

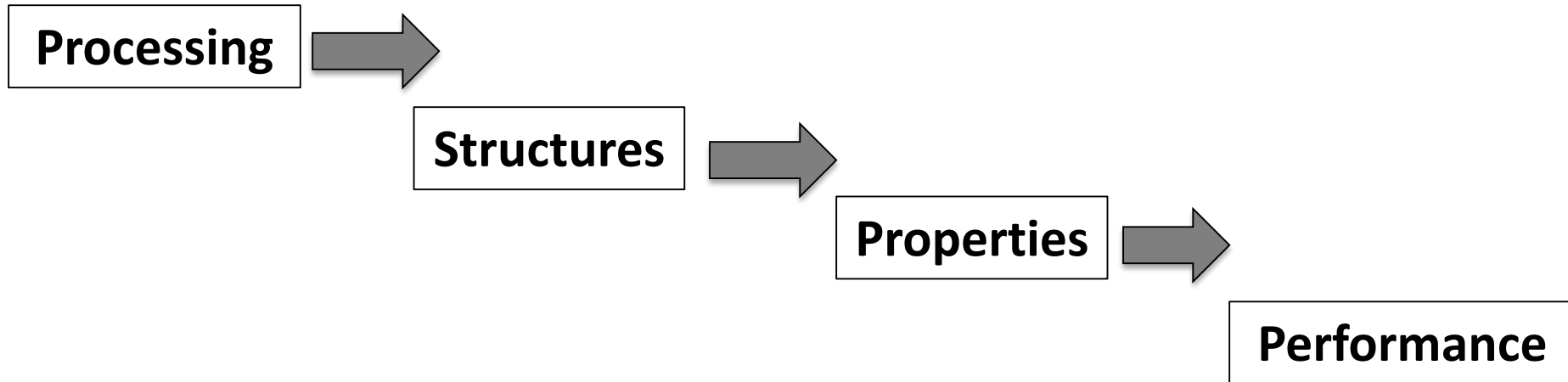
Review

Chapter 1

Introduction

Chapter 1: Summary

1) Materials Science and Engineering



2) Classification of Materials

(metals, ceramic, polymers, etc)

Classification of Materials

Metals:

Composed of one or more metallic elements, Fe, Cu, Al (& often small amounts of nonmetallic elements, O₂, N₂, C)

Ceramic

Compounds between metallic and nonmetallic elements (usually oxides, nitrides, carbides). Al₂O₃, SiC, glass, etc

Polymers

Plastic and rubbers (mainly based on carbon, hydrogen, and other nonmetallic elements).

Composites

Composed of two or more of the above classes (fiberglass, carbonfiber)

Advanced materials *(for high-tech applications)*

e.g. semiconductor, biomaterials, nano-materials, etc

Chapter 2

Atomic Structure and Interatomic Bonding

Atom

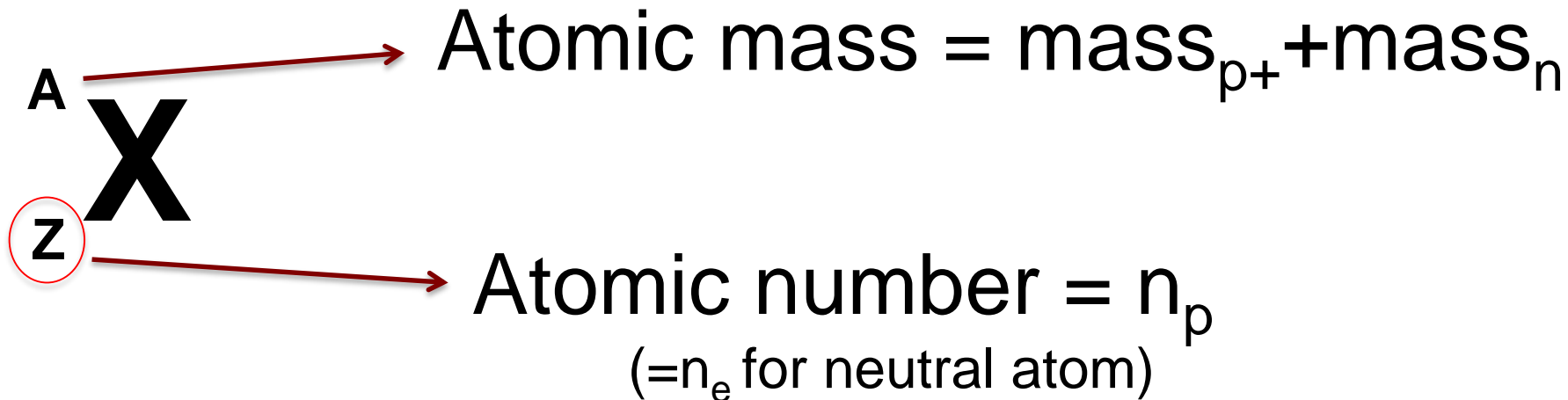
Nucleus

Proton (p^+) & neutron (n^0)

$1.6 \times 10^{-9} \text{ C}$
 $1.673 \times 10^{-27} \text{ kg}$

Electron (e^-)

$-1.6 \times 10^{-9} \text{ C}$
 $9.11 \times 10^{-31} \text{ kg}$



Review (from Chapter 2)

How do you calculate:

N_{moles} : # of moles

N_{atoms} : # of atoms

Remember that you need N_{atoms} to calculate the equilibrium number of vacancies, $N_v = N \exp(Q_v/kT)$.

Given:

Atomic weight, A (g/mole)

Avogadro number, N_{av} (atoms/mole)

Mass, M (g) or density, d (g/cm³)

- ❑ Atomic weight, A (g/mole)
- ❑ Avogadro number, N_{av} (atoms/mole)
- ❑ Mass, M (g) or density, d (g/cm³)

1 mole -----> A (g/mole)
 N_{moles} -----> M (g)

➔ $N_{\text{moles}} = M / A$

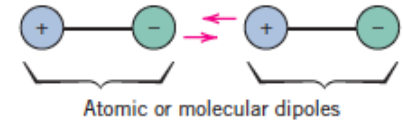
1 mole -----> N_{av} (atoms/mole)
 N_{moles} -----> N_{atoms}

➔ $N_{\text{atoms}} = N_{av} * N_{\text{moles}}$ ➔ $N_{\text{atoms}} = N_{av} M / A$

Atomic Bonds

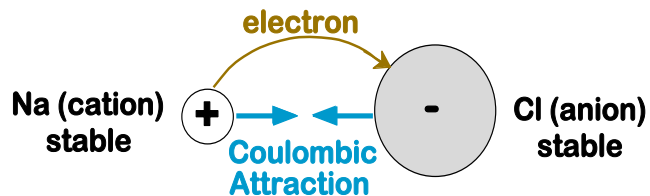
Primary interatomic bonds

Secondary, van der Waals, or physical bonds



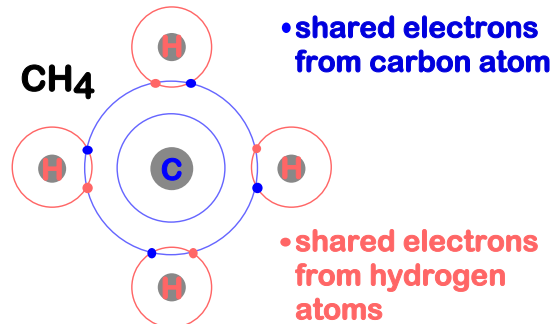
Ionic bonding

Atoms give up their valence electrons to other atoms



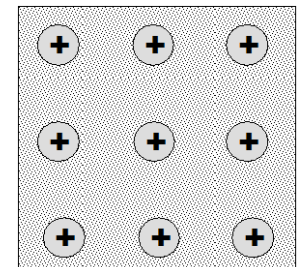
Covalent bonding

share electrons between adjacent atoms



Metallic bonding

Arises from a sea of donated valence electrons



Chapter 3

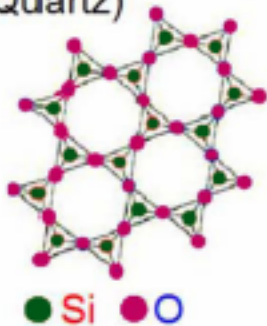
The Structure of Crystalline Solids

- ❑ Crystalline vs. non-crystalline materials
- ❑ Crystal structure, crystal system, lattice, unit cell, lattice parameters
- ❑ SC, BCC, FCC, HCP
 - Close packed direction
 - Coordination # (Z)
 - # of atoms/unit cell
 - APF

- ❑ Theoretical Density
- ❑ Single crystal vs. polycrystalline materials
- ❑ Point coordinates
- ❑ **Crystal direction**
- ❑ **Crystal planes**
- ❑ Linear density, $LD_{[xxx]}$
- ❑ Planar density, $PD_{(xxx)}$

Atomic arrangement

Crystalline SiO₂
(Quartz)

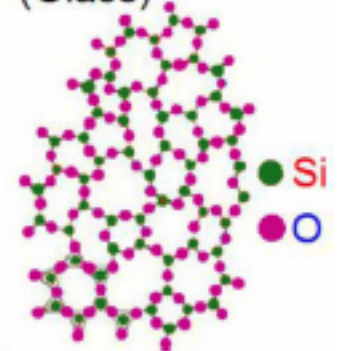


Solid

Crystalline

Amorphous

Amorphous SiO₂
(Glass)

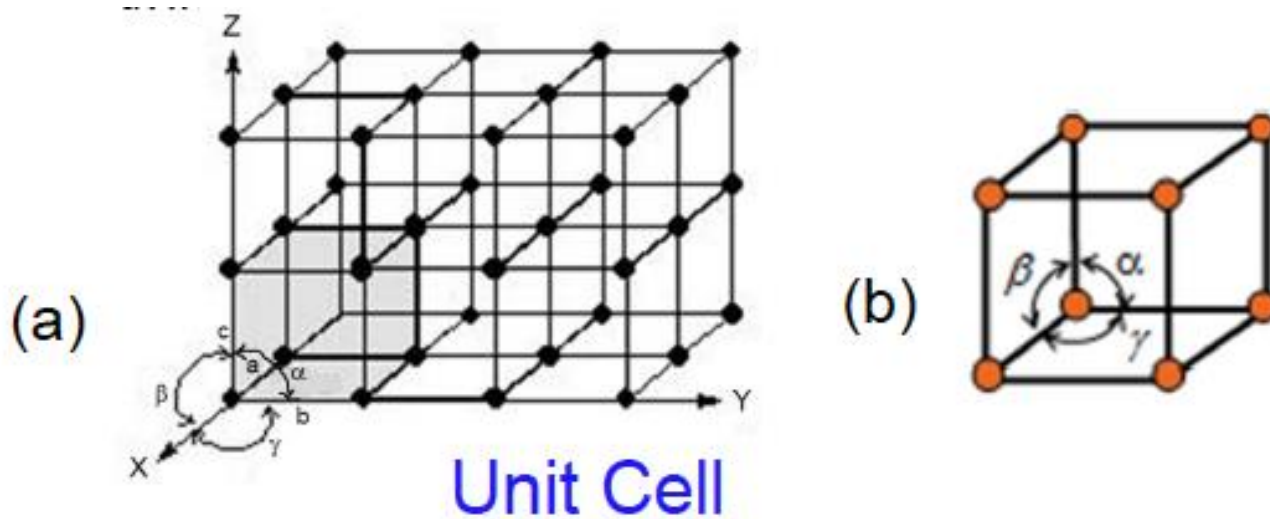


Crystalline – periodic arrangement of atoms: definite repetitive pattern

Non-crystalline or **Amorphous** – random arrangement of atoms.

Crystal structure

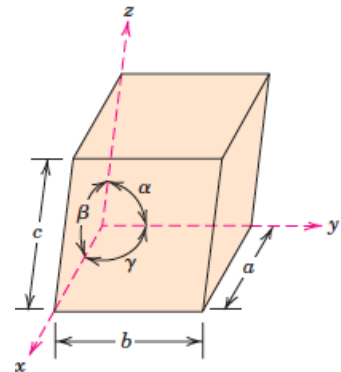
Crystal structure: spatial arrangement of atoms



Lattice: 3D array of points coinciding with atom positions (*hard sphere model*)

Unit cell: The basic structural unit of a crystal structure

Crystal system: defined based on the geometry of a unit cell (lattice parameters: a , b , c , α , β , γ)



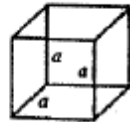
Crystal structure

- **7 Crystal systems** ← 7 unique “**shapes**” of unit cells

Shape of unit cell → 7 Crystal Systems

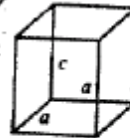
Cubic

$$a = b = c, \alpha = \beta = \gamma = 90^\circ$$



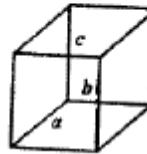
Tetragonal

$$a = b \neq c, \alpha = \beta = \gamma = 90^\circ$$



Orthorhombic
(or Rhombic)

$$a \neq b \neq c, \alpha = \beta = \gamma = 90^\circ$$



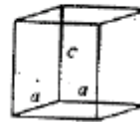
Rhombohedral
(or Trigonal)

$$a = b = c, \alpha = \beta = \gamma \neq 90^\circ$$



Hexagonal

$$a = b \neq c, \alpha = \beta = 90^\circ, \gamma = 120^\circ$$



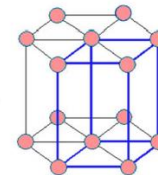
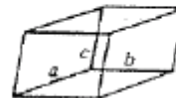
Monoclinic

$$a \neq b \neq c, \alpha = \gamma = 90^\circ \neq \beta$$



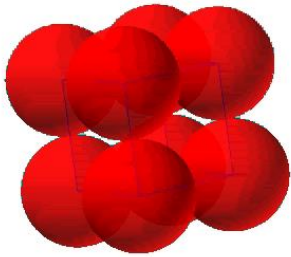
Triclinic

$$a \neq b \neq c, \alpha \neq \beta \neq \gamma \neq 90^\circ$$

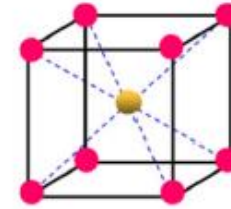
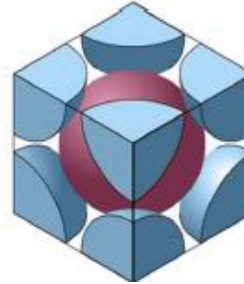


Hexagonal
 $a = b \neq c$
 $\alpha = \beta = 90^\circ \gamma = 120^\circ$

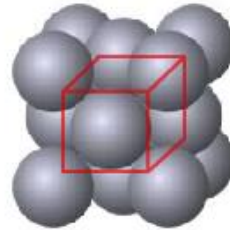
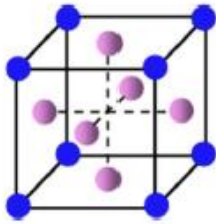
SIMPLE CUBIC STRUCTURE (SC)



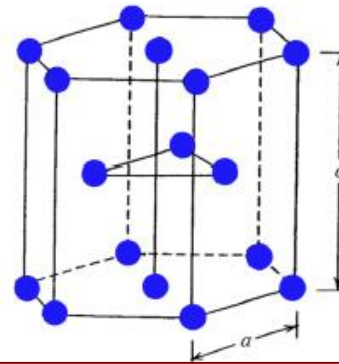
Body Centered Cubic (BCC)



Face Centered Cubic (FCC)



Hexagonal Close Packed (HCP)



Close packed direction:

Coordination # (Z): no. of nearest neighbor to a particular atom in the crystal

of atoms/unit cell:

Atomic Packing Factor =

$$APF = \frac{\text{volume of atoms in a unit cell}}{\text{total unit cell volume}}$$

| | Close packed direction | Coordination # (Z) | # of atoms/unit cell | APF |
|---------------------------|------------------------|--------------------|----------------------|------|
| Simple cubic | Cube edge | 6 | 1 | 0.52 |
| Body Centered Cubic (BCC) | Cube diagonal 0.68 | 8 | 2 | |
| Face Centered Cubic (FCC) | Face Diagonal | 12 | 4 | 0.74 |
| Hexagonal Close Packed | Edge | 12 | 6 | 0.74 |

THEORETICAL DENSITY

$$r = \frac{n A}{V_c N_A}$$

atoms/unit cell \rightarrow n Atomic weight (g/mol) \rightarrow A
 Volume/unit cell (cm³/unit cell) \rightarrow V_c Avogadro's number (6.023 x 10²³ atoms/mol) \rightarrow N_A

Example: Copper

- crystal structure = FCC: 4 atoms/unit cell
- atomic weight = 63.55 g/mol (1 amu = 1 g/mol)
- atomic radius $R = 0.128$ nm (1 nm = 10⁻⁷cm)
 $V_c = a^3$; For FCC, $a = 4R/\sqrt{2}$; $V_c = 4.75 \times 10^{-23}$ cm³

Result: theoretical $r_{Cu} = 8.89$ g/cm³

Compare to actual: $r_{Cu} = 8.94$ g/cm³

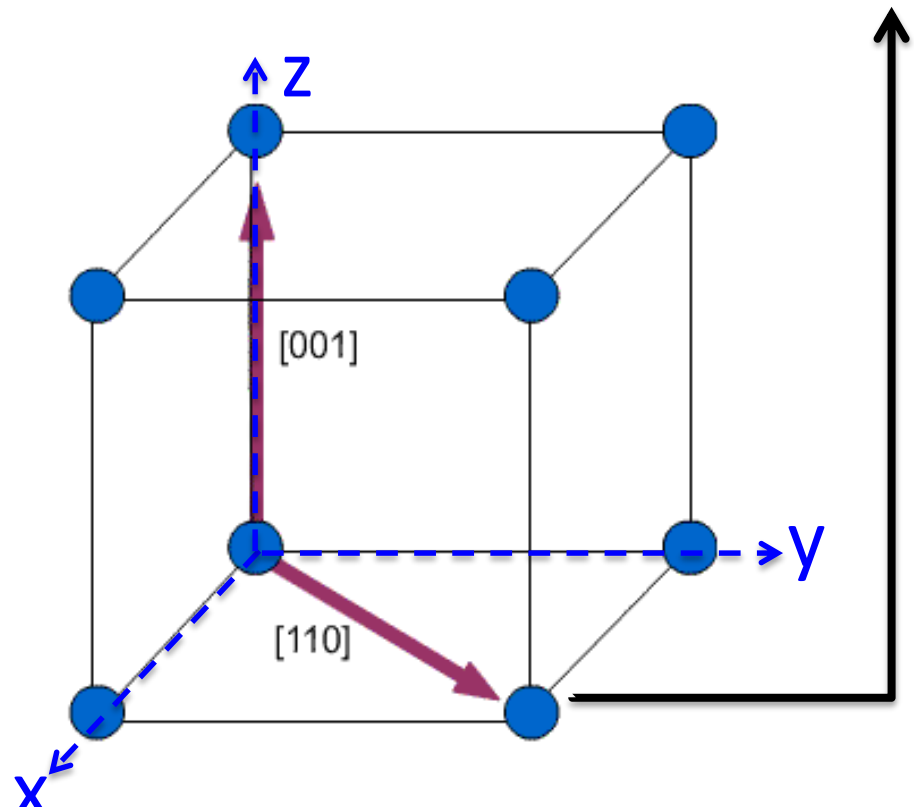
Crystallographic direction

To specify a direction:

Position the vector such that it passes through the origin

1. Find the coordinates of the two ends of the line (head & tail)
2. Subtract the coordinates of the two ends (head-tail)
3. Convert fractions, if any, into integers (multiply by a common factor) and reduce to lowest terms
4. Enclose in square brackets [u v w]

| | | | |
|----------------------|-------------------|---|---|
| Coordinates of Head: | 1 | 1 | 0 |
| Coordinates of Tail: | 0 | 0 | 0 |
| Subtract: | 1 | 1 | 0 |
| No fractions | | | |
| => | [u v w] = [1 1 0] | | |

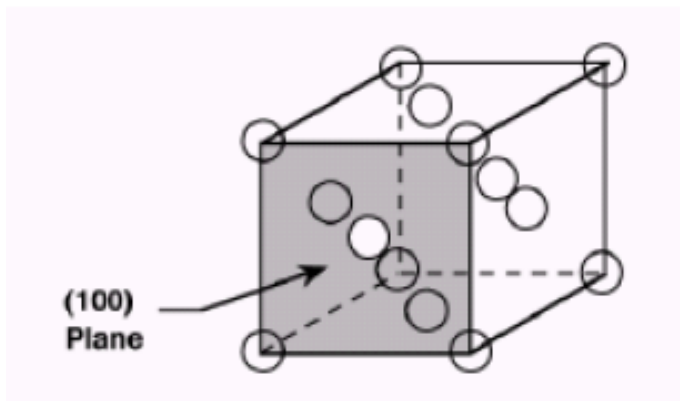


Crystallographic Planes:

Planes are described by notations, called **Miller indices (h k l)**

To find the Miller Indices of a plane, follow these steps:

- Determine the intercepts of the plane along the crystal axes
- Take the reciprocals
- Clear fractions
- Reduce to lowest terms and enclose in brackets ()



Intercept: $1 \infty \infty$

Reciprocal: $1 \ 0 \ 0$

Plane: (100)

□ Linear Density

The number of atoms per unit length for a specific crystallographic direction

$$LD = \frac{\text{number of atoms centered on direction vector}}{\text{length of direction vector}}$$

Example:

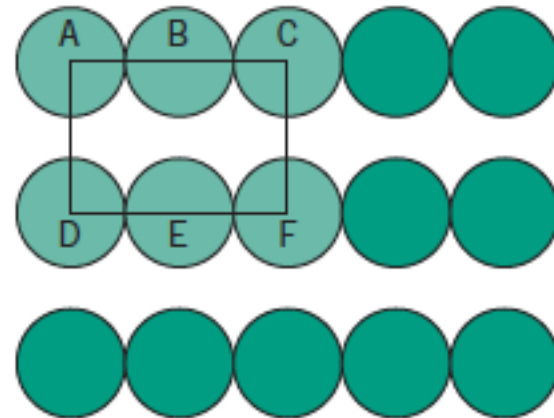
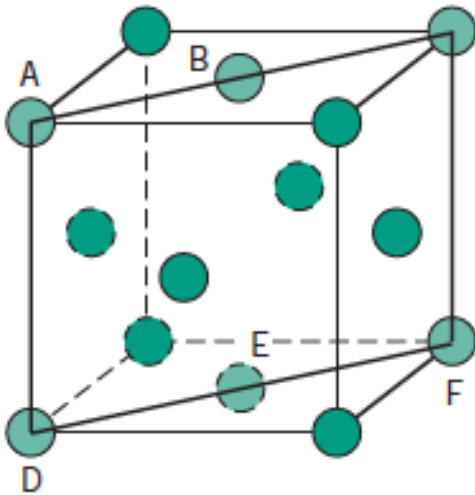
Calculate $LD_{[100]}$, $LD_{[110]}$, & $LD_{[111]}$ for FCC and BCC crystal structures

□ Planar Density

The number of atoms per unit area for a particular crystallographic plane

$$PD = \frac{\text{number of atoms centered on a plane}}{\text{area of plane}}$$

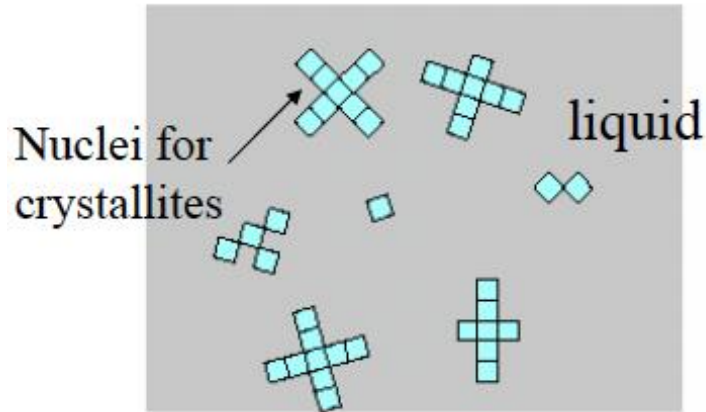
Example: $PD_{(110)/FCC}$ for FCC crystal structure



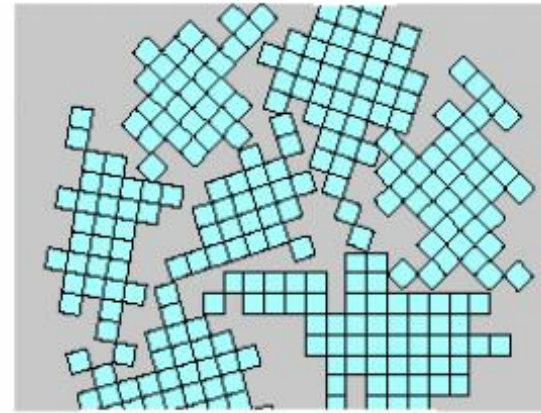
$$\begin{aligned} PD_{(110)/FCC} &= 2 \text{ atoms}/(\sqrt{2} a * a) \\ &= \sqrt{2} / a^2 \end{aligned}$$

Single crystal vs. polycrystalline materials

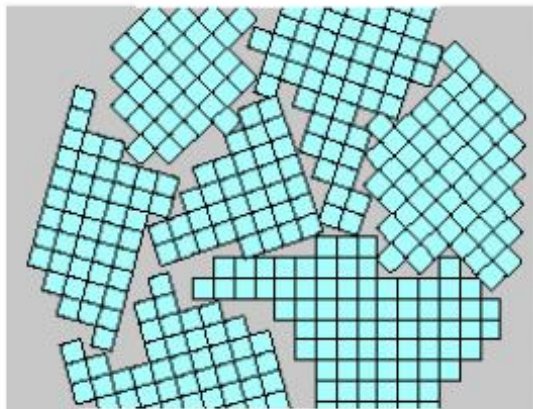
Solidification of a polycrystalline metal



^(a)
nucleation



Growth



^(c)



^(d)
Grains are formed

Main relations (Chapter 3)

$$\text{APF} = \frac{n * \frac{4}{3} \pi R^3}{\text{Volume of unit cell}}$$

$$\rho = \frac{nA}{V_c N_A}$$

$$\text{LD} = \frac{\text{number of atoms centered on direction vector}}{\text{length of direction vector}}$$

$$\text{PD} = \frac{\text{number of atoms centered on a plane}}{\text{area of plane}}$$

Chapter 4

Imperfections in Solids

Types of defects

1. Point defects (0D):

1.1) Vacancy

1.2) Self-interstitial

1.3) Impurities

Substitutional and Interstitial **solid solutions**

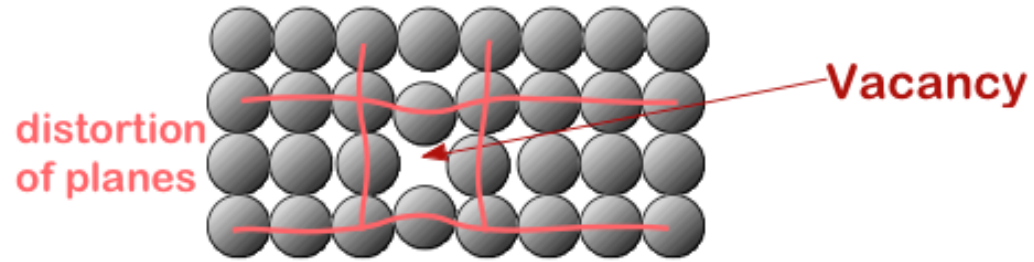
2. Line defects (1D): dislocations

3. Planar defects (2D): Grain boundaries

Defects

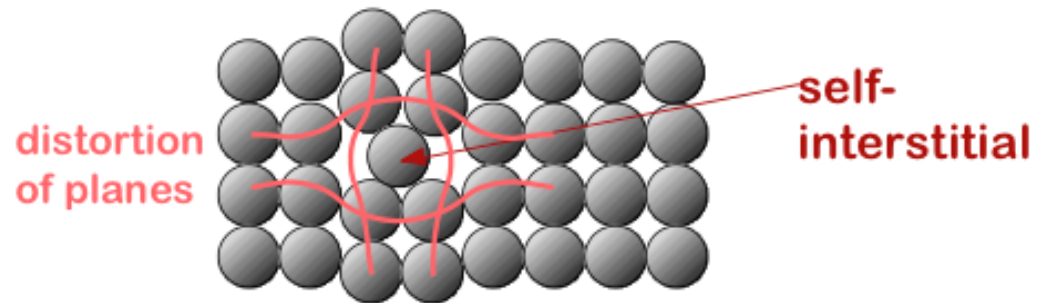
1. Point defects

1.1) Vacancy atoms



(host atoms
that occupy interstitial sites)

1.2) Self-interstitial atoms



A **host** atom is crowded into an interstitial site (*a space that under ordinary circumstances is not occupied*)

Equilibrium concentration of vacancies

$$N_v = N \exp\left(-\frac{Q_v}{kT}\right)$$

N_v : Equilibrium number of vacancies

N : Total number of atomic sites

Q_v : Energy required to form a vacancy

T : Temperature in Kelvin ($^{\circ}\text{C} + 273$)

k : Boltzmann's constant

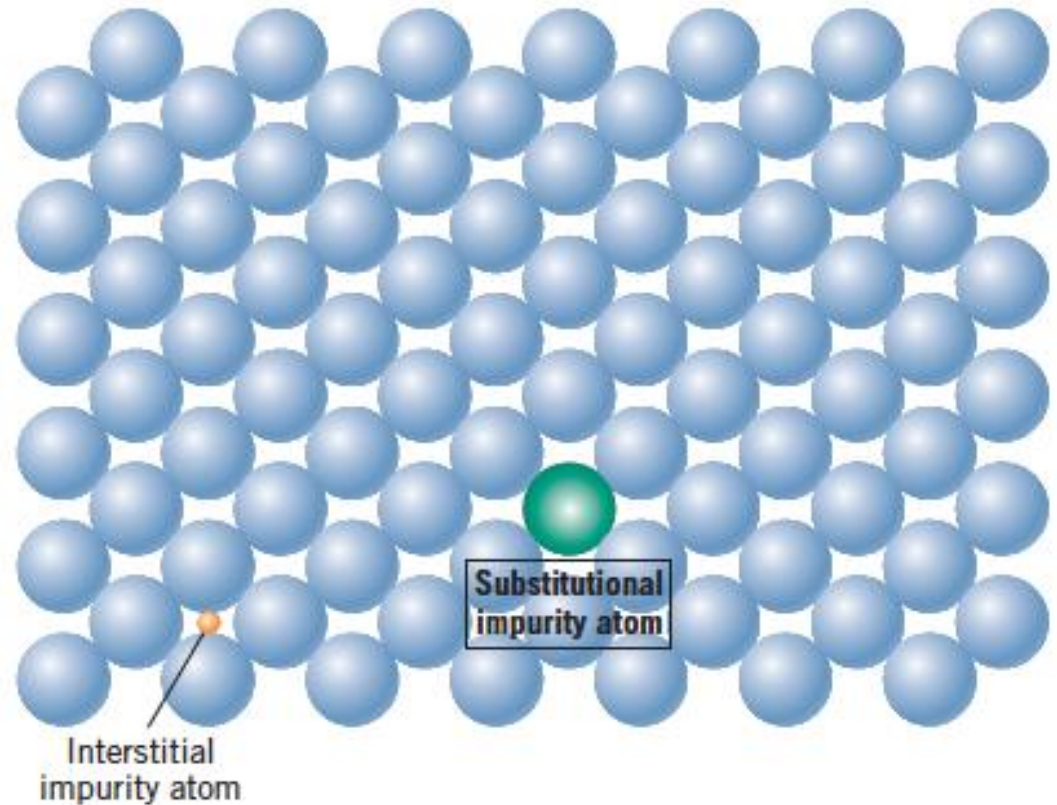
$(1.38 \times 10^{-23} \text{ J/atom K})$

$(8.62 \times 10^{-5} \text{ eV/atom K})$

1.3) Solid solutions: A homogenous crystalline phase that contains more than one chemical species

A. Substitutional solid solutions: The solute atoms replace or substitute for the host atoms.

B. Interstitial solid solutions: solute atoms occupy interstitial positions between the solvent atoms.



Factors that affect the complete solubility in solid solutions:

1. Atomic size factor: $|\Delta R\%| < 15\%$

The absolute difference in atomic radii between the two atom types is less than 15%. Otherwise, a new phase will form.

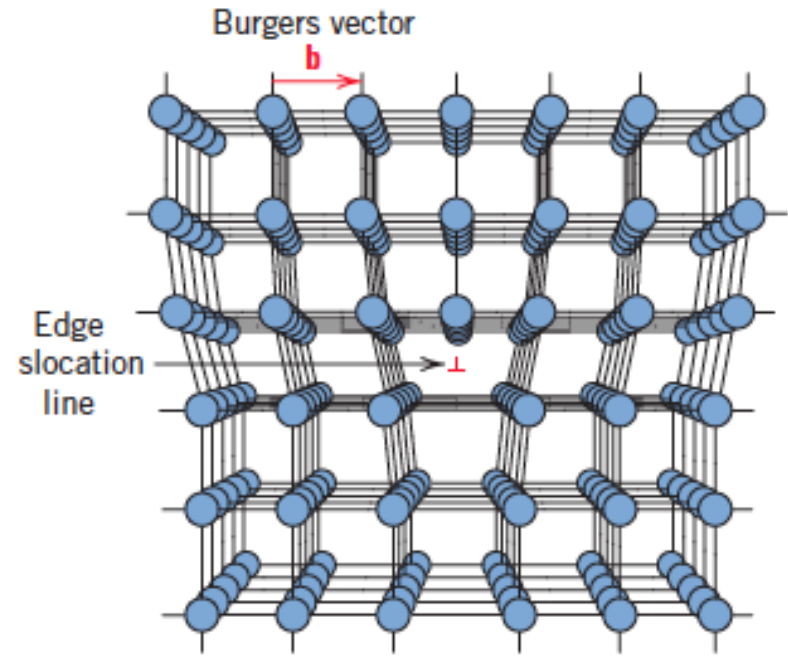
2. Crystal structure: The crystal structures for metals of both atom types must be the same.

3. Electronegativity: The electronegativities must be similar (see next slide) (*0.4 is assumed to be high*)

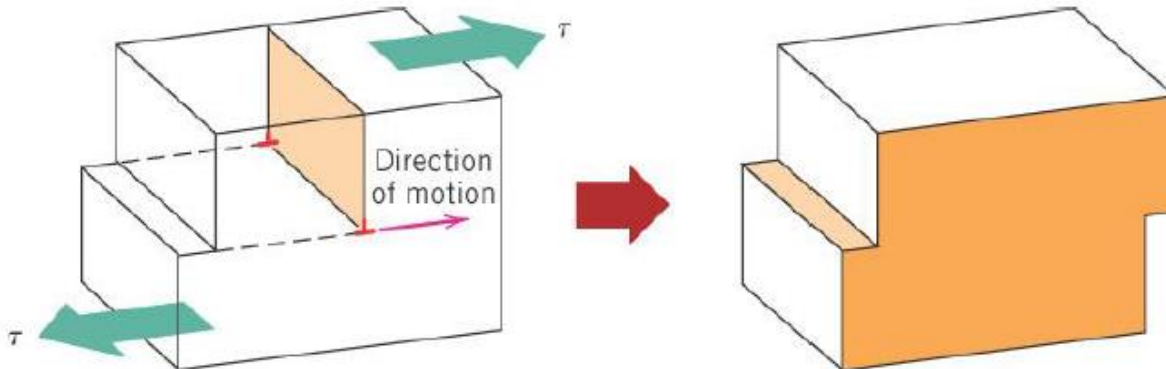
4. Valences: The valences should be the same, or nearly the same.

Line defects: dislocations

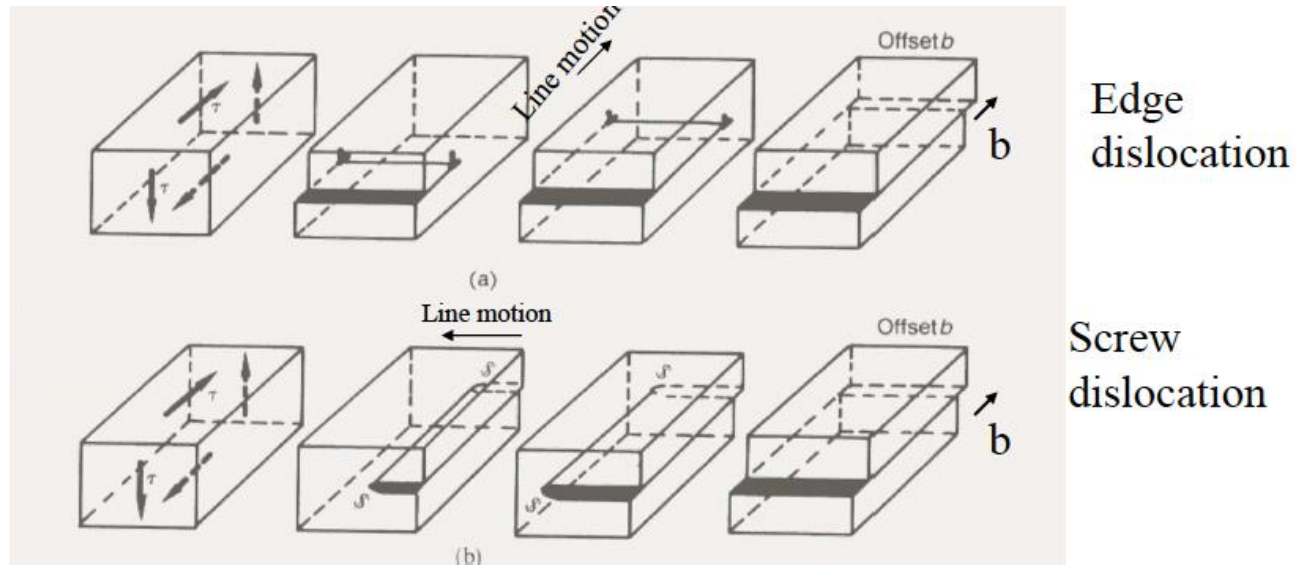
Dislocation is a linear crystalline defect around which there is atomic misalignment.



The movement of dislocations (slip) is the main reason for plastic (permanent) deformation in most metals.

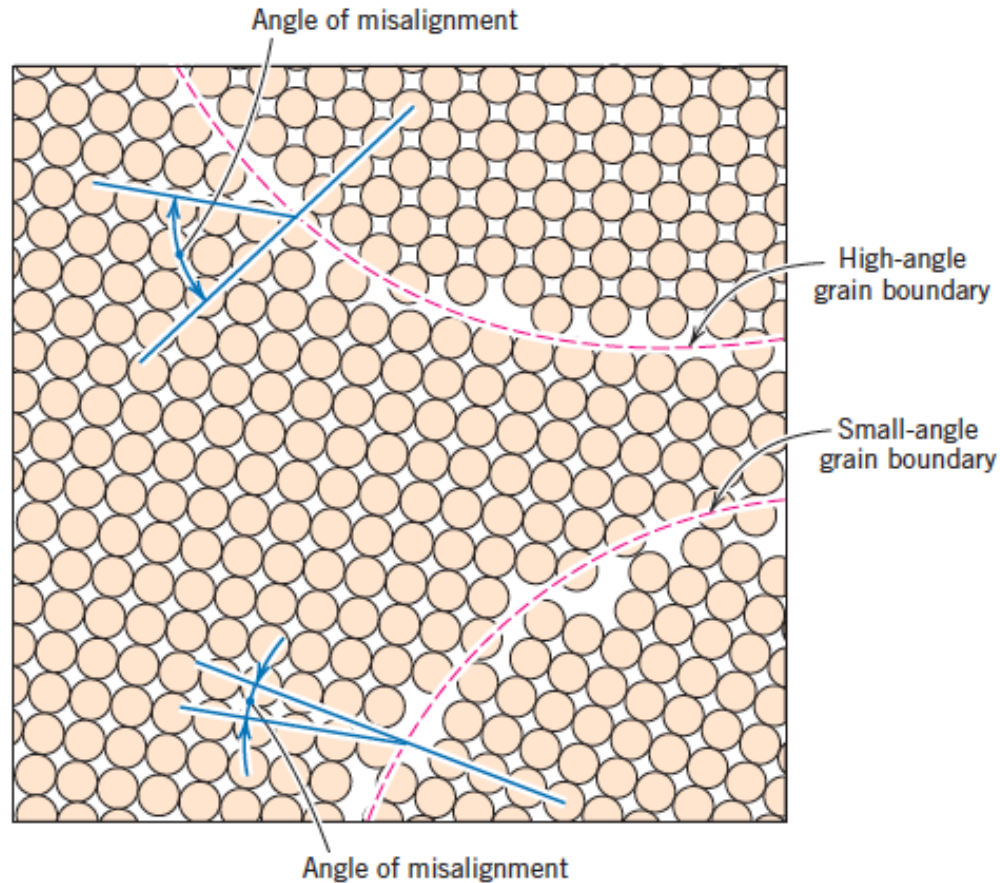


Geometric properties of dislocations



| Dislocation Property | Type of dislocation | |
|---|-----------------------------|-----------------------------|
| | Edge | Screw |
| Relation between dislocation line (\mathbf{t}) and \mathbf{b} | \perp | \parallel |
| Slip direction | \parallel to \mathbf{b} | \parallel to \mathbf{b} |
| Direction of dislocation line movement relative to \mathbf{b} | \parallel | \perp |

□ Planar defects: grain boundaries



Different grains have different orientations of atoms

Grain boundaries separate grains that have different lattice orientations and impede dislocation motion.

COMPOSITION

The relative content of a particular element within an alloy.

How to express the composition of an alloy?

Two descriptions



Weight %

it's based on the weight of a particular element relative to the total alloy weight

$$C_B = \frac{\text{mass of B}}{\text{total mass}} \times 100$$

Atom %

It's based on the number of moles of an element relative to the total moles of the elements in the alloy

$$C'_B = \frac{\# \text{ atoms of B}}{\text{total \# atoms}} \times 100$$