg3`

– Implements $\text{reg}_1 \leftarrow \text{reg}_2 - \text{reg}_3$

`cgen(e1 - e2) =`

`cgen(e1)`

`sw $a0 0($sp)`

`addiu $sp $sp -4`

`cgen(e2)`

`lw $t1 4($sp)`

`sub $a0 $t1 $a0`

`addiu $sp $sp 4`

- New instruction: `sub reg1 reg2 reg3`
 - Implements $reg_1 \leftarrow reg_2 - reg_3$
`cgen(e1 - e2) =`
`cgen(e1)`
`sw $a0 0($sp)`
`addiu $sp $sp -4`
`cgen(e2)`
`lw $t1 4($sp)`
`sub $a0 $t1 $a0`
`addiu $sp $sp 4`

What is the difference between this and the code for `e1+e2`?

- New instruction: `sub reg1 reg2 reg3`

– Implements $\text{reg}_1 \leftarrow \text{reg}_2 - \text{reg}_3$

`cgen(e1 - e2) =`

`cgen(e1)`

`sw $a0 0($sp)`

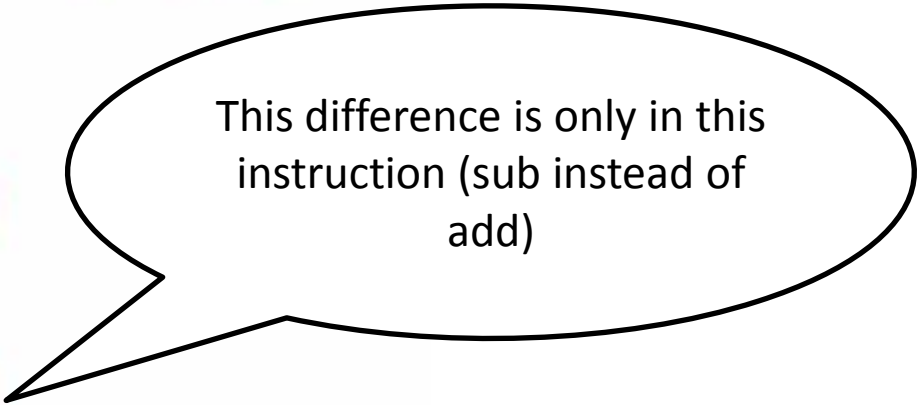
`addiu $sp $sp -4`

`cgen(e2)`

`lw $t1 4($sp)`

`sub $a0 $t1 $a0`

`addiu $sp $sp 4`



This difference is only in this instruction (sub instead of add)

To be able to generate code for **if expressions** we need two more MIPS instructions:

- New instruction: `beq reg1 reg2 label`
 - Branch to label if `reg1 = reg2`
- New instruction: `b label`
 - Unconditional jump to label

cgen(if $e_1 = e_2$ then e_3 else e_4) =

cgen(e_1)

sw $\$a0$ 0($\$sp$)

addiu $\$sp$ $\$sp$ -4

cgen(e_2)

lw $\$t1$ 4($\$sp$)

addiu $\$sp$ $\$sp$ 4

beq $\$a0$ $\$t1$ true_branch

false_branch:

cgen(e_4)

b end_if

true_branch:

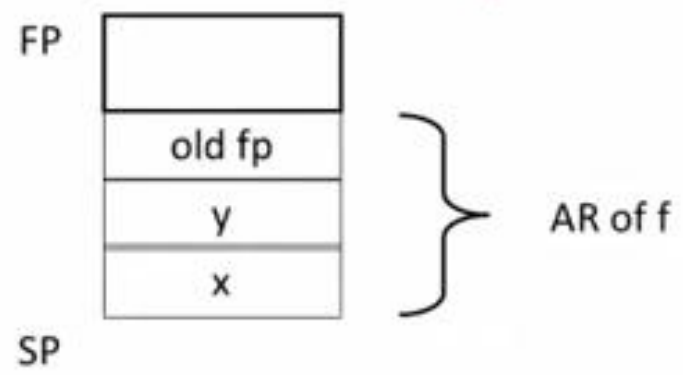
cgen(e_3)

end_if:

- Code for function calls and function definitions depends on the layout of the AR
- A very simple AR suffices for this language:
 - The result is always in the accumulator
 - No need to store the result in the AR
 - The activation record holds actual parameters
 - For $f(x_1, \dots, x_n)$ push x_n, \dots, x_1 on the stack
 - These are the only variables in this language

- The stack discipline guarantees that on function exit $\$sp$ is the same as it was on function entry
 - No need for a control link
- We need the return address
- A pointer to the current activation is useful
 - This pointer lives in register $\$fp$ (frame pointer)

- Summary: For this language, an AR with the caller's frame pointer, the actual parameters, and the return address suffices
- Picture: Consider a call to $f(x,y)$, the AR is:



- The calling sequence is the instructions (of both caller and callee) to set up a function invocation
- New instruction: `jal label`
 - Jump to label, save address of next instruction in `$ra`
 - On other architectures the return address is stored on the stack by the “call” instruction

The code that will execute on the Caller Side

```
cgen(f(e1,...,en)) =  
sw $fp 0($sp)  
addiu $sp $sp -4  
cgen(en)  
sw $a0 0($sp)  
addiu $sp $sp -4  
...  
cgen(e1)  
sw $a0 0($sp)  
addiu $sp $sp -4  
jal f_entry
```

The caller saves its value of the frame pointer

Then it saves the actual parameters in reverse order

Finally the caller saves the return address in register $\$ra$

The AR so far is $4*n+4$ bytes long

The code that will execute on the Callee Side

- New instruction: jr *reg*
 - Jump to address in register *reg*

cgen(def $f(x_1, \dots, x_n) = e$) =

Entry: *move* \$fp \$sp
sw \$ra 0(\$sp)
addiu \$sp \$sp -4
cgen(*e*)
lw \$ra 4(\$sp)
addiu \$sp \$sp *z*
lw \$fp 0(\$sp)
jr \$ra

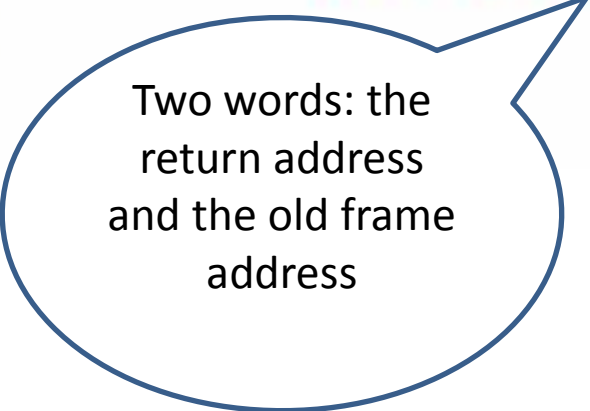
- New instruction: jr *reg*
 - Jump to address in register *reg*

cgen(def $f(x_1, \dots, x_n) = e$) =

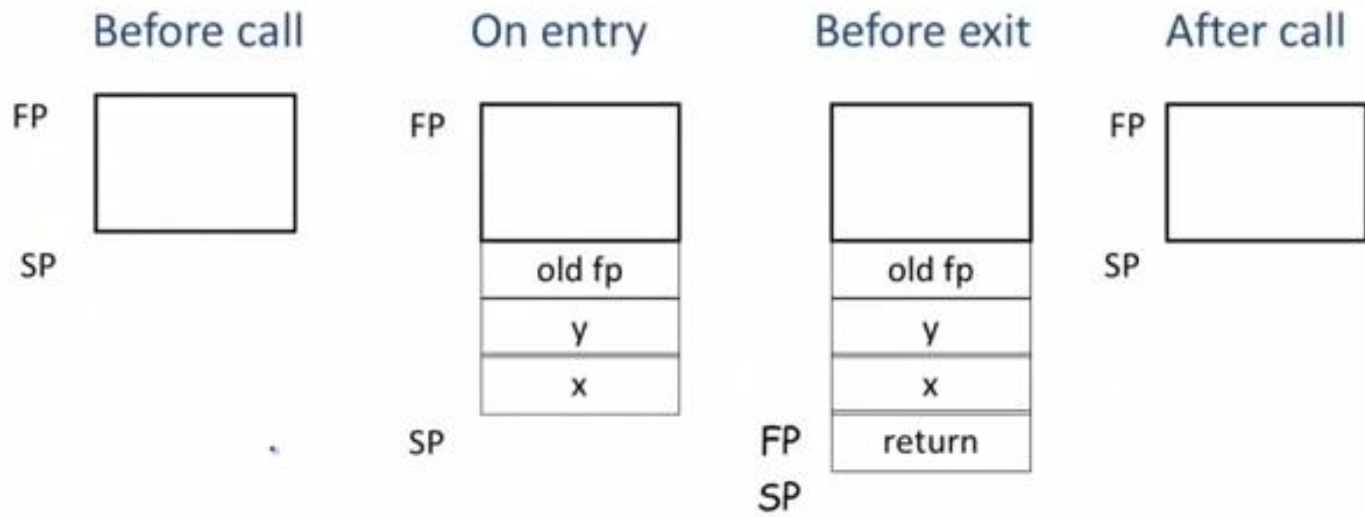
Entry: `move $fp $sp`
`sw $ra 0($sp)`
`addiu $sp $sp -4`
cgen(*e*)
`lw $ra 4($sp)`
`addiu $sp $sp z`
`lw $fp 0($sp)`
`jr $ra`

- Note: The frame pointer points to the top, not bottom of the frame
- The callee pops the return address, the actual arguments and the saved value of the frame pointer

- $z = 4 * n + 8$



Two words: the
return address
and the old frame
address



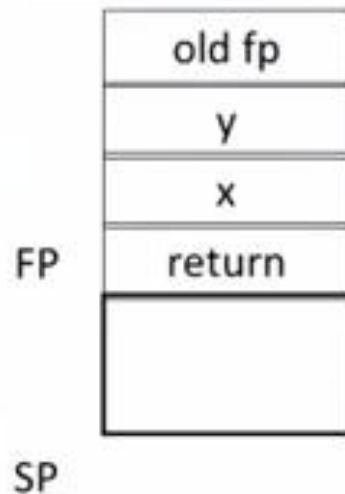
Generating Code for Reference Variables: i.e. generate code that determines their place in the activation record.

- Variable references are the last construct
- The “variables” of a function are just its parameters
 - They are all in the AR
 - Pushed by the caller
- Problem: Because the stack grows when intermediate results are saved, the variables are not at a fixed offset from $\$sp$

- Solution: use a frame pointer
 - Always points to the return address on the stack
 - Since it does not move it can be used to find the variables
- Let x_i be the i^{th} ($i = 1, \dots, n$) formal parameter of the function for which code is being generated

$$\text{cgen}(x_i) = \text{lw } \$a0 \text{ z}(\$fp) \quad (z = 4*i)$$

- Example: For a function `def f(x,y) = e` the activation and frame pointer are set up as follows:



- X is at $fp + 4$
- Y is at $fp + 8$

Code Generation Example

def sumto(X) = if x=0 then 0 else x+sumto(x-1)

Sumto_entry:

```
        move      $fp      $sp          % fp points to AR of sumto
        sw        $ra      0($sp)
        addiu     $sp      $sp    -4
        lw        $a0      4($fp)      //load x
        sw        $a0      0($sp)
        addiu     $sp      $sp    -4
        li        $a0      0          //code for 0
        lw        $t1      4($sp)      //pop x
        addiu     $sp      $sp    4
        beq       $a0      $t1    true1 //goto then part
```

false1:

false1:

```
lw      $a0      4($fp)      % x
sw      $a0      0($sp)
addiu   $sp      $sp -4
```

% call sumto(x-1) here we insert what happens at the caller side

% store old fp on the new activation record

```
sw      $fp      0($sp)
addiu   $sp      $sp -4
```

% compute x-1 and store it in the new AR

```
lw      $a0      4($fp)
sw      $a0      0($sp)
addiu   $sp      $sp -4
li      $a0      1          //code for 1
lw      $t1      4($sp)    // x
sub     $a0      $t1 $a0
addiu   $sp      0($sp)    //pop stack
```

%store x-1 in the new AR

```
sw      $a0      0($sp)
```

% jump to sumto(x-1)

```
                jal                Sumto_entry

% add X

                lw                 $t1                4($sp)           % x was stored in the stack
                                                    because it is part of the
                                                    expression x+sumto(x-1)

                add                $a0                $t1    $a0

                addiu               $sp                $sp    4        %pop x

                b                   endif

% the true part    0

true1:

                li                 $a0                0

% function ends so we return

endif:          lw                 $ra                4($sp)

% pop AR

                addiu               $sp                $sp    12

                lw                 $fp                0($sp)

% jump back to the caller

                jr                  $ra
```

Two Observations:

1. Although the code is correct it is extremely inefficient, notice that we load x from the stack (memory op) then immediately after that we store it back in the stack.
2. Temporary values are stored in the AR; a better alternative might be to store them in temporary registers.

Summary

- The activation record must be designed together with the code generator
- Code generation can be done by recursive traversal of the AST
- The stack model simplifies things.
- Production compilers do different things
 - Emphasis is on keeping values (esp. current stack frame) in registers
 - Intermediate results are laid out in the AR, not pushed and popped from the stack

An Improvement

- Idea: Keep temporaries in the AR
- The code generator must assign a fixed location in the AR for each temporary (this saves the need to keep pushing an popping them).

Example

```
def fib(x) = if x = 1 then 0 else  
            if x = 2 then 1 else  
              fib(x - 1) + fib(x - 2)
```

- What intermediate values are placed on the stack?
- How many slots are needed in the AR to hold these values? i.e. how many intermediate values are needed?

How Many Temporaries?

- Let $NT(e)$ = # of temps needed to evaluate e
- $NT(e_1 + e_2)$
 - Needs at least as many temporaries as $NT(e_1)$
 - Needs at least as many temporaries as $NT(e_2) + 1$
- Space used for temporaries in e_1 can be reused for temporaries in e_2

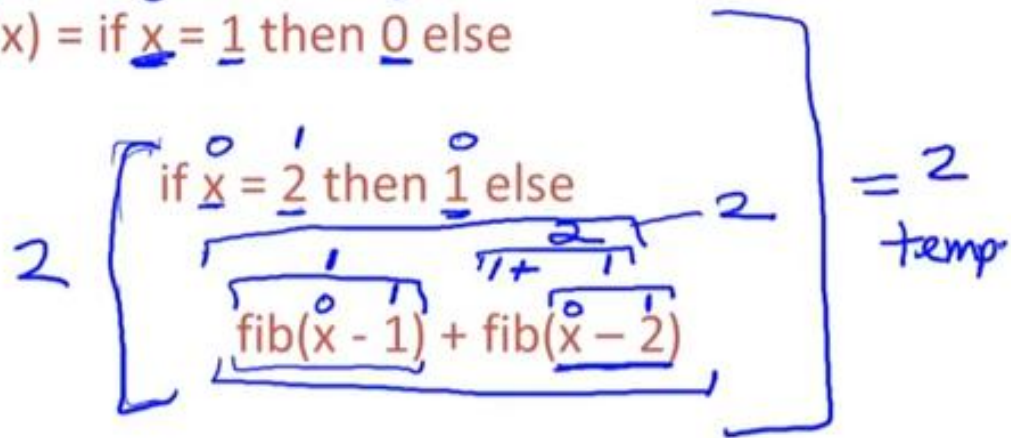
The Equations

- $NT(e_1 + e_2) = \max(NT(e_1), 1 + NT(e_2))$
- $NT(e_1 - e_2) = \max(NT(e_1), 1 + NT(e_2))$
- $NT(\text{if } e_1 = e_2 \text{ then } e_3 \text{ else } e_4) = \max(NT(e_1), 1 + NT(e_2), NT(e_3), NT(e_4))$
- $NT(\text{id}(e_1, \dots, e_n)) = \max(NT(e_1), \dots, NT(e_n))$
- $NT(\text{int}) = 0$
- $NT(\text{id}) = 0$

- What is NT(...code for fib...)?

- The answer is 2

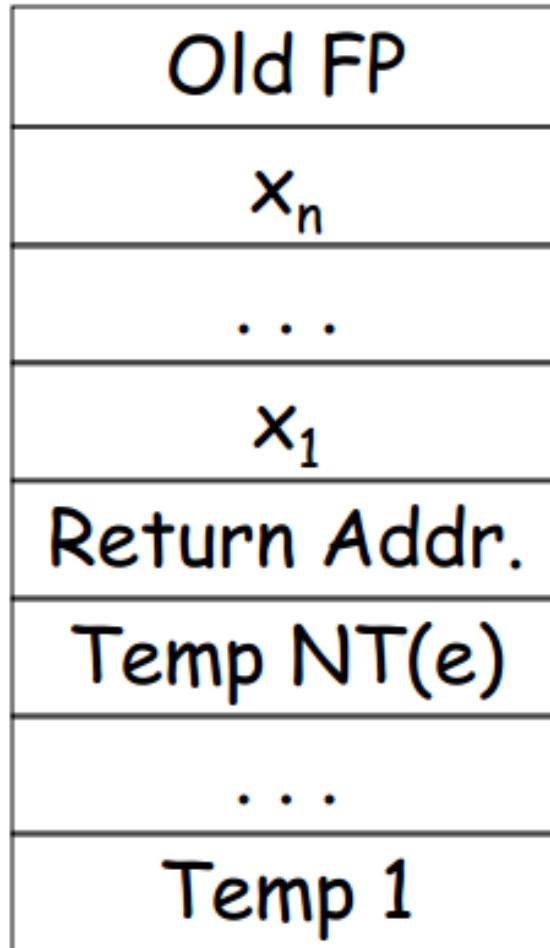
def fib(x) = if ⁰x = ¹1 then ⁰0 else



The Revised AR

- For a function definition $f(x_1, \dots, x_n) = e$ the AR has $2 + n + \text{NT}(e)$ elements
 - Return address
 - Frame pointer
 - n arguments
 - $\text{NT}(e)$ locations for intermediate results

Picture



Revised Code Generation

- Code generation must know how many temporaries are in use at each point
- Add a new argument to code generation: the position of the next available temporary

Code Generation for + (original)

$\text{cgen}(e_1 + e_2) =$

$\text{cgen}(e_1)$

`sw $a0 0($sp)`

`addiu $sp $sp -4`

$\text{cgen}(e_2)$

`lw $t1 4($sp)`

`add $a0 $t1 $a0`

`addiu $sp $sp 4`

Code Generation for + (revised)

```
cgen( $e_1 + e_2$ , nt) =  
    cgen( $e_1$ , nt)  
    sw $a0 nt($fp)  
    cgen( $e_2$ , nt + 4)  
    lw $t1 nt($fp)  
    add $a0 $t1 $a0
```

Notes

- Two sentences shorter and substantially more efficient.
- The temporary area is used like a small, fixed-size stack