



**SECOND MID TERM EXAM
 (SOLUTION)**

Name (in Arabic):

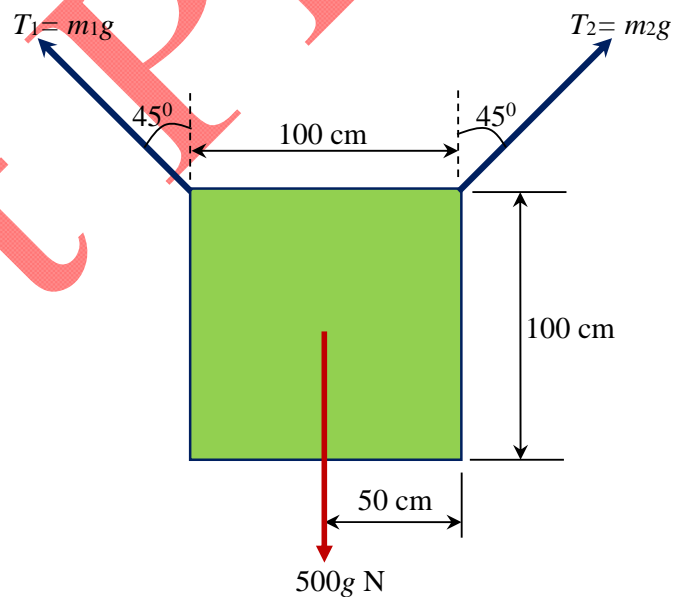
Student No.:

Section / Instructor:

Q. No.	Max. Marks	Marks Obtained
1	10	
2	10	
3	10	
Total	30	

Question # 1(a) 2.5 Marks)

A 500 kg uniform plate is hanging as shown in the figure. Calculate the values of the two masses (m_1 and m_2) for the equilibrium of the plate.



Solution

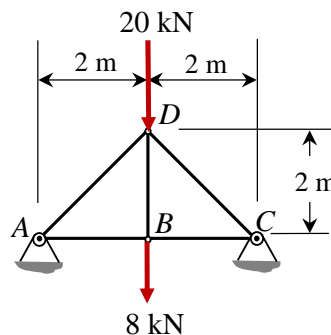
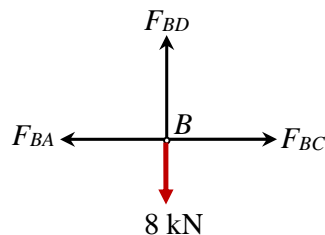
Applying the equilibrium equations, we have

$$\begin{aligned} \rightarrow \Sigma F_x = 0 &\Rightarrow -T_1 \sin 45^\circ + T_2 \sin 45^\circ = 0 \\ \Rightarrow T_1 = T_2 &\Rightarrow m_1 g = m_2 g \Rightarrow m_1 = m_2 \\ \uparrow \Sigma F_y = 0 &\Rightarrow T_1 \cos 45^\circ + T_2 \cos 45^\circ - 500g = 0 \\ \Rightarrow 2T_1 \frac{1}{\sqrt{2}} = 500g &\Rightarrow T_1 = \frac{500}{\sqrt{2}} g \Rightarrow m_1 g = \frac{500}{\sqrt{2}} g \\ \underline{m_1 = m_2 = 353.5 \text{ kg}} &\text{ Ans.} \end{aligned}$$

Question # 1(b) (2.5 Marks)

For the truss shown in the figure, calculate the force in member **DB**.

Solution



$$\uparrow \Sigma F_y = 0 \Rightarrow F_{BD} - 8 = 0 \Rightarrow \underline{\underline{F_{BD} = 8 \text{ kN}}} \text{ Ans.}$$

Student name

Marks obtained
for Q.1

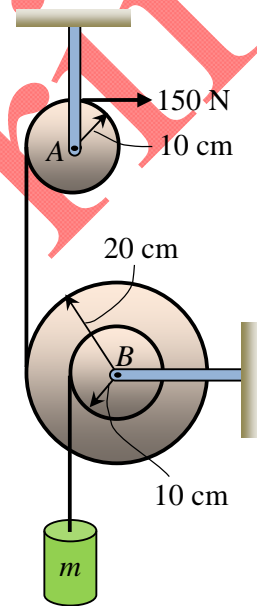
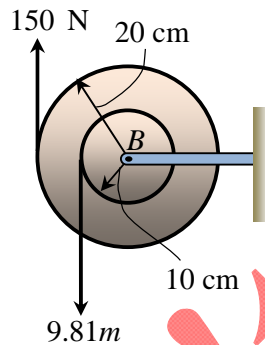
page 2/4

Student number

Question # 1(c) (2.5 Marks)

If the pulley system is in equilibrium, calculate the mass (m) of the hanging cylinder.

Solution



$$CCW(+) \Sigma M_B = 0 \Rightarrow 9.81m \times 10 - 150 \times 20 = 0$$

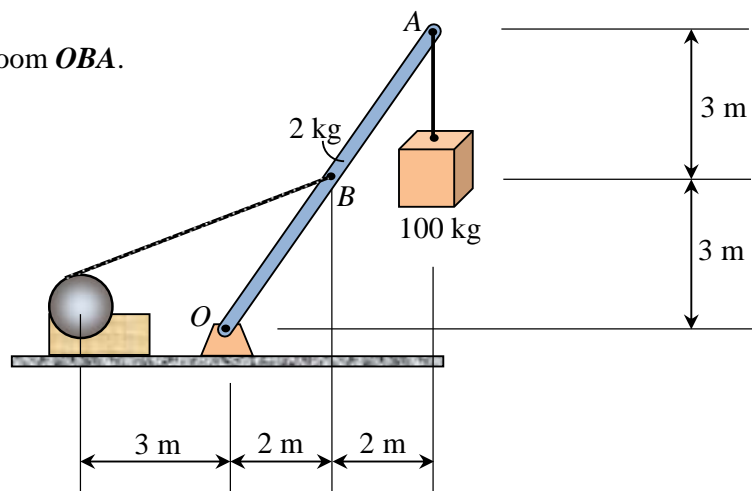
$$\Rightarrow \underline{\underline{m = 30.6 \text{ kg}}} \text{ Ans.}$$

Question # 1(d) (2.5 Marks)

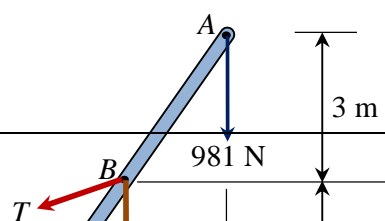
Draw the free body diagram (FBD) of 2kg-boom OBA .

(Show the correct directions of all forces)

Solution



Free body diagram of 2kg-boom OBA :



Student name

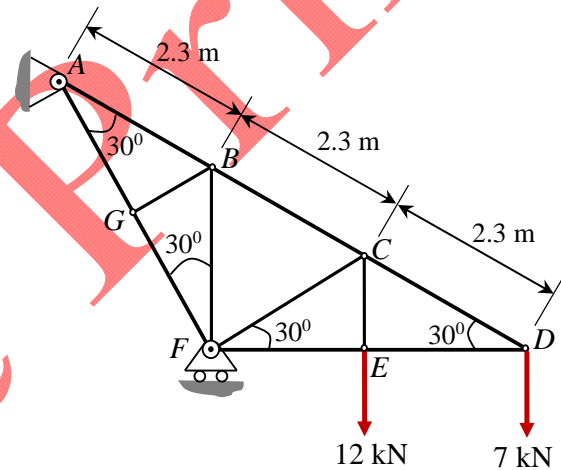
Marks obtained
for Q.2

Student number

Question # 2 (10 Marks)

For the truss and loading shown in the figure:

- a) Calculate the support reactions at pin **A** and roller **F**.
- b) Identify the all zero-force members.
- c) Calculate the forces in members **AB** and **AG** by using method of joints
- d) Calculate the forces in members **CB**, **CF** and **EF** by using method of sections
(Specify whether **Tension** or **Compression**)



Solution

a) Reactions:

$$\rightarrow \Sigma F_x = 0 \Rightarrow \underline{A_x = 0} \quad \text{Ans.}$$

$$CCW(+) \Sigma M_A = 0$$

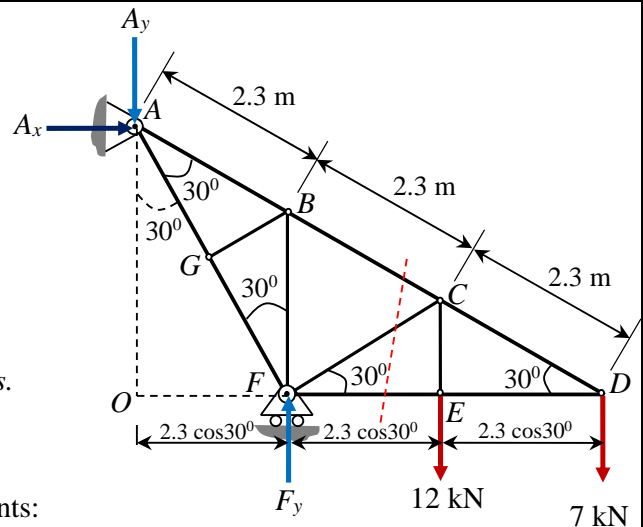
$$\Rightarrow F_y \times 2.3 \cos 30^\circ - 12 \times 4.6 \cos 30^\circ - 7 \times 6.9 \cos 30^\circ = 0$$

$$\Rightarrow \underline{F_y = 45 \text{ kN} \uparrow} \quad \text{Ans.}$$

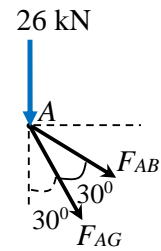
$$\uparrow \Sigma F_y = 0 \Rightarrow -A_y + 45 - 12 - 7 = 0 \Rightarrow \underline{A_y = 26 \text{ kN} \downarrow} \quad \text{Ans.}$$

b) Zero force members: **BG** and **BF**

c) Forces in the members **AB** and **AG** using method of joints:



$$\begin{aligned} \uparrow \Sigma F_y = 0 &\Rightarrow -F_{AG} \cos 30^\circ - F_{AB} \cos 60^\circ - 26 = 0 \Rightarrow F_{AG} = -(0.58F_{AB} + 30) \\ \rightarrow \Sigma F_x = 0 &\Rightarrow F_{AB} \sin 60^\circ + F_{AG} \sin 30^\circ = 0 \Rightarrow F_{AB} \sin 60^\circ - (0.58F_{AB} + 30) \sin 30^\circ = 0 \\ F_{AB} (\sin 60^\circ - 0.58 \sin 30^\circ) - 15 &= 0 \Rightarrow \underline{F_{AB} = 26 \text{ kN (T)}} \quad \text{Ans.} \\ \therefore F_{AG} = -(0.58 \times 26 + 30) &= -45 \text{ kN} \Rightarrow \underline{F_{AG} = -45 \text{ kN (C)}} \quad \text{Ans.} \end{aligned}$$



d) Forces in the members CB , CF and EF using method of sections:

Cut the truss into two parts through the section shown above, and consider the right part of the truss.

$$EC = 2.3 \sin 30^\circ = 1.15 \text{ m}$$

$$CCW(+) \Sigma M_D = 0 \Rightarrow F_{CF} \cos 30^\circ \times 1.15 + F_{CF} \sin 30^\circ \times 2.3 \cos 30^\circ + 12 \times 2.3 \cos 30^\circ$$

$$\Rightarrow \underline{F_{CF} = -12 \text{ kN (C)}} \quad \text{Ans.}$$

$$\uparrow \Sigma F_y = 0 \Rightarrow F_{CB} \sin 30^\circ - (-12) \sin 30^\circ - 12 - 7 = 0 \Rightarrow \underline{F_{CB} = 26 \text{ kN (T)}} \quad \text{Ans.}$$

$$\rightarrow \Sigma F_x = 0 \Rightarrow -F_{EF} - 26 \cos 30^\circ - (-12) \cos 30^\circ = 0 \Rightarrow \underline{F_{EF} = -12.1 \text{ kN (C)}} \quad \text{Ans.}$$

Student name

Marks obtained
for Q.3

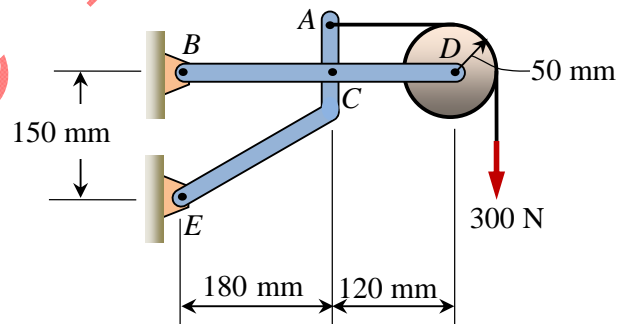
page 4/4

Student number

Question # 3 (10 Marks)

For the frame shown in the figure:

- Find the reactions at the pin supports B and E respectively.
- Draw the free body diagrams (FBD) for each member.
- Determine the horizontal and vertical components of force at C .



Solution

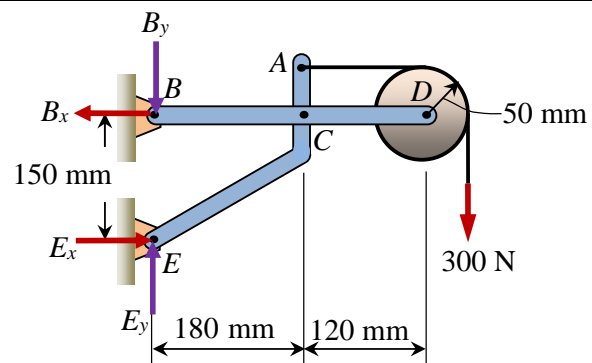
a) Reactions:

$$CCW(+) \Sigma M_E = 0 \Rightarrow$$

$$B_x \times 150 - 300 \times 350 = 0 \Rightarrow \underline{B_x = 700 \text{ N}} \leftarrow \text{Ans.}$$

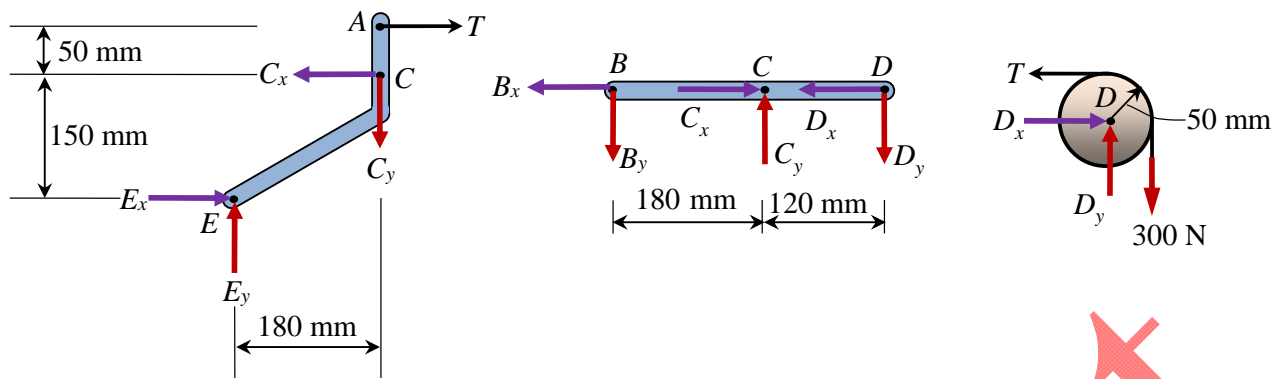
$$\rightarrow \Sigma F_x = 0 \Rightarrow E_x - 700 = 0 \Rightarrow \underline{E_x = 700 \text{ N}} \rightarrow \text{Ans.}$$

$$\uparrow \Sigma F_y = 0 \Rightarrow E_y - B_y - 300 = 0 \Rightarrow B_y = E_y - 300$$



As the number of unknowns are more than the numbers of independent equilibrium equations, reaction components E_y and B_y will be obtained from the free body diagrams of individual members in part (c).

b) Free Body Diagrams:



a – Contd.) Remaining reaction components: From member ECA
 $CCW(+)\Sigma M_C = 0 \Rightarrow 700 \times 150 - E_y \times 180 - 300 \times 50 = 0 \Rightarrow E_y = 500 \text{ N}$ Ans.

$$\therefore B_y = E_y - 300 = 500 - 300 \Rightarrow B_y = 200 \text{ N} \text{ Ans.}$$

(c) Horizontal and vertical components of the force at C: From member ECA

$$\overset{+}{\rightarrow} \Sigma F_x = 0 \Rightarrow -C_x + E_x + T = 0 \Rightarrow -C_x + 700 + 300 = 0 \Rightarrow C_x = 1000 \text{ N} \text{ Ans.}$$

$$\overset{+}{\uparrow} \Sigma F_y = 0 \Rightarrow -C_y + E_y = 0 \Rightarrow -C_y + 500 = 0 \Rightarrow C_y = 500 \text{ N} \text{ Ans.}$$