King Saud University College of Engineering Civil Engineering Department

CE 431: Highway Engineering
Tutorial Note 3: Chapter 7
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7.1 Given $\Delta=35^{\circ}, R=1,350 \mathrm{ft}$, and the PI station $75+28.10$, compute the curve data and the station of the PT using conventional US units. Compute the deflection angles at even $100-\mathrm{ft}$ stations.

$$
\begin{array}{lr}
\text { PC Sta. }=\text { PI Sta. }-T & \text { PT Sta. }=\text { PC Sta. }+L \\
T=R \tan \frac{\Delta}{2} & L=\frac{2 \pi R \Delta}{360}
\end{array}
$$

$T=1350 \tan \frac{35}{2}=425.65 \mathrm{ft}$
$L=\frac{2 \pi \times 1350 \times 35}{360}=824.67 \mathrm{ft}$
PC Sta. $=7528.1-425.65=7102.45 \mathrm{ft} \rightarrow \rightarrow 71+02.45$
PT Sta. $=7102.45+824.67=7927.12 \mathrm{ft} \rightarrow \rightarrow 79+27.12$
The deflection angle to the P.T. is $\Delta / 2$.
The deflection angle to intermediate stations is proportional to the distance from the P.C.
The distance to station $72+00$ is $=7200-7102.45=97.55 \mathrm{ft}$.
Deflection angle $=\frac{\Delta}{2} \times \frac{79.55}{824.67}=2^{\circ} 4^{\prime} 12^{\prime \prime}$
Other deflection angles are computed similarly:

| Station | Deflection Angle <br> (degrees-minutes-seconds) |
| :---: | :---: |
| $72+00$ | $2^{\circ} 04^{\prime} 12^{\prime \prime}$ |
| $73+00$ | $4^{\circ} 11^{\prime} 32^{\prime \prime}$ |
| $74+00$ | $6^{\circ} 18^{\prime} 51^{\prime \prime}$ |
| $75+00$ | $8^{\circ} 26^{\prime} 11^{\prime \prime}$ |
| $76+00$ | $10^{\circ} 33^{\prime} 30^{\prime \prime}$ |
| $77+00$ | $12^{\circ} 40^{\prime} 49^{\prime \prime}$ |
| $78+00$ | $14^{\circ} 48^{\prime} 09^{\prime \prime}$ |
| $79+00$ | $16^{\circ} 55^{\prime} 28^{\prime \prime}$ |
| $79+27.12$ | $17^{\circ} 30^{\prime} 0^{\prime \prime}$ |

7.2 Given a horizontal curve with a radius of 410 m , a $\Delta$ angle of $32^{\circ}$, and PI station of $1+120.744$, compute the curve data and the station of the PT. compute the deflection angles at even $\mathbf{2 0} \mathbf{- m}$ stations.

$$
\begin{array}{lr}
\text { PC Sta. }=\text { PI Sta. }-T & \text { PT Sta. }=\text { PC Sta. }+L \\
T=R \tan \frac{\Delta}{2} & L=\frac{2 \pi R \Delta}{360}
\end{array}
$$

$T=410 \tan \frac{32}{2}=117.566 \mathrm{~m}$
$L=\frac{2 \pi \times 410 \times 32}{360}=228.987 \mathrm{~m}$
PC Sta. $=1120.744-117.566=1003.178 m \rightarrow \rightarrow 1+003.178$
PT Sta. $=1003.178+228.987=1232.165 m \rightarrow \rightarrow 1+232.165$
The deflection angle to the P.T. is $\Delta / 2$.
The deflection angle to intermediate stations is proportional to the distance from the P.C.
The distance to station $1+020.000$ is $=(1020.000)-(1003.178)=16.822 \mathrm{~m}$.
Deflection angle $=\frac{\Delta}{2} \times \frac{16.822}{228.987}=1^{\circ} 10^{\prime} 31^{\prime \prime}$
Other deflection angles are computed similarly:

| Station | Deflection Angle <br> (degrees-minutes-seconds) |
| :---: | :---: |
| $1+020$ | $1^{\circ} 10^{\prime} 31^{\prime \prime}$ |
| $1+040$ | $2^{\circ} 34^{\prime} 22^{\prime \prime}$ |
| $1+060$ | $3^{\circ} 58^{\prime} 13^{\prime \prime}$ |
| $1+080$ | $5^{\circ} 22^{\prime} 04^{\prime \prime}$ |
| $1+100$ | $6^{\circ} 45^{\prime} 55^{\prime \prime}$ |
| $1+120$ | $8^{\circ} 9^{\prime} 46^{\prime \prime}$ |
| $1+140$ | $9^{\circ} 33^{\prime} 37^{\prime \prime}$ |
| $1+160$ | $10^{\circ} 57^{\prime} 27^{\prime \prime}$ |
| $1+180$ | $12^{\circ} 21^{\prime} 18^{\prime \prime}$ |
| $1+200$ | $13^{\circ} 45^{\prime} 09^{\prime \prime}$ |
| $1+220$ | $15^{\circ} 09^{\prime} 00^{\prime \prime}$ |
| $1+232.165$ | $16^{\circ} 00^{\prime} 00^{\prime \prime}$ |

7.3 What superelevation rate would you recommend for a roadway with a design speed of 75 mph and a radius of curvature of $\mathbf{1 , 4 0 0} \mathrm{ft}$ ? Assume $\boldsymbol{f}=\mathbf{0 . 1 1}$.
$0.01 e+f=\frac{V^{2}}{15 R} \rightarrow \rightarrow e=\left(\frac{V^{2}}{15 R}-f\right) \times 100=\left(\frac{75^{2}}{15 \times 1400}-0.11\right) \times 100=15.79 \%$
Based on Table 7-4 and Figure 7-8, this superelevation rate is too large for highway design.
Change design speed or R .
7.4 What superelevation rate would you recommend for a roadway with a design speed of $100 \mathrm{~km} / \mathrm{hr}$ and a radius of curvature of 500 m ? Assume $\mathrm{f}=\mathbf{0 . 1 1}$.
$0.01 e+f=\frac{V^{2}}{127 R} \rightarrow \rightarrow e=\left(\frac{V^{2}}{127 R}-f\right) \times 100=\left(\frac{100^{2}}{127 \times 500}-0.11\right) \times 100=4.75 \%$
Based on Table 7-4 and Figure 7-8, this superelevation rate is acceptable for highway design.
7.5 A 1-mile racetrack is to be designed with a $1 / 4-$ mile turns at each end. Determine the superelevation rate for a design speed of 70 mph , assuming $f=\mathbf{0 . 2 0}$.

$$
\begin{aligned}
& L=0.25 \mathrm{mi} \times \frac{5280 f t}{1 m i}=1320 f t \quad L=\frac{2 \pi R \Delta}{360} \rightarrow R=\frac{360 L}{2 \pi \Delta}=\frac{360 \times 1320}{2 \pi \times 180}=420.17 \mathrm{ft} \\
& 0.01 e+f=\frac{V^{2}}{15 R} \rightarrow \rightarrow e=\left(\frac{V^{2}}{15 R}-f\right) \times 100=\left(\frac{70^{2}}{15 \times 420.17}-0.2\right) \times 100=57.75 \%
\end{aligned}
$$

7.6 A 1-km racetrack is to be designed with turn 250 m in length at each end. Determine the superelevation rate you would recommend for a design speed of $140 \mathrm{~km} / \mathrm{hr}$, assuming $f=0.20$.

$$
\begin{aligned}
& L=250 \mathrm{~m} \\
& L=\frac{2 \pi R \Delta}{360} \rightarrow R=\frac{360 L}{2 \pi \Delta}=\frac{360 \times 250}{2 \pi \times 180}=79.578 \mathrm{~m} \\
& 0.01 e+f=\frac{V^{2}}{127 R} \rightarrow \rightarrow e=\left(\frac{V^{2}}{127 R}-f\right) \times 100=\left(\frac{140^{2}}{127 \times 79.578}-0.2\right) \times 100=173.9 \%
\end{aligned}
$$

7.7 A plus 5.1 percent grade intersects a minus 2.8 grade at station $68+70$ at an elevation of 327.5 ft . Calculate the centerline elevation at every $\mathbf{1 0 0}-\mathrm{ft}$ station for $500-\mathrm{ft}$ vertical curve.

PVC Sta. $=$ PVI $-\frac{L}{2}=6870-\frac{500}{2}=6620 \mathrm{ft} \rightarrow \rightarrow 66+20$
PVT Sta. $=P V C+L=6620+500=7120 \mathrm{ft} \rightarrow \rightarrow 71+20$
$E_{P V C}=E_{P V I}-\frac{G}{100} \times \frac{L}{2}=327.50-\frac{5.1}{100} \times \frac{500}{2}=314.75 \mathrm{ft}$
The distance to station $67+00$ is $=6700-6620=80 \mathrm{ft}$.
$E_{x}=E_{P V C}+\frac{G_{1}}{100} x+\frac{\left(G_{2}-G_{1}\right) x^{2}}{200 L}$
$E_{67+00}=314.75+\frac{5.1}{100} \times 80+\frac{(-2.8-5.1) \times 80^{2}}{200 \times 500}=318.32 \mathrm{ft}$
Other elevations are computed similarly:

| Station | Elevation, ft |
| :---: | :---: |
| $67+00$ | 318.32 |
| $68+00$ | 321.37 |
| $69+00$ | 322.84 |
| $70+00$ | 322.72 |
| $71+00$ | 321.03 |
| $71+20$ | 319.0 |

7.8 A plus 2.8 percent grade intersects a minus 5.1 grade at station $2+087.224$ at an elevation of 190.28m. Calculate the centerline elevation at every $20-\mathrm{m}$ station for $150-\mathrm{m}$ vertical curve.

PVC Sta. $=$ PVI $-\frac{L}{2}=2087.224-\frac{150}{2}=2012.224 \rightarrow \rightarrow 2+012.224$
PVT Sta. $=P V C+L=2012.224+150=2162.224 \rightarrow \rightarrow 2+162.224$
$E_{P V C}=E_{P V I}-\frac{G}{100} \times \frac{L}{2}=190.28-\frac{2.8}{100} \times \frac{150}{2}=188.180 \mathrm{~m}$
The distance to station $2+020$ is $=2020-2012.224=7.8 \mathrm{~m}$.
$E_{x}=E_{P V C}+\frac{G_{1}}{100} x+\frac{\left(G_{2}-G_{1}\right) x^{2}}{200 L}$
$E_{2+020}=188.180+\frac{2.8}{100} \times 7.8+\frac{(-5.1-2.8) \times 7.8^{2}}{200 \times 150}=188.382 \mathrm{~m}$
Other elevations are computed similarly:

| Station | Elevation, ft |
| :---: | :---: |
| $2+020$ | 188.382 |
| $2+040$ | 188.754 |
| $2+060$ | 188.916 |
| $2+080$ | 188.867 |
| $2+100$ | 188.608 |
| $2+120$ | 188.138 |
| $2+140$ | 187.457 |
| $2+160$ | 186.566 |
| $2+162.2$ | 186.455 |

7.9 A vertical parabolic curve is to be used as a sag curve, and it is desired to know the location and elevation of low point. The curve is 750 ft long, and the minus grade of 3.6 percent intersects with the plus grade of 6.2 percent at station $240+80.00$. Calculate the low point of the curve if the intersection at station $240+80.00$ is at elevation 426.84 .

PVC Sta. $=P V I-\frac{L}{2}=24080-\frac{750}{2}=23705 \mathrm{ft} \rightarrow \rightarrow 237+05$
PVT Sta. $=P V C+L=23705+750=24455 \mathrm{ft} \rightarrow \rightarrow 244+55$
$x_{m}=\left|\frac{G_{1} L}{G_{2}-G_{1}}\right|=\left|\frac{-3.6 \times 750}{6.2-(-3.6)}\right|=275.51 \mathrm{ft}$
$E_{P V C}=E_{P V I}-\frac{G}{100} \times \frac{L}{2}=426.84-\frac{-3.6}{100} \times \frac{750}{2}=440.34 \mathrm{ft}$
$E_{x_{m}}=E_{P V C}+\frac{G_{1}}{100} x_{m}+\frac{\left(G_{2}-G_{1}\right) x_{m}^{2}}{200 L}$
$E_{x_{m}}=440.34+\frac{-3.6}{100} \times 275.51+\frac{(6.2-(-3.6)) \times 275.51^{2}}{200 \times 750}=435.38 \mathrm{ft}$
Low point Sta. $=P V C+x_{m}=23705+275.51=23980.51 \mathrm{ft} \rightarrow \rightarrow 239+80.51$
7.10 A vertical parabolic curve is to be used under a grade separation structure. The curve is $\mathbf{2 5 0} \mathbf{~ m}$ long, and the minus grade of 3.8 percent intersects with the plus grade of 5.4 percent at station $0+120.424$. Calculate the low point of the curve if the intersection at station $\mathbf{0 + 1 2 0 . 4 2 4}$ is at elevation $\mathbf{2 3 0 . 0 8 5}$.

PVC Sta. $=$ PVI $-\frac{L}{2}=120.424-\frac{250}{2}=-4.576 m \rightarrow 0-004.576$
PVT Sta. $=P V C+L=-4.576+250=245.424 m \rightarrow \rightarrow 0+245.424$
$x_{m}=\left|\frac{G_{1} L}{G_{2}-G_{1}}\right|=\left|\frac{-3.8 \times 250}{5.4-(-3.8)}\right|=103.261 \mathrm{~m}$
$E_{P V C}=E_{P V I}-\frac{G}{100} \times \frac{L}{2}=230.085-\frac{-3.8}{100} \times \frac{250}{2}=234.835 \mathrm{~m}$
$E_{x_{m}}=E_{P V C}+\frac{G_{1}}{100} x_{m}+\frac{\left(G_{2}-G_{1}\right) x_{m}^{2}}{200 L}$
$E_{x_{m}}=234.835+\frac{-3.8}{100} \times 103.261+\frac{(5.4-(-3.8)) \times 103.261^{2}}{200 \times 250}=232.873 \mathrm{~m}$
Low point Sta. $=P V C+x_{m}=-4.576+103.261=98.685 m \rightarrow \rightarrow 0+098.685$
7.11 Calculate the stopping sight distance over the crest of a $1,500 \mathrm{ft}$ vertical curve with a plus grade of 4.4 percent and a minus grade of 2.3 percent.
$A=G_{2}-G_{1}=-2.3-4.4=-6.7 \%$
Assume $S<$ L per equation 7-11a,
$L=\frac{A S^{2}}{2158} \rightarrow \rightarrow S=\sqrt{\frac{2158 L}{A}}=\sqrt{\frac{2158 \times 1500}{6.7}}=695.08 \mathrm{ft}$
Check assumption: 695.08 < 1500, OK
Therefore, $\mathbf{S}=\mathbf{6 9 5 . 0 8} \mathbf{f t}$ and equation 7-11a applies. [Otherwise, use equation 7-12a and check that assumption].
7.12 Calculate the stopping sight distance over the crest of a 450 m vertical curve with a plus grade of 5.6 percent and a minus grade of 3.2 percent.
$A=G_{2}-G_{1}=-3.2-5.6=-8.8 \%$
Assume $S<L$ per equation 7-11b,
$L=\frac{A S^{2}}{658} \rightarrow \rightarrow S=\sqrt{\frac{658 L}{A}}=\sqrt{\frac{658 \times 450}{8.8}}=183.433 \mathrm{~m}$
Check assumption: 183.433 < 450, OK
Therefore, $\mathrm{S}=183.433 \mathrm{~m}$ and equation $7-11 \mathrm{~b}$ applies. [Otherwise, use equation $7-12 \mathrm{~b}$ and check that assumption].
7.13 Calculate the passing sight distance over the crest described in problem 7.11.

Assume S < L per equation 7-9

$$
\begin{aligned}
& L=\frac{A S^{2}}{100\left[\sqrt{2 h_{1}}+\sqrt{2 h_{2}}\right]^{2}} \\
& 1500=\frac{6.7 \times S^{2}}{100[\sqrt{2 \times 3.5}+\sqrt{2 \times 3.5}]^{2}} \rightarrow \rightarrow S=791.75 \mathrm{ft}
\end{aligned}
$$

Check assumption: 791.75 < 1500, OK,There, $\mathbf{S}=\mathbf{7 9 1 . 7 5} \mathbf{f t}$ and equation 7-9 applies. [Otherwise, use equation 7-10 and check that assumption]

### 7.14 Calculate the passing sight distance over the crest described in problem 7.12.

Assume S < L per equation 7-9
$L=\frac{A S^{2}}{100\left[\sqrt{2 h_{1}}+\sqrt{2 h_{2}}\right]^{2}}$
$450=\frac{8.8 \times S^{2}}{100[\sqrt{2 \times 1.08}+\sqrt{2 \times 1.08}]^{2}} \rightarrow \rightarrow S=210.195 \mathrm{~m}$
Check assumption: $210.195<450$, OK, There, $\mathbf{S}=\mathbf{2 1 0 . 1 9 5} \mathbf{~ m}$ and equation 7-9 applies.
7.15 Given a horizontal curve with a $1,360 \mathrm{ft}$ radius, estimate the minimum length of spiral necessary for a smooth transition from tangent alignment to circular curve.

Assume design speed, $V=65 \mathrm{mph}$. By equation 7-5a,
$L_{s}=\frac{3.5 V^{3}}{R C}=\frac{3.5 \times 65^{3}}{1360 \times 4}=159.02 \mathrm{ft}$
7.16 Given a horizontal curve with a 410 m radius, estimate the minimum length of spiral necessary for a smooth transition from tangent alignment to circular curve. The design speed is $90 \mathrm{~km} / \mathrm{hr}$.

By equation 7-5b,
$L_{s}=\frac{0.0214 V^{3}}{R C}=\frac{0.0214 \times 65^{3}}{1360 \times 1.2}=31.709 \mathrm{~m}$

