

```
(* Abeer S. Al-Humaimedy / SEP.2012 *)
(* Implementing soaCSP in Coq *)
```

```
Require Import Arith.
Require Import ZArith.
Require Import Bool.
Require Import List.
Require Import String.
Require Import Logic.
Require Import Relations.
```

```
(* Compensating CSP *)
Section cCSP.
```

```
Set Implicit Arguments.
Unset Strict Implicit.
```

```
(***** Process Section *****)
(* isomorphisim *)
Parameter A:Set.
```

```
(* Channel *)
Axiom Ch :Set -> Set.
```

```
(* Inductive types Decleration *)
```

```
(* Channel Type *)
Inductive Channeltype (M:Set) :Set := addM : M -> Channeltype M ->
Channeltype M.
```

```
(* Actions *)
```

```
Inductive Action :Type:=
  |SUCC    : Action
  |Thr     : Action
  |Y       : Action
  |TAUI    : Action
  |CompI   : Action -> Action -> Action
  |TAU     : forall (A:Set), Ch A -> Action
  |Atomic  : forall (A:Set), A -> Action
  |IN      : forall (A:Set), Ch A -> A -> Action
  |OUT     : forall (A:Set), Ch A -> A -> Action.
```

```
(* Process *)
```

```
CoInductive Process : Type :=
  | STOP           : Process
  | Pref           : Action -> Process -> Process
  | Par            : Process -> Process -> Process
  | inchoice      : Process -> Process -> Process
  | exchoice      : Process -> Process -> Process
  | Seq           : Process -> Process -> Process
  | interrupt     : Process -> Process -> Process
  | Compen        : Process -> Process -> Process.
```

```
(* Simulation of CSP notations *)
```

```
Variable (pro1 pro2:Process) (va:A) (cha:Ch A) (ac:Action).
Notation "cha ! va " := (OUT cha va ) (at level 100).
```

```

Notation "cha ? va " := (IN cha va ) (at level 100).
Notation " ac ->> pro1 " := (Pref ac pro1) (at level 80).
Notation " pro1 |P| pro2" := (Par pro1 pro2) (at level 80).
Notation " pro1 [] pro2 " := (exchoice pro1 pro2) (at level 80).
Notation " pro1 |-| pro2 " := (inchoice pro1 pro2) (at level 80).
Notation " pro1 ; pro2 " := (Seq pro1 pro2) (at level 80).
Notation " pro1 (%) pro2 " := (Compen pro1 pro2) (at level 80).
Notation " pro1 |> pro2 " := (interrupt pro1 pro2) (at level 80).

```

(* Standard Processes *)

```

Definition Skip :Process := Pref SUCC STOP.
Definition Throw :Process := Pref Thr STOP.
Definition Yield :Process := Pref Y STOP.
Definition Skipp := Skip (%) Skip.
Definition Throww := Throw (%) Skip.
Definition Yieldd := Yield (%) Skip.
CoFixpoint Run (a : list Action) :Process :=
  match a with
  | nil => STOP
  | b :: nil => Pref b (Run a)
  | _ :: b :: _ => Pref b (Run a)
  end.

```

```

Definition Chaos ( a : list Action ) :Process := inchoice STOP (Run a).

```

(* Operational Semantics *)

```

Inductive Transition: Process -> Action -> Process -> Prop :=
  | Tr_prefix : forall l p, Transition ( l ->> p ) l p
  | Tr_ParL : forall p p' q l, Transition p l p' -> Transition (p
|P| q) l (p'|P| q)
  | Tr_ParR : forall p q q' l, Transition q l q' -> Transition (p
|P| q) l (p |P| q')
  | Tr_ParSen : forall p p' q q' l, (Transition p l p') /\ (Transition
q l q') -> Transition (p |P| q) l (p' |P| q')
  | Tr_inchl : forall A (c:Ch A) p q, Transition ( p |-| q) (TAU c) p
  | Tr_inchr : forall A (c:Ch A) p q, Transition ( p |-| q) (TAU c) q
  | Tr_exchl : forall p p' q l, Transition p l p' -> Transition (p []
q) l p'
  | Tr_exchr : forall p q q' l, Transition q l q' -> Transition (p []
q) l q'
  | Tr_Seq1 : forall p p' q l, Transition p l p' -> Transition (p ;
q) l (p' ; q)
  | Tr_Seq2 : forall A (c:Ch A) p p' q , Transition p SUCC p' ->
Transition (p ; q) (TAU c) q
  | Tr_Compen1 : forall p p' q l , Transition p l p' -> Transition ( p
(%) q) l (p' (%) q)
  | Tr_Compen2 : forall p q , Transition p SUCC STOP -> Transition (p
(%) q) SUCC q
  | Tr_Compen3 : forall p q , Transition p Thr STOP -> Transition (p
(%) q) Thr STOP
  | Tr_interp1 : forall p p' q l, Transition p l p' -> Transition (p |>
q) l (p'|> q)
  | Tr_interp2 : forall p q' q l, Transition p Thr STOP /\ Transition q
l q' -> Transition (p |> q) l q'.

```

(* Transitions *)

```

Inductive Transitions : Process -> Process -> Prop :=
  | Transition0: forall p q l, Transition p l q -> Transitions p q
  | Transitioni : forall p q r l , Transition p l q -> Transitions
q r -> Transitions p r.

```

(* Collection of Lemmas (Process Section) *)

```

Lemma One: forall (l1 l2:Action) p q , l1=l2 /\ Pref l1 p = Pref l2 q ->
p = q .

```

Proof.

```

  intros.
  destruct H.
  generalize H0.
  rewrite H.
  intros.
  injection H1.
  intros.
  auto.

```

Qed.

```

Lemma one :forall (l:Action) , (Pref l STOP) <> STOP.

```

Proof.

```

  intros.
  case Pref.
  intros.
  unfold not.
  intros.
  discriminate.

```

Qed.

```

Lemma OOne :forall (p q r :Process) (v:A)(c: Ch A) (l:Action) ,
p= ((c ! v) ->> r) /\ l= (OUT c v) -> Transition p l q = Transition
((c ! v) ->> r) (OUT c v) q.

```

Proof.

```

  intros.
  destruct H.
  rewrite H.
  rewrite H0.
  reflexivity.

```

Qed.

```

Lemma tOOne :forall A (c:Ch A)(p:Process) (v:A),Transition ((c ! v) ->>
p) (OUT c v) p.

```

Proof.

```

  intros.
  apply (Tr_prefix (OUT c v) p).

```

Qed.

```

Lemma two : forall p (c:Ch A) (k v:A) ,exists q,
(Transition ((c ! v) ->> ( (c ! k) ->> p)) (OUT c v)
q) /\ (Transition q (OUT c k) p).

```

Proof.

```

  intros.
  exists ((c ! k) ->> p).

```

```

    split.
    apply (Tr_prefix (OUT c v) ((c ! k) ->> p)).
    apply (Tr_prefix (OUT c k) p).
Qed.

```

Lemma Trans: forall p q r, Transitions p q -> Transitions q r ->
 Transitions p r.
 Proof.

```

    intros p q r H H0.
    generalize H.
    induction 1.
    apply (Transitioni H1 H0) .
    apply (Transitioni H1).
    apply IHTransitions; auto.

```

Qed.

(***** end of Prcess Section *****)

(***** Trace Section *****)

(* Lazy Lists*)

```

CoInductive Llist (A:Type) :Type :=
  | LNil : Llist A
  | LCons : A -> Llist A -> Llist A.

```

```

CoInductive Llists (A:Type) :Type :=
  | LNil : Llists A
  | LConss : A -> Llists A -> Llists A
  | LlConss : A -> Llists A -> Llists A -> Llists A.

```

```

CoFixpoint LAppend (A:Type) (u v: Llist A) :Llist A:=
  match u with
  | LNil => v
  | LCons a u' => LCons a (LAppend u' v )
end.

```

(* Trace Predicate *)

```

Inductive isTrace : Process -> list Action -> Prop :=
  | empty_Trace      : isTrace STOP nil
  | lcons_TracePrf   : forall (p:Process) (l: list Action) (a:Action),
isTrace p l -> isTrace (a ->> p) (a::l)
  | lcons_TraceSeq   : forall (p q:Process) (l k :list Action) (a:Action),
isTrace p (a::l) -> isTrace q k -> isTrace (p ; q)
(a::(l+k))
  | lcons_Traceincl  : forall (p q:Process) (l k :list Action),
isTrace p l -> isTrace q k -> isTrace (p |-| q)
(TAUI::l)
  | lcons_Traceinchr : forall (p q:Process) (l k : list Action),
isTrace p l -> isTrace q k -> isTrace (p |-| q)
(TAUI::k)
  | lcons_Traceexchl : forall (p q:Process) (l k : list Action) (a:Action),
isTrace p l -> isTrace q k -> isTrace (p [] q) l
  | lcons_Traceexchr : forall (p q:Process) (l k : list Action) (b:Action),

```

```

        isTrace p l -> isTrace q k -> isTrace (p [] q) k
|lcons_TraceParl  : forall (p q:Process) (l k pk: list Action) (a
b:Action),
        isTrace p (a::l) -> isTrace q (b::k) -> isTrace (p
|P| q) pk -> isTrace (p |P| q) (a::(b::(pk)))
|lcons_TraceParr  : forall (p q:Process) (l k pk: list Action) (a
b:Action),
        isTrace p (a::l) -> isTrace q (b::k) -> isTrace (p
|P| q) pk -> isTrace (p |P| q) (a::(b::(pk)))
|lcons_TraceSen   : forall (p q:Process) (l k pk: list
Action) (a:Action),
        isTrace p (a::l) -> isTrace q (a::k) -> isTrace (p
|P| q) pk -> isTrace (p |P| q) (a::pk)
|lcons_TraceCompen: forall (p q:Process) (l k pk:list Action) (a
b:Action),
        isTrace p (a::l) -> isTrace q (b::k) -> isTrace (p (%)
q) pk -> isTrace (p (%) q) ((CompI a b )::pk)
|lcons_TraceInter1 : forall (p q:Process) (l k : list
Action) (a:Action),
        isTrace p (a::l) -> isTrace q k -> isTrace (p |> q)
(a::l)
|lcons_TraceInter2 : forall (p q:Process) (l k : list
Action) (b:Action),
        isTrace p (Thr::nil) -> isTrace q (b::k) -> isTrace (p
|> q) (b::k).

```

Variable trace : forall p:Process, {t:list Action | isTrace p t}.

```

Definition Enumtrace (p:Process) (T:{t:list Action | isTrace p t}) : list
Action :=
  match T with
  | exist t h => t end.

```

```

Definition Trace (p:Process) : {T:(list Action) | isTrace p T }.
  intros.
  case p.
  exists nil.
  apply (empty_Trace).
  intros.
  exists(a:: Enumtrace(trace p0)).
  apply (lcons_TracePrf a) .
  destruct trace. simpl.
  exact i.
  intros;apply trace.
  intros;apply trace.
  intros;apply trace.
  intros;apply trace.
  intros;apply trace.
  intros;apply trace.
  Defined.

```

Definition intrace (p:Process) (t:list Action): Prop := (isTrace p t).

```

CoInductive AllTraces :Process -> Llist (list Action) -> Prop :=
  |TracesofSTOP : AllTraces STOP (LCons nil (LNil (list Action)))

```

```

|TracesOfPrf: forall (p:Process)(l: list Action)(k:Llist (list
Action)) (a:Action),
  isTrace p l -> AllTraces p k -> AllTraces (a ->> p) (LCons (a::l) k)
|TracesOfSeq: forall (p q:Process)(l: list Action)(k1 k:Llist (list
Action)) (a:Action),
  isTrace p l -> AllTraces p k -> AllTraces q k1 -> AllTraces (p ; q)
(LCons l (LAppend k k1))
|TracesOfinchl: forall (p q:Process)(l: list Action)(k1 k:Llist (list
Action)),
  isTrace p l -> AllTraces p k -> AllTraces q k1 -> AllTraces (p |-| q)
(LCons (TAUI::l) k)
|TracesOfinchr: forall (p q:Process)(l: list Action)(k1 k:Llist (list
Action)),
  isTrace q l -> AllTraces p k -> AllTraces q k1 -> AllTraces (p |-| q)
(LCons (TAUI::l) k1)
|TracesOfexchl : forall (p q:Process)(l: list Action)(k1 k:Llist (list
Action)) (a:Action),
  isTrace p (a::l) -> AllTraces p k -> AllTraces q k1 -> AllTraces (p []
q) (LCons (a::l) k)
|TracesOfexchr : forall (p q:Process)(l: list Action)(k1 k:Llist (list
Action)) (a:Action),
  isTrace q (a::l) -> AllTraces p k -> AllTraces q k1 -> AllTraces (p []
q) (LCons (a::l) k1)
|TracesOfParl : forall (p q:Process)(l k kp: list Action)(a
b:Action)(k1:Llist (list Action)),
  isTrace q (a::l) -> isTrace p (b::k) -> isTrace (p |P| q) kp ->
AllTraces (p |P| q) k1 ->
                                                                 AllTraces
(p |P| q) (LCons (a::(b::kp))k1)
|TracesOfParr : forall (p q:Process)(l k kp: list Action)(a
b:Action)(k1:Llist (list Action)),
  isTrace q (a::l) -> isTrace p (b::k) -> isTrace (p |P| q) kp ->
AllTraces (p |P| q) k1 ->
                                                                 AllTraces
(p |P| q) (LCons (b::(a::kp))k1)
|TracesOfSen : forall (p q:Process)(l k kp: list
Action)(a:Action)(k1:Llist (list Action)),
  isTrace q (a::l) -> isTrace p (a::k) -> isTrace (p |P| q) kp ->
AllTraces (p |P| q) k1 ->
AllTraces (p |P| q) (LCons (a::kp) k1)
|TracesOfComp : forall (p q:Process)(l k kp: list Action)(a
b:Action)(k1:Llist (list Action)),
  isTrace q (a::l)-> isTrace p (b::k)-> isTrace (p (%) q) kp ->
AllTraces (p (%) q) k1 ->
AllTraces (p (%) q) (LCons ((CompI a b)::kp) k1)
|TracesOfInter1: forall (p q:Process)(l k: list Action)(k1:Llist (list
Action)),
  isTrace q l -> isTrace p k -> AllTraces (p (%) q) k1 -> AllTraces (p
(%) q) (LCons l k1)
|TracesOfInter2: forall (p q:Process)(l k: list Action)(k1:Llist (list
Action)),
  isTrace q (Thr::nil) -> isTrace p k -> AllTraces (p (%) q) k1 ->
AllTraces (p (%) q) (LCons k k1).

Variable traces : forall p:Process, {t:Llist(list Action) | AllTraces p
t}.

```

```

Definition Enumtraces (p:Process) (T:{t:Llist(list Action) | AllTraces p
t}) :Llist( list Action) :=
  match T with
  | exist t h => t end.

```

```

Definition Traces (p:Process) : {T:Llist (list Action) | AllTraces p T }.
  intros.
  case p.
  exists (LCons nil (LNil (list Action))).
  apply TracesofSTOP.
  intros.
  exists (LCons (a::Enumtrace(trace p0)) (Enumtraces(traces p0))).
  apply (TracesOfPrf a) .
  destruct trace. simpl.
  exact i.
  destruct traces. simpl.
  exact a0.
  intros;apply traces.
  intros;apply traces.
  intros;apply traces.
  intros;apply traces.
  intros;apply traces.
  intros;apply traces.
  intros;apply traces.
Defined.

```

(* Process Bisimulation *)

```

CoInductive Process_eq :Process -> Process -> Prop :=
  Pro_eq :
    forall p q:Process,
      (forall (a:Action) (p':Process), Transition p a p' -> exists q'
:Process , Transition q a q' /\ Process_eq p' q' ) ->
      (forall (a:Action) (q':Process), Transition q a q' -> exists p'
:Process , Transition p a p' /\ Process_eq p' q') ->
      Process_eq p q.

```

Lemma Process_refl : forall p:Process, Process_eq p p.

```

Proof.
  cofix.
  intros.
  apply (Pro_eq ).
  intros. exists p'.
  split; auto with v62.
  intros. exists q'.
  split; auto with v62.

```

Qed.

Lemma Process_sym : forall p q : Process, Process_eq p q -> Process_eq q

```

p.
  cofix.
  intros p q H. inversion_clear H.
  apply Pro_eq.
  intros a q'.
  intros trans.
  elim (H1 a q' trans). clear H1.

```

```

intros p' H; elim H; exists p'; split; auto with v62.
intros a p' trans.
elim (H0 a p' trans); clear H0.
intros q' H; elim H; clear H.
intros transl str.
exists q'; split; auto with v62.
Qed.

```

Hint Immediate Process_sym.

Lemma Process_trans :

```

forall p q r : Process, Process_eq p q -> Process_eq q r -> Process_eq p
r.

```

cofix.

```

intros p q r pq qr.
inversion_clear pq; inversion_clear qr.
apply Pro_eq.
intros a p' tp.
cut (exists q' : Process, Transition q a q' /\ Process_eq p' q').
intros G. elim G. clear G.
intros q' G. elim G.
intros tq pq'. elim (H1 a q' tq).
clear G.
intros r' G; elim G; clear G.
intros tr qr'; exists r'; split. auto with v62.
apply Process_trans with q'; auto with v62.
elim (H a p' tp).
intros q' G; elim G; clear G.
intros tq pq'.
exists q'; split; auto with v62.
intros a r' tr.
cut (exists q' : Process, Transition q a q' /\ Process_eq q' r').
intros G; elim G; clear G.
intros q' G; elim G; clear G.
intros tq qr'.
elim (H0 a q' tq).
intros p' G; elim G; clear G.
intros tp pq'; exists p'; split; auto with v62.
apply Process_trans with q'; auto with v62.
elim (H2 a r' tr).
intros q' G; elim G; clear G.
intros tq qr'; exists q'; split; auto with v62.
Qed.

```

(* Traces Bisimulation *)

```

(*)
CoInductive Traces_eq : Llist (list Action) -> Llist (list Action)-> Prop
:=
  |Ts_eq: forall (p q: Process) (t:list Action),
    Traces_eq (Enumtraces(Traces p)) (Enumtraces(Traces q)) /\
isTrace p t /\ isTrace q t ->
    Traces_eq (LCons t (Enumtraces(Traces p))) (LCons t
(Enumtraces(Traces q))).
*)

```



```

CoInductive Llist_eq (A:Type):Llist A-> Llist A -> Prop:=
  | eq0: Llist_eq (LNil A) (LNil A)
  | eq1: forall (a : A) (u u':Llist A), Llist_eq u u' -> Llist_eq (LCons
a u) (LCons a u').

```

```

Lemma Llist_refl : forall (A:Type)(l:Llist A), Llist_eq l l.

```

```

Proof.

```

```

  cofix H.

```

```

  intros.

```

```

  case l; [left | right ].

```

```

  apply H.

```

```

Qed.

```

```

Lemma Pro_Traces_refl : forall p:Process, Llist_eq (Enumtraces(Traces p))
(Enumtraces(Traces p)).

```

```

cofix H.

```

```

intros.

```

```

case (Enumtraces(Traces p)).

```

```

apply eq0.

```

```

intros.

```

```

apply eq1.

```

```

apply (Llist_refl l0).

```

```

Qed.

```

```

(* Trace Equivalence *)

```

```

Theorem Trace_Eqv : forall p q:Process , Llist_eq (Enumtraces(Traces p))
(Enumtraces(Traces q))

```

```

-> Process_eq p q.

```

```

Proof.

```

```

  cofix H.

```

```

  intros.

```

```

  destruct p .

```

```

  destruct q .

```

```

  apply (Process_refl STOP).

```

```

  apply (Pro_eq).

```

```

  intros; exists p' ; split ; inversion H0 ; apply (Process_refl p') .

```

```

  intros; exists q' ; split ; inversion H0 ; apply (Process_refl q') .

```

```

  apply (Pro_eq).

```

```

  intros ; exists p' ; split ; inversion H1 ; apply (Process_refl p') .

```

```

  intros .

```

```

  cut (exists p' : Process, Transition STOP a p' /\ Process_eq p' q').

```

```

  intros G; elim G.

```

```

  intros p' m. apply G. elim H1.

```

```

  intros.

```

```

  intros tq qr'.

```

```

  elim m. intros.

```

```

  apply G .

```

```

  exists q'. split. inversion H0.

```

```

  inversion H1.

```

```

  elim (H1 a q').

```

```

  exists q'. split .

```

```
(***** End of Trace Section *****)
(***** Refusals Section *****)
```

```
(* Refusals *)
```

```
CoInductive Refusal (relem:Set) :Set :=
  | addref : relem -> Refusal relem -> Refusal relem.
```

```
(*****
(* Pictorial Representation of a Process *)
```

```
CoInductive Tree (A:Type):Type :=
  | leaf      : Tree A
  | OneNode   : A -> Tree A -> Tree A
  | OneNodeE  : Tree A -> Tree A
  | TwoNodes  : A -> Tree A -> Tree A -> Tree A
  | TwoNodesE: Tree A -> Tree A -> Tree A.
```

```
CoFixpoint Seq2To1 (p q :Process):Process :=
  match p with
  | STOP => q
  | a ->> p' => a ->> (Seq2To1 p' q)
  | inchoice p' q' => inchoice (Seq2To1 p' q) (Seq2To1 q' q)
  | exchoice p' q' => exchoice (Seq2To1 p' q) (Seq2To1 q' q)
  | Seq p' q' => Seq p' (Seq2To1 q' q)
  | Par p' q' => Par (Seq2To1 p' q) (Seq2To1 q' q)
  | _ => q
  end.
```

```
CoFixpoint PTrace (p:Process): Tree Action :=
  match p with
  | STOP      => leaf Action
  | a ->> p'   => OneNode a (PTrace p')
  | inchoice p' q => TwoNodes TAU1 (PTrace p') (PTrace q)
  | exchoice p' q => TwoNodesE (PTrace p') (PTrace q)
  | Seq p' q => OneNodeE (PTrace (Seq2To1 p' q) )
  | Par p' q =>
    match p', q with
    | STOP , _ => OneNodeE (PTrace q)
    | _ , STOP => OneNodeE (PTrace p')
    | a->> p'' , b ->> q' => TwoNodesE (OneNode a (PTrace (p'' |P|
q))) (OneNode b (PTrace (p' |P| q'))))
    | a->> p'' , q' [] q'' =>
      TwoNodesE (OneNode a (PTrace (p'' |P| q))) (TwoNodesE
(PTrace (p' |P| q')) (PTrace (p' |P| q'')))
    | a->> p'' , q' |-| q'' =>
      TwoNodesE (OneNode a (PTrace (p'' |P| q))) (TwoNodes
TAUI (PTrace (p' |P| q')) (PTrace (p' |P| q'')))
    | a->> p'' , q' |P| q'' =>
      TwoNodesE (OneNode a (PTrace (p'' |P| q))) (OneNodeE
(PTrace (q |P| p')))
    | a->> p'' , q' ; q'' => OneNode a (PTrace (p'' |P| (Seq2To1 q'
q'')))
    | a ->> p'' , q' |> q'' => OneNode a (PTrace (p'' |P| q'))
    | a ->> p'' , q' (%) q'' => OneNode a (PTrace (p'' |P| q'))
  end.
```

```

    | q' [] q'', _ => TwoNodesE (PTrace (q' |P| q)) (PTrace (q'' |P|
q))
    | q' |-| q'', _ => TwoNodes TAU1 (PTrace (q' |P| q)) (PTrace (q''
|P| q))
    | q' ; q'', _ => OneNodeE (PTrace ((Seq2To1 q' q'') |P| q))
    | q' |P| q'', _ => OneNodeE (PTrace (q' |P| (q'' |P| q)) )
    |_, _ =>leaf Action
end
|_ =>leaf Action

end.

```

```

Fixpoint unfold_Tree (A:Type) (n:nat) (t1 :Tree A):Tree A := match n with
| 0 => t1
| S n' => match t1 with
| leaf => (leaf A)
| OneNodeE t1' => OneNodeE (unfold_Tree n' t1')
| OneNode a t1'=> OneNode a (unfold_Tree n' t1')
| TwoNodes a t1' t1'' => TwoNodes a (unfold_Tree n' t1')
(unfold_Tree n' t1'')
| TwoNodesE t1' t1''=> TwoNodesE (unfold_Tree n' t1')
(unfold_Tree n' t1'')
end
end.

```

```

CoFixpoint Ptf (t1:Tree Action)(li:list Action): Tree (list Action) :=
match t1 with
|leaf => (leaf (list Action))
|OneNode a t1'=> OneNode (a::li)(Ptf t1' (a::li) )
|OneNodeE t1' => OneNodeE (Ptf t1' li )
|TwoNodes a t1' t2 => TwoNodes (a::li) ( Ptf t1' (a::li) ) ( Ptf
t2 (a::li) )
|TwoNodesE t1' t2=> TwoNodesE (Ptf t1' (li) ) ( Ptf t2 (li) )
end.

```

```

Definition TracesSimulation (t1:Tree Action): Tree (list Action) := Ptf
t1 nil .

```

```

Variable a b c f d a' b' c':Action.

```

```

Definition xx:Process := a ->> (f ->> (d ->> ((b ->> STOP) [] (c ->>
STOP) ))) .

```

```

Definition xx':Process := a' ->> ((b' ->> STOP) [] (c' ->> STOP) ).

```

```

Eval compute in (unfold_Tree 50 ( (PTrace (xx ; (xx' ; xx')) ) ) ).

```

```

Eval compute in (unfold_Tree 100( TracesSimulation (PTrace (xx ; (xx' ;
xx') )))).

```

```

(*****
*****
)

```

```

(* Testing Example *)

```

```

Variable a b c a' b' c':Action.

```

```

Definition xx:Process := a ->> ((b ->> STOP) [] (c ->> STOP) ).

```

```

Definition xx':Process := a' ->> ((b' ->> STOP) [] (c' ->> STOP) ).

```

```

Eval compute in (unfold_n 300( PTrace (( Seq2To1 xx xx') |P| xx) ) ).

```