

PHYS 404
HANDOUT 8 – Applications of Bessel Functions in Physics

1. Given that $J_0(x) = \frac{1}{2\pi} \int_0^{2\pi} e^{ix \cos \theta} d\theta$, estimate the integral which appears in the study of Fraunhofer diffraction through a circular aperture of radius a . The parameter b is given by $b = (2\pi / \lambda) \sin \phi$, where ϕ is the angle defined by a point on a screen below the circular aperture relative to the normal through the center point.

$$\Phi \approx \int_0^a \int_0^{2\pi} e^{ibr \cos \theta} d\theta r dr .$$

(Arf. p. 580)

2. Find the energy spectrum of a quantum mechanical particle which is inside a sphere of radius a . Show what happens in the Bessel equation when $x = k\rho$.

(Arf. p. 629)

3. A circular plate has a radius equal to 1 and its plane surfaces thermally isolated from the environment. If the initial temperature is $F(\rho)$ and the circumference is kept at zero temperature, calculate the temperature of a point of the plate as a function of time.

(Sch. p. 114)

4. A hollow tube has an internal radius equal to a and an external one equal to b . If the initial temperature is $F(\rho)$ and both the internal and external surfaces are kept at zero temperature, calculate the temperature of a point of the cylinder as a function of time.

(Sch. p. 120)