



Contents lists available at SciVerse ScienceDirect

## Chemical Engineering Research and Design

journal homepage: [www.elsevier.com/locate/cherd](http://www.elsevier.com/locate/cherd)

# Compressibility factor model of sweet, sour, and condensate gases using genetic programming

Eissa M. El-M. Shokir<sup>a,b,\*</sup>, Musaed N. El-Awad<sup>a</sup>, Abdulrahman A. Al-Quraishi<sup>c</sup>, Osama A. Al-Mahdy<sup>a</sup>

<sup>a</sup> Petroleum and Natural Gas Engineering Department, College of Engineering, King Saud University, P.O. Box 800, Riyadh 11421, Saudi Arabia

<sup>b</sup> Mining, Petroleum, and Metallurgical Department, Faculty of Engineering, Cairo University, Egypt

<sup>c</sup> King Abdulaziz City for Science and Technology, Riyadh, Saudi Arabia

## A B S T R A C T

Gas compressibility factor (*z*-factor) is necessary in most petroleum engineering calculations. The most common sources of *z*-factor values are experimental measurements, equations of state (EOS) and empirical correlations. There are more than twenty correlations available with two variables for calculating the *z*-factor from fitting Standing-Katz chart values in an EOS or just through fitting techniques. However, these correlations are too complex, which require initial value and longer computations, and have significant error. This work presents a new model for estimating *z*-factors of sweet gases, sour gases and gas condensates using genetic programming (GP). The *z*-factor model was developed using pseudo-reduced pressure, and pseudo-reduced temperature. Moreover, two new models of pseudo-critical pressure and temperature were built as a function of the gas composition (mol percent of C<sub>1</sub>–C<sub>7+</sub>, H<sub>2</sub>S, CO<sub>2</sub>, and N<sub>2</sub>) and the specific gravity of the C<sub>7+</sub>. The developed new GP-based model yields a more accurate prediction of gas *z*-factor compared to the commonly used correlations and EOS's.

© 2011 The Institution of Chemical Engineers. Published by Elsevier B.V. All rights reserved.

**Keywords:** Gas compressibility factor; Sour gas; Condensate gas; Genetic programming

## 1. Introduction

In the oil and gas industries, gas compressibility factor (*z*-factor) is one of the most important parameters in upstream and downstream operations. The importance of *z*-factor cannot be overemphasized in material balance, gas reserve evaluation, gas reservoir simulation, gas well testing and gas processing calculations. Occasionally, experimental data is unavailable and estimation from EOS or empirical correlations becomes a necessity. The existing methods of calculating *z*-factor, at significant amounts of acid gases like carbon dioxide (CO<sub>2</sub>) and hydrogen sulfide (H<sub>2</sub>S), incur high deviation from the actual value. Consequently, searching for a simple and an accurate model for predicting the compressibility factors of sweet, sour, lean and rich gas condensate reservoirs becomes very important.

Therefore, in this paper a new model for estimating *z*-factors of sweet gases, sour gases, and lean to rich gas condensates using genetic programming is presented. The new model was designed to be simpler as it eliminates the numerous computations involved in any equation of state applications. The efficiency of the developed model was tested against the most commonly used gas compressibility correlations and EOS's. In addition, risk analysis was used to demonstrate the sensitivity of the new model and the dependency extent of the compressibility factor on each of the independent variables. The *z*-factor model was developed using pseudo-reduced pressure, and pseudo-reduced temperature. However, the pseudo-reduced pressure and temperature are defined based on pseudo-critical pressure and pseudo-critical temperature ( $P_{Pr} = P/P_{Pc}$  and  $T_{Pr} = T/T_{Pc}$ ), respectively. Therefore, these two

\* Corresponding author at: Petroleum and Natural Gas Engineering Department, College of Engineering, King Saud University, P.O. Box 800, Riyadh 11421, Saudi Arabia. Tel.: +966 14676882; fax: +966 14674422.

E-mail addresses: [shokir@ksu.edu.sa](mailto:shokir@ksu.edu.sa), [shokir05@yahoo.com](mailto:shokir05@yahoo.com) (E.M.E.-M. Shokir).

Received 4 April 2011; Received in revised form 10 October 2011; Accepted 10 October 2011  
0263-8762/\$ – see front matter © 2011 The Institution of Chemical Engineers. Published by Elsevier B.V. All rights reserved.  
doi:[10.1016/j.cherd.2011.10.006](https://doi.org/10.1016/j.cherd.2011.10.006)

**Nomenclature**

T	terminal set
F	genetic operator function
$T_{Pc}$	pseudo-critical temperature
$P_{Pc}$	pseudo-critical pressure
$T_{Pr}$	pseudo-reduced temperature
$P_{Pr}$	pseudo-reduced pressure
$zC_1$	mole percent of methane
$zC_2$	mole percent of ethane
$zC_3$	mole percent of propane
$zC_4$	mole percent of iso-butanes
$zC_5$	mole percent of <i>n</i> -butanes
$zC_6$	mole percent of iso-pentanes
$zC_7$	mole percent of <i>n</i> -pentanes
$zC_{7+}$	mole percent of hexanes
$zCO_2$	mole percent of heptanes-plus
$zH_2S$	mole percent of carbon dioxide
$zN_2$	mole percent of hydrogen sulfide
$SPG\ C_{7+}$	mole percent of nitrogen
AARE	specific gravity of heptanes-plus average absolute relative error, $100/N \sum_1^N  (y_{calculated} - y_{measured})/y_{measured} , \%$

parameters (pseudo-critical pressure and temperature) were modelled as a function of the gas composition (mol percent of  $C_1-C_{7+}$ ,  $H_2S$ ,  $CO_2$ , and  $N_2$ ) and the specific gravity of the  $C_{7+}$ .

A total of 1270 data points for a variety of natural gases, covering lean, sweet to rich and acid or sour gases ( $H_2S$ , and  $CO_2$ ), were collected from literature (Buxton and Campbell, 1967; Elsharkawy, 2002, 2004; Reamer et al., 1942, 1952, 1953; Reamer and Sage, 1962; Elsharkawy and Foda, 1998; Wichert, 1970; Simon et al., 1977) to develop a new predictive model of sweet gases, sour gases, and lean to rich gas condensates z-factors. These data include gas compositions (mol percent of  $C_1-C_{7+}$ ,  $H_2S$ ,  $CO_2$ , and  $N_2$ ), molecular weight and specific gravity of the  $C_{7+}$ , experimentally measured compressibility factors, pressures, temperatures. The corresponding pseudo-critical pressures and temperatures were calculated using mixing rule of Piper et al. (1993). Some points were discarded due to the lack of  $C_{7+}$  fraction properties (which is essential for establishing the new z-factor models). Finally, 1150 gas samples are randomly divided into two parts. The first part, contains 800 gas samples, was introduced for building the new models using genetic programming, and the second part (350 gas samples) was used for validating and testing the developed models against the other early published gas compressibility correlations and EOS's.

## 2. Gas compressibility factor

The ratio of the actual volume to the ideal volume of real gas "which is a measure of the amount the gas deviates from perfect behavior" is called the compressibility factor. It is also called the gas deviation factor and is denoted by the symbol  $z$ . The most common sources of  $z$ -factor values are experimental measurement, equations of state and empirical correlations. Scarcity of experimental data for the required composition, pressure, and temperature conditions arise the need for modelling. Several different correlations are available for this important parameter. The basic correlations use the corresponding states concept. The theory of

corresponding states dictates that the  $z$ -factor can be uniquely defined as a function of reduced pressure and reduced temperature. The reduced pressure and reduced temperature are defined as

$$P_r = \frac{P}{P_c} \quad (1)$$

$$T_r = \frac{T}{T_c} \quad (2)$$

where  $P_r$  and  $T_r$  are reduced pressure and reduced temperature, respectively, and  $P_c$  and  $T_c$  are critical pressure and critical temperature of the gas, respectively. The values of pseudo-critical pressure and pseudo-critical temperature can be estimated from the following equations if the composition of the gas and the critical properties of the individual components are known (Kay, 1936):

$$P_{Pc} = \sum_{i=1}^n P_{ci} y_i \quad (3)$$

$$T_{Pc} = \sum_{i=1}^n T_{ci} y_i \quad (4)$$

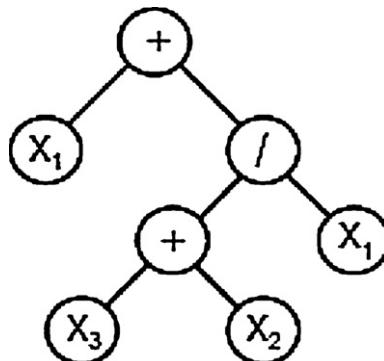
where  $P_{ci}$  and  $T_{ci}$  are the critical pressure and temperature of component  $i$ , respectively; and  $y_i$  is the mole fraction of component  $i$ .

For unknown composition of different gas systems, there are different correlations to predict pseudo-critical temperature and pressure from gas specific gravity like Standing (1981), Elsharkawy et al. (2001) and Sutton (2007). Standing and Katz (1942) developed an accepted chart (SKC) according to the theory of corresponding states for the  $z$ -factor. On the other hand, there are more than twenty correlations available with two variables for calculating the  $z$ -factor from fitting SKC values in an EOS as reported by Hall and Yarborough (1973), Dranchuk and Abou-Kassem (1975), Nishiumi and Saito (1975), Dranchuk et al. (1974), and Benedict et al. (1940) or just through fitting techniques like Gopal (1977). In addition, Brill and Beggs (1974) presented an explicit relation to estimate/predict the  $z$ -factor. They reported that 94 data points were used to establish this correlation, which yields an average absolute error of 0.19%. However, their correlation can only be used in the range of  $1.2 \leq T_{Pr} \leq 2.4$  and  $0 \leq P_{Pr} \leq 10$ .

The above mentioned correlations are complicated in a sense of initial value availability, longer computations and/or accompanied magnitude error. Therefore, the objective of this paper is to apply GP to generate a simplified new compressibility factor model of sweet, sour, lean and rich gas condensate reservoirs as a function of the pseudo-reduced pressure and pseudo-reduced temperature. Moreover, new pseudo-critical pressure and pseudo-critical temperature models were developed using GP as function of gas compositions (mol percent of  $C_1-C_{7+}$ ,  $H_2S$ ,  $CO_2$ , and  $N_2$ ) and the specific gravity of the  $C_{7+}$ .

## 3. Genetic programming

GP is a recent development in the field of evolutionary algorithms, which extends the classical genetic algorithms (Reeves, 1997; Shokir et al., 2004) to a symbolic optimization technique (Koza, 1992; Shokir, 2008). It is based on so-called "tree representation". This representation is extremely flexible, because trees can represent computer programs,



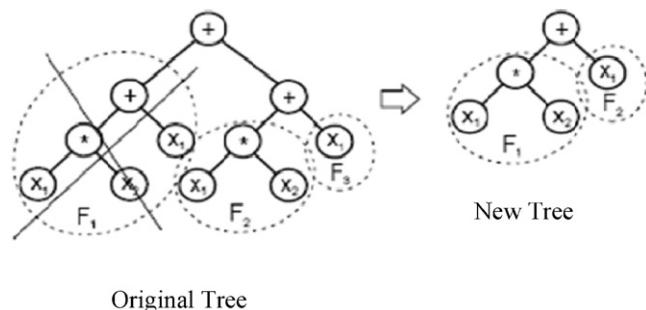
**Fig. 1 – A tree structure for the model (Madar et al., 2004):**  
 $y = x_1 + (x_3 + x_2)/x_1$ .

mathematical equations, or complete models of process systems. This scheme has been already used for circuit design in electronics and algorithm development for quantum computers and is suitable for generating model structures, e.g., identification of kinetic orders (Cao et al., 1999), steady-state models (McKay et al., 1997), and differential equations (Sakamoto and Iba, 2001). GP initially creates an initial population [i.e., it means generating individuals (trees) randomly to achieve high diversity]. In all iterations, the algorithm evaluates the individuals, selects individuals for reproduction, generates new individuals by mutation, crossover, and direct reproduction, and finally creates the new generation (Koza, 1992; Madar et al., 2004; Pearson, 2003; Potvin et al., 2004). Unlike common optimization methods, in which potential solutions are represented as numbers (usually vectors of real numbers), the symbolic optimization algorithms represent the potential solutions by structural ordering of several symbols, as shown in Fig. 1.

The generated potential solutions in the form of a tree structure during the GP operation may have better and worse terms (subtrees) that contribute more or less to the accuracy of the model represented by the tree structure. Using an orthogonal least squares (OLS) algorithm estimates the contribution of the branches of the tree to the accuracy of the model. Whereas, using the OLS, one can select the less significant terms in a linear regression problem. Terms having the smallest error reduction ratio could be eliminated from the tree (Pearson, 2003). Fig. 2 illustrates an example of elimination a sub-tree based on OLS. A complete explanation of the presentation of the mathematical model in GP and the OLS algorithm is found in Koza (1992) and Shokir (2008).

#### 4. Building the gp-based pseudo-critical pressure and temperature and z-factor models

As mentioned before the data set that was used in building the new pseudo-critical pressure, pseudo-critical temperature, and z-factor models is equal to 1150 gas samples. Eight hundred data points are randomly selected from the collected data for building the pseudo-critical pressure, pseudo-critical temperature, and gas factor models, and the remaining 350 data points put aside for testing the developed models. Table 1 summarizes the minimum and maximum values of all components in the collected gases. Table 2 shows the minimum and maximum values for the used data in building the new pseudo-critical pressure and temperature models. The maximum and minimum values of the different parameters



**Fig. 2 – Elimination a sub-tree based on OLS (Madar et al., 2004).**

constitute the limits of the developed model domains; extrapolation beyond these values could lead to unrealistic results.

The GP-OLS technique was applied to generate the new pseudo-critical pressure and pseudo-critical temperature models for sweet, sour, lean and rich condensate gas reservoirs, using Matlab software. On the basis of the input data, the GP identified the model equation. During the identification process, the function set  $F$  contained the basic arithmetic operations  $F = (+, -, \times, /)$  and the terminal set  $T$  contained repressor variables

$$T = zC_1 + \dots, zC_{7+}, zN_2 + zH_2S + zCO_2, SPG C_{7+} \quad (5)$$

The OLS evaluation is inserted into the fitness evaluation step. Before calculation of the fitness value of the tree, the OLS calculates the error reduction ratio of the branches of the tree, and the terms that have an error reduction ratio below a threshold value are eliminated from the tree. With the help of the selected branches, the OLS estimates the parameters of the model represented by the tree. After that, this new individual proceeds on its way in the GP algorithm (fitness evaluation, selection, etc.). Table 3 summarizes the final GP parameters that were used in building the new pseudo-critical pressure and temperature models.

The resulted new pseudo-critical temperature is:

$$T_{Pc} = A + B + C + D + E + F \quad (6)$$

where

$$\begin{aligned} A &= 0.90802((ziC_4 - ziC_4 ziC_5)(zC_3 + zH_2S + (znC_4 zCO_2))) \\ &\quad + 0.50786((zH_2S + zC_2)znC_4) \end{aligned}$$

$$\begin{aligned} B &= -2.123366(ziC_4(zH_2S + zC_2)) + 1.159927zC_3 - 2.071292zC_1 \\ &\quad - 69.070023(ziC_5 SPG C_{7+}^2) \end{aligned}$$

$$C = -2.996917zN_2 - 8.917447zC_{7+} + 21.072914ziC_4$$

$$- 1.422166SPG C_{7+} + 0.35641(znC_4 C_2)$$

$$\begin{aligned} D &= 3.83187(zC_6 zC_{7+}) - 3.81694znC_5 - 7.13966znC_4 \\ &\quad + 1.2344zH_2S + 13.2054(SP G C_{7+} zC_{7+}) \end{aligned}$$

$$\begin{aligned} E &= -0.308395(SP G C_{7+} zH_2S) - 0.012482(zN_2 zH_2S) \\ &\quad + 64.093536(SP G C_{7+} ziC_5) \end{aligned}$$

$$\begin{aligned} F &= 0.724091ziC_5 + 3.57128zC_6 - 1.47642(znC_4 ziC_5) \\ &\quad + 19.845762(ziC_4 znC_5) - 0.024106zCO_2 + 550.092621 \end{aligned}$$

**Table 1 – The minimum and maximum values of all components in the collected gases.**

	$C_1$ (mol%)	$C_2$ (mol%)	$C_3$ mol%	$i-C_4$ (mol%)	$n-C_4$ (mol%)	$i-C_5$ (mol%)	$n-C_5$ (mol%)	$C_6$ (mol%)	$C_{7+}$ (mol%)	$N_2$ (mol%)	$CO_2$ (mol%)	$H_2S$ (mol%)	SPG $C_{7+}$	Mw $C_{7+}$	T (°F)	P (psi)	$P_{Pc}$	$T_{Pc}$	z factor
Min.	17.3	0	0	0	0	0	0	0	0	0	0	0	0	0	39	150	640	345	0.456
Max.	97.5	28.67	13.16	1.07	1.8	1.59	0.79	1.31	6.18	25.15	54.5	73.85	0.91	150	299	7040	1170	602	1.361

**Table 2 – The minimum and maximum values for the used data in building the new pseudo-critical pressure and temperature models.**

	$C_1$ (mol%)	$C_2$ (mol%)	$C_3$ (mol%)	$i-C_4$ (mol%)	$n-C_4$ (mol%)	$i-C_5$ (mol%)	$n-C_5$ (mol%)	$C_6$ (mol%)	$C_{7+}$ (mol%)	$N_2$ (mol%)	$CO_2$ (mol%)	$H_2S$ (mol%)	SPG $C_{7+}$	T (°F)	P (psi)	$P_{Pc}$	$T_{Pc}$
Min.	17.27	0	0	0	0	0	0	0	0	0	0	0	0	39	150	640	345
Max.	97.48	28.67	13.16	1.07	1.8	1.59	0.79	1.31	6.18	25.15	54.46	73.85	0.91	299	7040	1170	602

**Table 3 – GP parameters used in building the new pseudo-critical pressure and temperature models.**

Population size	160
Maximum generation	250
Type of selection	Tournament <sup>a</sup>
Type of mutation	Point-mutation
Type of crossover	One-point (2 parents)
Type of replacement	Elitist <sup>b</sup>
Generation gap ( $P_{gap}$ parameter) <sup>b</sup>	0.8
Probability of crossover	0.7
Probability of mutation	0.4
Probability of changing terminal – non-terminal nodes (vica versa) during mutation	0.25
Maximum tree depth	7

<sup>a</sup> This method chooses each parent by randomly drawing a number of individuals from the population and selecting only the best of them.

<sup>b</sup> Before new individuals inserted to the population, it is necessary to ‘kill’ the old individuals. Elitist replacement strategy was applied in order to keep the best solutions with a ‘generation gap’  $P_{gap}$  parameter. E.g., the  $P_{gap} = 0.8$  means that 80% of population is ‘killed’ and the only the best 20% will survive.

**Table 5 – GP parameters Used in building the new z-factor model.**

Population size	110
Maximum generation	350
Type of selection	Tournament <sup>a</sup>
Type of mutation	Point-mutation
Type of crossover	One-point (2 parents)
Type of replacement	Elitist <sup>b</sup>
Generation gap ( $P_{gap}$ parameter) <sup>b</sup>	0.8
Probability of crossover	0.8
Probability of mutation	0.7
Probability of changing terminal – non-terminal nodes (vica versa) during mutation	0.25
Maximum tree depth	6

<sup>a</sup> This method chooses each parent by randomly drawing a number of individuals from the population and selecting only the best of them.

<sup>b</sup> Before new individuals inserted to the population, it is necessary to ‘kill’ the old individuals. Elitist replacement strategy was applied in order to keep the best solutions with a ‘generation gap’  $P_{gap}$  parameter. E.g., the  $P_{gap} = 0.8$  means that 80% of population is ‘killed’ and the only the best 20% will survive.

**Table 4 – The minimum and maximum values for the used data in building the new z-factor model.**

	$T_{Pr}$ (mol%)	$P_{Pr}$ (mol%)	z-Factor
Min.	1.967	0.17	0.456
Max.	0.974	10.2	1.361

The resulted new pseudo-critical pressure is:

$$P_{Pr} = A + B + C + D + E + F \quad (7)$$

where

$$A = 0.007417((zCO_2 + ziC_5) + 2zH_2S)(zC_1(zC_{7+} - SPG\ C_{7+}))$$

$$B = -1.15556((zH_2S(znC_5 + ziC_5))((znC_6SPG\ C_{7+}) + SPG\ C_{7+}))$$

$$C = 2.5781((znC_5 + zC_{7+}) - (zCO_2zC_6)) - 2.3518zCO_2$$

$$- 5.9904zC_2 - 16.0772znC_4 + 0.05118(zN_2 + znC_4)(H_2S + znC_5)$$

$$D = -8.30318zN_2 - 0.16079(zH_2SzCO_2SPG\ C_{7+}) - 1.01137ziC_4 \\ + 13.5415(SPG\ C_{7+}ziC_4)$$

$$E = -6.39055zC_1 + 22.30057(SPG\ C_{7+}ziC_5) \\ - 50.32981(zC_{7+} - SPG\ C_{7+}) - 1.90345(zH_2SzC_6)$$

$$F = -6.90457zC_3 - 0.54279(zC_1SPG\ C_{7+}) + 24.59715zC_{7+} \\ + 8.27392zC_6 + 0.303324znC_5 - 9.24827ziC_5 + 1306.82706$$

The developed GP-based pseudo-critical pressure and pseudo-critical temperature models were used to calculate the pseudo-reduced pressure and pseudo-reduced temperature for each gas samples which used for building the new GP-based gas z-factor model. The minimum and maximum values for the used data in building the new z-factor model are shown in Table 4. The above mentioned procedures of GP-OLS

were used in developing the new z-factor model. Table 5 summarizes the final GP parameters that were used in building the new z-factor model.

The resulted new z-factor model is:

$$z\text{-factor} = A + B + C + D + E \quad (8)$$

where

$$A = 2.679562 \frac{(2T_{Pr} - P_{Pr} - 1)}{[(P_{Pr}^2 + T_{Pr}^3)/P_{Pr}]}$$

$$B = -7.686825 \left[ \frac{P_{Pr}T_{Pr} + P_{Pr}^2}{T_{Pr}P_{Pr} + 2T_{Pr}^2 + T_{Pr}^3} \right]$$

$$C = -0.000624(T_{Pr}^2P_{Pr} - T_{Pr}P_{Pr}^2 + T_{Pr}P_{Pr}^3 + 2T_{Pr}P_{Pr} - 2P_{Pr}^2 + 2P_{Pr}^3)$$

$$D = 3.067747 \frac{(T_{Pr} - P_{Pr})}{(P_{Pr}^2 + T_{Pr} + P_{Pr})}$$

$$E = \left[ \frac{0.068059}{T_{Pr}P_{Pr}} \right] + 0.139489T_{Pr}^2 + 0.081873P_{Pr}^2 - \left[ \frac{0.041098T_{Pr}}{P_{Pr}} \right] \\ + \left[ \frac{8.152325P_{Pr}}{T_{Pr}} \right] - 1.63028P_{Pr} + 0.24287T_{Pr} - 2.64988$$

#### 4.1. Validation of the new Gp-based models

To validate the new pseudo-critical pressure and temperature models, the randomly stored 350 points from the original database were used for that propose. The minimum and maximum values for these test data parameters are shown in Table 6. The results of the new pseudo-critical pressure and temperature models show a good accuracy as well as a low average absolute relative error (AARE) equals to 0.04% and 0.03%, respectively (Figs. 3 and 4).

On the other hand, the performance and the accuracy of the developed GP-based model to predict the z-factors for sweet gases, sour gases, and lean to rich gas condensates were tested and validated by comparing the predicted z-factor with those

	$C_1$ (mol%)	$C_2$ (mol%)	$C_3$ (mol%)	$i-C_4$ (mol%)	$n-C_4$ (mol%)	$i-C_5$ (mol%)	$n-C_5$ (mol%)	$C_6$ (mol%)	$C_{7+}$ (mol%)	$N_2$ (mol%)	$H_2S$ (mol%)	SPG $C_{7+}$	$T_p^c$	$P$ (psi)	$T$ (°F)	$T$ (°C)	$Z$ factor
Min.	20.2	0	0	0	0	0	0	0	0	0	0	0	640	154	345	0.48	
Max.	97.48	28.67	13.16	1.07	1.8	1.59	0.79	1.31	6.18	25.15	54.46	70.03	1170	7026	602	1.28	

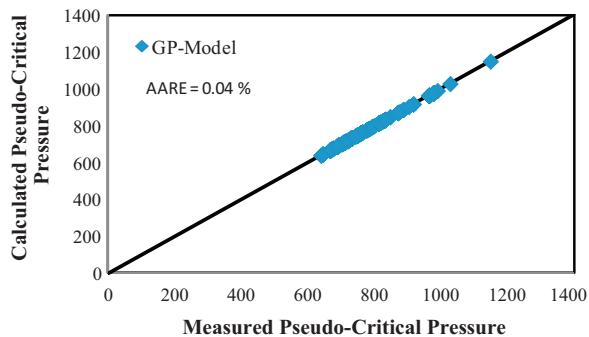


Fig. 3 – Cross plot of the predicted pseudo-critical pressures from the new GP-based model versus the calculated values from Piper et al. (1993) correlation.

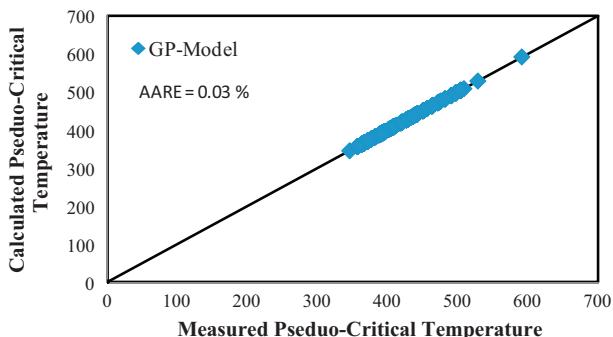


Fig. 4 – Cross plot of the predicted pseudo-critical temperature from the new GP-based model versus the calculated values from Piper et al. (1993) correlation.

predicted from the early published correlations (Elsharkawy, 2004; Dranchuk and Abou-Kassem, 1975; Hall and Yarborough, 1973; Gopal, 1977; Brill and Beggs, 1974; Dranchuk et al., 1974), and EOS's (Lawal et al. (LLS-EOS), 1985; Peng and Robinson (PR-EOS), 1976; Redlich and Kwong (RK-EOS), 1949). Cross-plot of the predicted z-factor values from the GP-based model versus the experimental values is shown in Fig. 5. This cross-plot shows the degree of agreement between the experimentally measured data and the predicted z-factor values. The new z-factor model yields the closest match between the predicted and the measured z-factor. It is clear from Table 7 that the new GP-based model presented in this study for calculating gas compressibility factor has the smallest average relative errors (ARE), smallest average absolute relative errors (AAARE), and the highest coefficient of correlations (COC) for all types of natural gases considered. Table 7 also indicates that the new

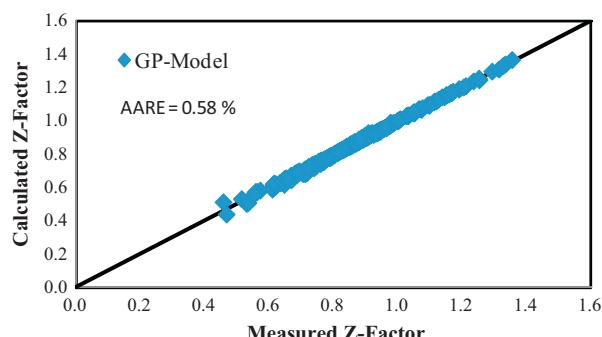
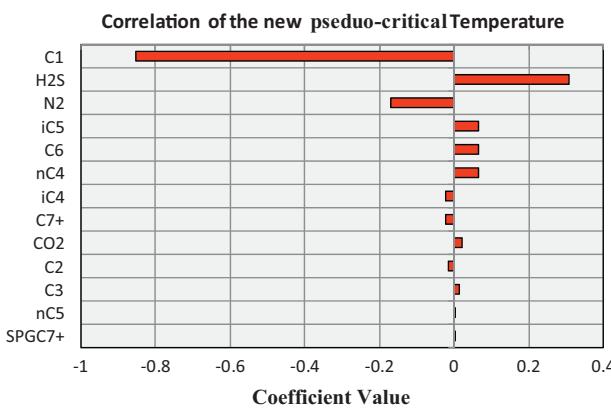


Fig. 5 – The predicted z-factor values from the new GP-based model versus and the experimental measured values.

**Table 7 – Comparison between the accuracy of different methods in predicting the gas compressibility factors of different types of natural gases.**

	ARE (%)	AARE (%)	COC (%)
GP-based model	-0.02	0.58	99.88
Elsharkawy (2004)	-0.57	2.34	95.14
Gopal (1977)	5.15	5.22	89.55
Dranchuk and Abou-Kassem (1975)	-3.34	4.53	90.19
Dranchuk et al. (1974)	4.50	4.63	90.04
Brill and Beggs (1974)	4.70	4.79	88.80
Hall and Yarborough (1973)	1.62	3.66	97.09
Lawal et al. (1985)	4.33	4.33	94.15
Peng and Robinson (PR-EOS) (1976)	-5.03	5.77	95.02
Redlich and Kwong (RK-EOS) (1949)	2.20	2.77	95.53

**Fig. 6 – Sensitivity analysis of the new pseudo-critical temperature model and its dependence on each independent variable.**

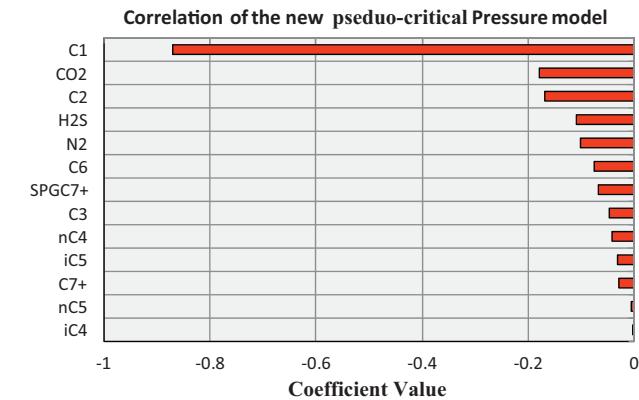
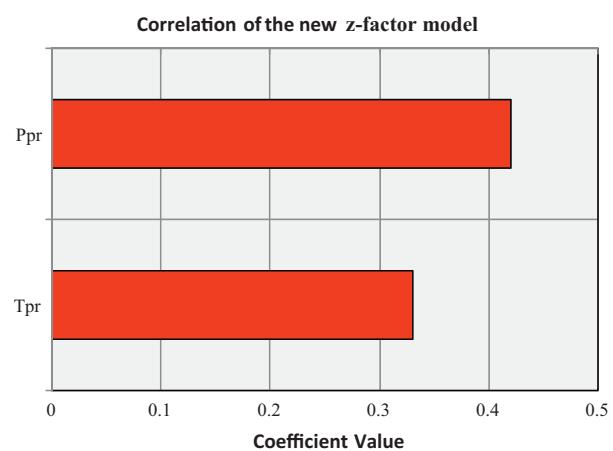
method shows superiority over all the correlations and EOS(s) considered in this study.

## 5. Sensitivity analysis

The influence of the individual independent variables on the new pseudo-critical pressure and temperature, and z-factor models were tested using MonteCarlo simulation software (@risk, 2008). This software was used to demonstrate the effect of all input variables on the depended predicted variable of each model. Figs. 6–8 show the results of sensitivity analysis of the new pseudo-critical pressure and temperature, and z-factor models. These figures show the rank correlation coefficients that were calculated between the output variable and the samples for each of the input parameters. In general, as the correlation coefficient between any input variable and output variable increases, the influence of that input in determining the output's value increases.

These figures indicate the following:

- From Figs. 6 and 7, it is obvious that the mole percent of  $C_1$  component has the major impact on both the pseudo-critical pressure and temperature. The pseudo-critical pressure and temperature decreases as a function of increasing mole percent of  $C_1$ . Decreasing the pseudo-critical temperature with increasing mole percent of  $C_1$  may be attributed to negative value of the pseudo-critical

**Fig. 7 – Sensitivity analysis of the new pseudo-critical pressure model and its dependence on each independent variable.****Fig. 8 – Sensitivity analysis of the new z-factor model and its dependence on each independent variable.**

temperature of the pure  $C_1$  and also the higher percent of this component in the gas mixture. On the other hand, decreasing the pseudo-critical pressure with increasing mole percent of  $C_1$  may be attributed to the higher compressibility of the  $C_1$  component.

- Fig. 6 also shows that pseudo-critical temperature decreases significantly if the mole percent of  $N_2$  increases. This observation is also attributed to the higher negative value of the pseudo-critical temperature of the pure  $N_2$  component. On the other hand, the results of sensitivity analysis of the new z-factor model are shown in Fig. 8. It shows that the z-factor increases with increasing the pseudo-reduced pressure and temperature. Fig. 6 also shows that pseudo-critical temperature decreases significantly if the mole percent of  $H_2S$  increases. This observation is also attributed to the higher negative value of the pseudo-critical temperature of the pure  $N_2$  component.
- Fig. 8 shows that the z-factor increases with increasing the pseudo-reduced pressure and pressure temperature.

## 6. Conclusions

- New models of the compressibility factor and pseudo-critical pressure and temperature for sweet gases, sour gases, and gas condensates were developed using genetic programming.

2. The comparison between the new GP-based model of the gas compressibility factor and the early published correlations and EOS's of the compressibility factor indicated that the new model is more accurate than the other tested correlations and EOS's. Therefore, the new model can be considered an alternative method to estimate the compressibility factor of lean and rich gas condensates, sweet gases, and sour gases, when the experimentally measurement is not available.
3. Sensitivity analysis using MonteCarlo simulation was used to examine the impact of different parameters on the predicted gas compressibility factor and pseudo-critical pressure and temperature for lean and rich gas condensates, sweet gases, and sour gases. The results were matched with the physical interrelationship between the input and output variables.

## Acknowledgments

The authors would like to acknowledge the Deanship of Scientific Research, Saudi National Plan for Sciences and technology, King Saud University and King AbdulAziz City for Science and Technology for providing the financial support for this work under Research Grant No. ENE341.

## References

- @risk, 2008. Risk Analysis and Simulation Add-in for Microsoft Excel V 5. Palisade Corporation.
- Benedict, M., Webb, G.B., Rubin, L.C., 1940. An empirical equation for thermodynamic properties of light hydrocarbons and their mixtures: I. methane, ethane, propane, and *n*-butane. *J. Chem. Phys.* 8 (4), 334–345.
- Brill, J.P., Beggs, H.D., 1974. Two-Phase Flow in Pipes. INTERCOMP Course, The Huge.
- Buxton, T.S., Campbell, J.M., 1967. Compressibility factors for naturally occurring petroleum gases. *SPEJ* 3, 80–86.
- Cao, H., Yu, J., Kang, L., Chen, Y., 1999. The kinetic evolutionary modelling of complex systems of chemical reactions. *Comput. Chem. Eng. J.* 23, 143–151.
- Dranchuk, P.M., Abou-Kassem, J.H., 1975. Calculation of Z factors for natural gases using equations of state. *JCP* 14 (3), 34–36.
- Dranchuk, P.M., Purvis, R.A., Robinson, D.B., 1974. Computer calculation of natural gas compressibility factors using the Standing and Katz correlation. *Inst. Petrol. Technol. (Pap. IP 74-008)*.
- Elsharkawy, A.M., 2002. Predicting the properties of sour gases and condensates: equations of state and empirical correlations. In: Paper SPE 74369 Presented at the Society of Petroleum Engineer International Petroleum Conferences and Exhibition, Villahermosa.
- Elsharkawy, A.M., 2004. Efficient methods for calculations of compressibility, density and viscosity of natural gases. *J. Fluid Phase Equilib.* 218, 1–13.
- Elsharkawy, A.M., Foda, S.G., 1998. EOS simulation and GRNN modeling of the constant volume depletion behavior of gas condensate reservoirs. *Energy Fuels J.* 12 (2), 353–364.
- Elsharkawy, A.M., Hashim, Y.S.K., Alikhan, A.A., 2001. Compressibility factor for gas condensates. *Energy Fuels J.* 15 (4), 807–816.
- Gopal, V.N., 1977. Gas z-factor equations developed for computer. *Oil Gas J.* 75, 58.
- Hall, K.R., Yarborough, L., 1973. A new EOS for z-factor calculations. *Oil Gas J.*, 82.
- Kay, W.B., 1936. Density of hydrocarbon gases and vapors at high temperature and pressure. *Ind. Eng. Chem.* 28, 1014–1019.
- Koza, J.R., 1992. Genetic Programming: On the programming of Computers by Means of Natural Evolution. MIT Press, Cambridge, MA.
- Lawal, A.S., van der Laan, E.T., Thambbynayagam, R.K.M., 1985. Four-parameter modification of the Lawal–Lake–Silberberg equation of state for calculating gas-condensate phase equilibria. In: Paper SPE 14269 Presented at the Society of Petroleum Engineer Annual Technical Conference, Las Vegas, September 22–25.
- Madar, J., Abonyi, J., Szeifert, F., 2004. Genetic programming for system identification. In: Intelligent Systems Design and Applications (ISDA 2004) Conference, Budapest, Hungary.
- McKay, B., Willis, M., Barton, G., 1997. Steady-state modelling of chemical process systems using genetic programming. *Comput. Chem. Eng. J.* 21, 981–996.
- Nishiumi, H., Saito, S., 1975. An improved generalized BWR equation of state applicable to low reduced temperature. *J. Chem. Eng. Jpn.* 8 (5), 356–360.
- Pearson, R., 2003. Selecting nonlinear model structures for computer control. *J. Process Control* 13, 1–26.
- Peng, D.Y., Robinson, D.B., 1976. A new two constants equation of state. *Ind. Eng. Chem. Fund. J.* 15, 59.
- Piper, L.D., McCain Jr., Corredor, J.H., 1993. Compressibility factors for naturally occurring petroleum gases. In: Paper SPE 26668, Presented at the Society of Petroleum Engineer International Petroleum Conferences and Exhibition, Houston, TX, October 3–6.
- Potvin, J-Y., Soriano, P., Vallee, M., 2004. Generating trading rules on the stock markets with genetic programming. *Comput. Oper. Res. J.* 31, 1033–1047.
- Reamer, H.H., Sage, B.H., 1962. Phase equilibria in hydrocarbon systems: volumetric and phase behavior of the ethane-*n*-decane system. *Ind. Eng. Chem. J.* 7 (2), 161–165.
- Reamer, H.H., Olds, R.H., Sage, B.H., Lacey, W.N., 1942. Phase equilibria in hydrocarbon systems-37: methane-decane system. *Ind. Eng. Chem. J.* 34 (12), 1526–1531.
- Reamer, H.H., Selleck, F.T., Sage, B.H., Lacey, W.N., 1952. Phase equilibria in hydrocarbon systems-57: volumetric behavior of the ethane–nitrogen system. *Ind. Eng. Chem. J.* 44 (1), 198–201.
- Reamer, H.H., Selleck, F.T., Sage, B.H., Lacey, W.N., 1953. Phase equilibria in hydrocarbon systems-60: volumetric and phase behavior of decane–hydrogen sulfide system. *Ind. Eng. Chem. J.* 45 (8), 1810–1812.
- Redlich, O., Kwong, J., 1949. On the thermodynamics of solutions. An equation of state. *Fugacities of gaseous solutions. Chem. Rev. J.* 44, 233.
- Reeves, C.R., 1997. Genetic algorithm for the operations research. *Informs J. Comput.* 9, 231–250.
- Sakamoto, E., Iba, H., 2001. Inferring a system of differential equations for a gene regulatory network by using genetic programming. In: Proceedings of the 2001 Congress on Evolutionary Computation CEC2001. IEEE Press, COEX, World Trade Center, pp. 720–726.
- Shokir, E.M.El.-M., 2008. Dew point pressure model for gas condensate reservoirs based on genetic programming. *Energy Fuels J.* 22, 3194–3200.
- Shokir, E.M.El-M., Emera, M.K., Eid, S.M., Abd Wally, A.A.W., 2004. A new optimization model For 3D well design. *Oil Gas Sci. Technol. J.* 59, 255–256.
- Simon, R., Fesmire, C.J., Dicharry, R.M., Vorhis, F.H., 1977. Compressibility factors for CO<sub>2</sub>–methane mixtures. *JPT* 5052, 81–85.
- Standing, M.B., 1981. Volumetric and Phase Behaviour of Oil Field Hydrocarbon Systems. Society of Petroleum Engineers of AIME, Dallas, TX.
- Standing, M.B., Katz, D.L., 1942. Density of natural gases. *Trans. AIME* 146, 140–149.
- Sutton, R.P., 2007. Fundamental PVT calculations for associated and gas/condensate natural-gas systems. *SPERE* J. 10 (3), 270–284.
- Wichert, E., 1970. Compressibility of Sour Natural Gases. MS Thesis, University of Calgary, Alberta.