



SECOND MID TERM EXAM

Name (in Arabic): .....

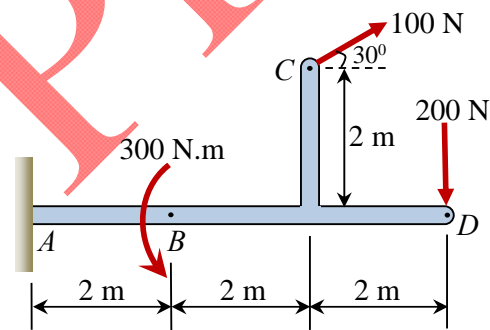
Student No.: .....

Section / Instructor: .....

Q. No.	Max. Marks	Marks Obtained
1	10	
2	10	
3	10	
<b>Total</b>	<b>30</b>	

**Question # 1(a) (5 Marks)**

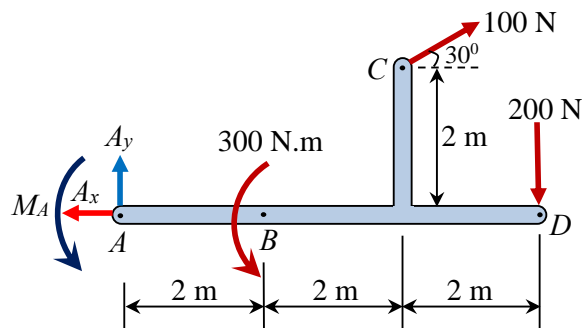
For the beam shown in the figure, calculate the reactions at the fixed support A.



**Solution**

As the support A is a fixed support, it will offer three reactions as shown in the free body diagram. Let us assume that these three reactions are  $A_x$ ,  $A_y$  and  $M_A$  respectively. We will find these three reactions with the help of three equilibrium equations as follows:

Free Body Diagram



$$\rightarrow \Sigma F_x = 0 \Rightarrow -A_x + 100 \cos 30^\circ = 0$$

$$\Rightarrow \underline{A_x = 86.6 \text{ N}} \quad \text{Ans.}$$

1 mark

$$\uparrow \Sigma F_y = 0 \Rightarrow A_y + 100 \sin 30^\circ - 200 = 0$$

$$\Rightarrow \underline{A_y = 150 \text{ N}} \quad \text{Ans.}$$

1 mark

$$CCW(+) \Sigma M_A = 0 \Rightarrow M_A + 300 + (100 \sin 30^\circ) \times 4 - (100 \cos 30^\circ) \times 2 - 200 \times 6 = 0$$

$$\Rightarrow \underline{M_A = 873.2 \text{ N.m}} \quad \text{Ans.}$$

3 marks

Student name

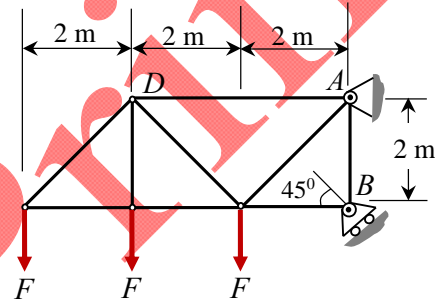
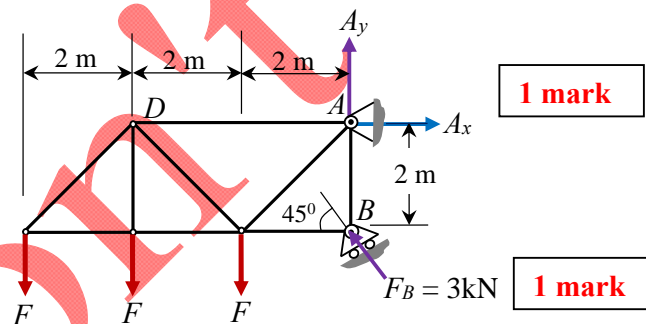
Marks obtained  
for Q.1

Student number

**Question # 1(b) (5 Marks)**

For the truss and loading shown in the figure:

If the magnitude of the reaction at the roller **B** is **3 kN**, determine the magnitude of each of the three forces **F** that can be supported by the truss.

**Solution**

1 mark

1 mark

The forces  $F$  can be obtained by applying  $\sum M_A = 0$  (as the unknowns  $A_x$  and  $A_y$  can be eliminated by taking the moments about point  $A$ ), that is:

$$CCW(+)\sum M_A = 0 \Rightarrow F \times 6 + F \times 4 + F \times 2 - 3 \cos 45^\circ \times 2 = 0 \Rightarrow F = 0.354 \text{ kN}$$

$$\Rightarrow \underline{F = 354 \text{ N}} \text{ Ans.}$$

3 marks

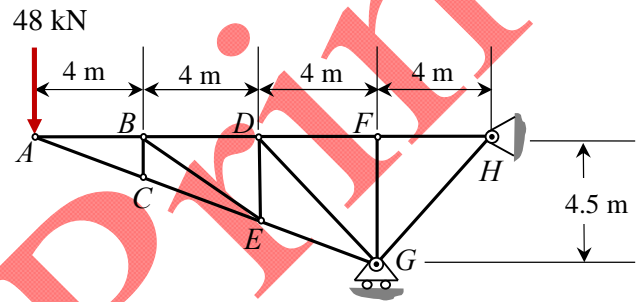
Student name	
Student number	

Marks obtained for Q.2

**Question # 2 (10 Marks)**

For the truss and loading shown in the figure:

- Calculate the support reactions at roller **G** and pin **H**
- Identify the correct zero-force members
- Calculate the forces in members **AB** and **AC** by using method of joints
- Calculate the forces in members **DF**, **DG** and **EG** by using method of sections



**Solution:**

a) Reactions:

$$\rightarrow \Sigma F_x = 0 \Rightarrow H_x = 0 \quad \text{Ans.}$$

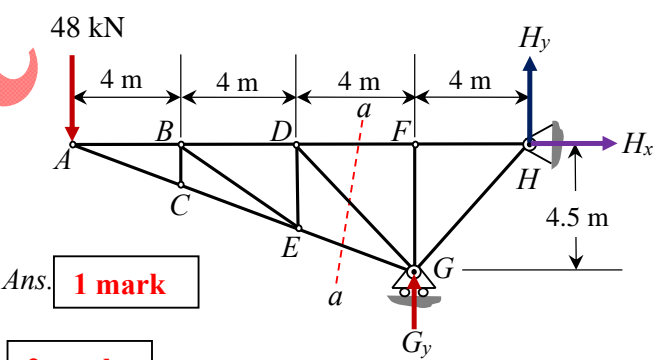
1 mark

$$CCW(+)\Sigma M_H = 0 \Rightarrow 48 \times 16 - 4 \times G_y = 0$$

1 mark

$$\Rightarrow G_y = 192 \text{ kN } \uparrow \quad \text{Ans.}$$

$$\uparrow \Sigma F_y = 0 \Rightarrow -48 + 192 + H_y = 0 \Rightarrow H_y = -144 \text{ kN } \downarrow \quad \text{Ans.}$$



1 mark

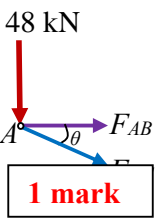
b) Zero force members: **BC; BE; DE; DG** and **FG**

2 marks

c) Forces in the members **AB** and **AC** using method of joints:

$$\tan \theta = \frac{4.5}{12} \Rightarrow \theta = 20.556^\circ; \quad \sin \theta = 0.3511 \text{ and } \cos \theta = 0.9363$$

$$\uparrow \Sigma F_y = 0 \Rightarrow -48 - F_{AC} \sin \theta = 0 \Rightarrow -48 - F_{AC} \times 0.3511 = 0 \Rightarrow F_{AC} = -136.7 \text{ kN (C)} \quad \text{Ans.}$$



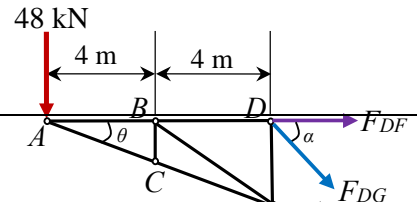
1 mark

$$\rightarrow \Sigma F_x = 0 \Rightarrow F_{AB} + F_{AC} \cos \theta = 0 \Rightarrow F_{AB} + (-136.7) \times 0.9363 = 0 \Rightarrow F_{AB} = 128 \text{ kN (T)} \quad \text{Ans.}$$

1 mark

d) Forces in the members **DF**, **DG** and **EG** using method of sections:

Cut the truss into the two parts through the section **a-a** as shown above, and then on the left side of the free body diagram (FBD) move the member forces **F<sub>DF</sub>** and **F<sub>DG</sub>** to the point **D** and **F<sub>EG</sub>** to the point **E**.



$$\tan \theta = \frac{4.5}{12} \Rightarrow \theta = 20.556^\circ; \sin \theta = 0.3511 \text{ and } \cos \theta = 0.9363$$

$$CCW(+)\Sigma M_A = 0 \Rightarrow F_{DG} \sin \alpha \times 8 = 0 \Rightarrow \underline{F_{DG} = 0} \quad \text{Ans.} \quad \boxed{1 \text{ mark}}$$

$$\uparrow \Sigma F_y = 0 \Rightarrow -48 - F_{EG} \sin \theta - F_{DG} \sin \alpha = 0 \Rightarrow -48 - F_{EG} \times 0.3511 - 0 = 0 \Rightarrow \underline{F_{EG} = -136.7 \text{ kN (C)}} \quad \text{Ans.}$$

**1 mark**

$$\rightarrow \Sigma F_x = 0 \Rightarrow F_{DF} + F_{DG} \cos \alpha + F_{EG} \cos \theta = 0 \Rightarrow F_{DF} + 0 + (-136.7) \times 0.9363 = 0 \Rightarrow \underline{F_{DF} = 128 \text{ kN (T)}} \quad \text{Ans.}$$

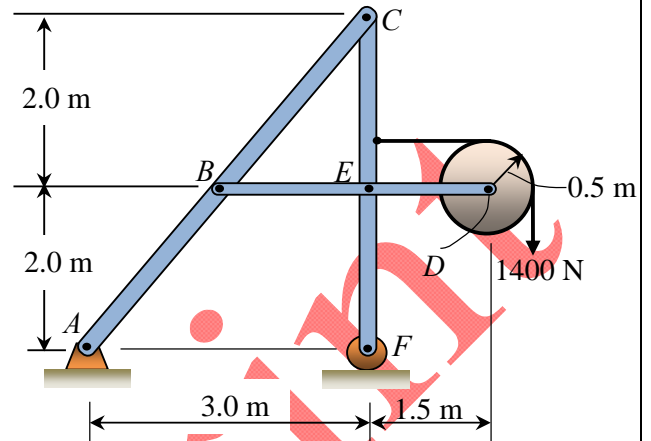
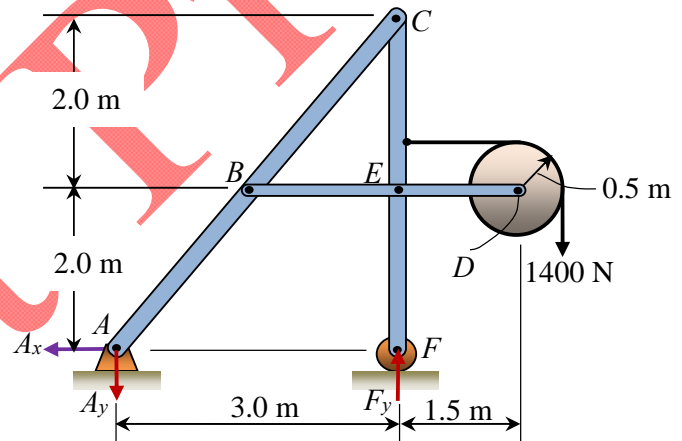
**1 mark**

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**Question # 3 (10 Marks)**

For the frame shown in the figure:

- Find the reactions at the pin and roller supports **A** and **F** respectively.
- Draw the free body diagrams (**FBD**) for each member.
- Determine the horizontal and vertical components of force at **C**.

**Solution**

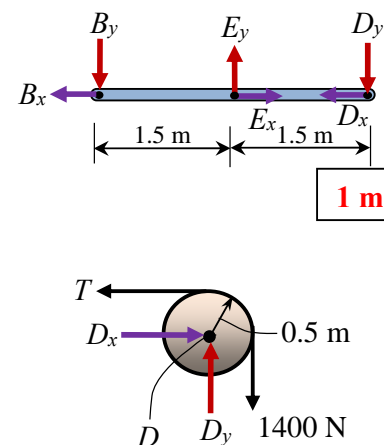
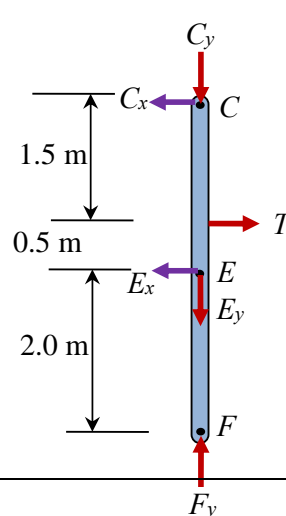
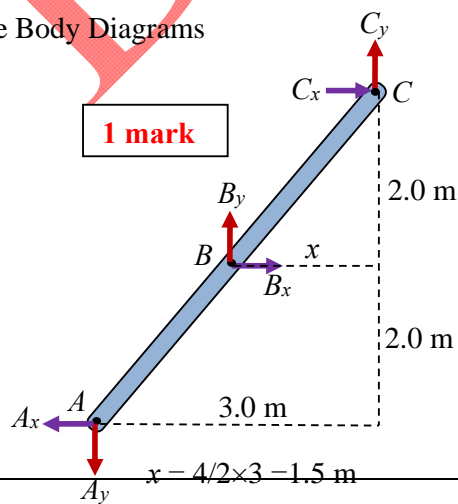
(a) Reactions

$$\rightarrow \Sigma F_x = 0 \Rightarrow -A_x = 0 \Rightarrow \underline{A_x = 0} \quad \text{Ans.} \quad \boxed{1 \text{ mark}}$$

$$CCW(+)\Sigma M_A = 0 \Rightarrow F_y \times 3.0 - 1400 \times 5 = 0 \Rightarrow \underline{F_y = 2333.3 \text{ N}} \quad \text{Ans.} \quad \boxed{1 \text{ mark}}$$

$$\uparrow \Sigma F_y = 0 \Rightarrow -A_y + F_y - 1400 = 0 \Rightarrow -A_y + 2333.3 - 1400 = 0 \Rightarrow \underline{A_y = 933.3 \text{ N}} \quad \text{Ans.} \quad \boxed{1 \text{ mark}}$$

(b) Free Body Diagrams



1 mark

1 mark

(c) Horizontal and vertical component of forces at C

From Pulley D

$$CCW(+)\Sigma M_D = 0 \Rightarrow T \times 0.5 - 1400 \times 0.5 = 0 \Rightarrow T = 1400 \text{ N}$$

1 mark

From vertical member CEF

$$CCW(+)\Sigma M_E = 0 \Rightarrow C_x \times (1.5 + 0.5) - T \times 0.5 = 0 \Rightarrow C_x \times 2.0 - 1400 \times 0.5 = 0 \Rightarrow C_x = 350 \text{ N} \quad \underline{\text{Ans.}}$$

1 mark

From inclined member ABC

$$CCW(+)\Sigma M_B = 0 \Rightarrow -A_x \times 2.0 + A_y \times 1.5 - C_x \times 2 + C_y \times 1.5 = 0$$

$$\Rightarrow 0 \times 2.0 + 933.3 \times 1.5 - 350 \times 2 + C_y \times 1.5 = 0 \Rightarrow C_y = -466.6 \text{ N} \quad \underline{\text{Ans.}}$$

1 mark

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