

Integration By Substitution

Math 106

Lecture 6

Dr. Nasser Bin Turki

King Saud University
Department of Mathematics

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$$\int f(g(x))g'(x)dx = F(g(x)) + c, \quad \forall x \in [a, b].$$

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Remarks: If we use the Integration By Substitution in the definite Integration we need to look at the new function in terms of limits of the integration.

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- (3) $\int_1^3 \frac{10x-7}{4+5x^2-7x} dx$?

Thanks for listening.